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ABSTRACT

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Keywords:

Energy storage Linear programming problem Optimization Simplex-method Energy-saving, improving energy efficiency, and finding a new efficient way to use energy are considered as an urgent problem in over the world. In this paper, we consider the economics of energy use in combination with energy storage units where two forms of electricity exist in the power system. Then the problem of optimizing the installation capacity (to optimize the investment costs for energy storage) is presented and investigated in connection with the conversion systems. The topic opens a very significant result, including the introduction of a mathematical model to calculate the simulation in optimizing the installation capacity of the equipment in the system, multi-source power, as well as voltage and power stability benefits.

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1. INTRODUCTION

This paper considers the problem, which related to the research project to improve economic and technical efficiency in the current period of the Russian Federation power systems. In fact, there have a two-price mechanism exists (electricity prices vary between peak and off-peak times) it is possible to receive some degree of energy cost savings when installing units. energy storage [1-12]. In this paper, we proposed the followings problems as 1) The level of cost savings of how energy is achieved and how to control the operation of the UPS to save costs; 2) The correlation of the capacity components of the load, the capacity of the supply network, the capacity of the converter and the capacity of the energy storage to how to save maximum cost; 3) the ability to stabilize the voltage in the system.

These problems are the aim of this paper. The investment and operation of an energy storage device are significant for the owner of the load if it reduces energy costs. The power supply system can also finance the investment and operation of storage devices if it helps reduce the unevenness of the network. In optimizing energy consumption costs, it means that we will consider the issue of energy efficiency from the owners' perspective [13, 14].

This paper develops and solves the problem of determining the minimum cost of energy consumption when the ratios of power consumption of load components, converter power, and storage capacity amount. Assume that energy consumers consume only active power. The load characteristics are

maximum during the day and vary between days in a week. The capacity of the load consists of two parts; the fixed component includes essential loads, and the component can be changed, that is, can shift the time of use. The unit, the load, and the power from the grid are connected to the distribution control system (including charge/discharge and converter controllers). To solve this problem, we put the problem of solving linear programming problems with thousands of variables. The system's working mode is simulated for a week with a discrete distance of 12 minutes. The results of the problem have proved that the use of UPSs brings economic efficiency of 5-25%, without taking into account the cost of the system, storage devices, and associated energy converters. The assessment of the overall economic efficiency of this topic must be investigated for all the above factors. In the general conclusion of the paper confirms that at present due to the price of the variable and energy storage devices is still high compared to the cost savings brought by the two-price mechanism, the use of such devices are inefficient. However, the topic opens a very significant result, including the introduction of a mathematical model to calculate the simulation in optimizing the installation capacity of the equipment in the system, multi-source power, as well as voltage and power stability benefits. The rest of the paper is constructed as the following. The mathematical formulation is proposed in the second section. In the third section, some numerical results and discussions are presented and analyzed. The last section draws some conclusions from this research.

2. MATHEMATICAL FORMULATION

In this section, we give the quantities describe the problem and their limitations. First, to make it clear, we introduce these quantities as continuous functions over time, then we take a discrete step over time, and all quantities describe the problem become vectors whose components will be valuable at discrete points. For UPS, $P_{\text{bat max}}$, $P_{\text{bat}}(t)$, $W_{\text{bat max}}$, $W_{\text{bat}}(t)$ are corresponding to the capacity of the power converter suitable to connect the unit and the grid. Instantaneous generating/receiving capacity of the unit must be synchronized with the capacity of the inverter. The quantities describe the electrical storage part are,

$$-P_{\text{bat max}} \le P_{\text{bat}}(t) \le P_{\text{bat max}} \tag{1}$$

$$0 \le W_{\text{hat}}(t) \le W_{\text{hat max}} \tag{2}$$

where
$$W_{\text{bat}}(t) = \int_{0}^{t} P_{\text{bat}}(t) dt + W_{\text{bat}}(0)$$

It should be noted that the maximum capacity and capacity of the battery must be taken according to the charge/discharge limits of the battery, within which the UPS operates correctly, i.e. depending on the charge/discharge characteristics according to the condition of the energy-saving unit. These limits are different for each type of battery used as shown in [15]. If $W_{\text{bat}}(0) = 0$, then

$$W_{\text{bat}}(t) = \int_{0}^{t} P_{\text{bat}}(t) dt$$
(3)

Regarding the capacity taken from the grid $P_{\text{net max}}$, $P_{\text{net}}(t)$ are the maximum power allowed from the grid and instantaneous power, we have:

$$0 \le P_{\text{net}}(t) \le P_{\text{net max}} \tag{4}$$

For load, $P_{\text{load}}(t)$ is the instantaneous power of the initial load. As mentioned above, there are two components $P_{\text{const}}(t)$ and $P_{\text{var}}(t)$ as shown in the below equation:

$$P_{\text{load}}(t) = P_{\text{const}}(t) + P_{\text{var}}(t)$$
(5)

where $P_{\text{const}}(t)$ is the load component is always present and cannot be changed at use time, i.e. its graph does not change after optimization; $P_{\text{var}}(t)$ is the component may change when it is used, i.e. its graph will be

changed after optimization. The load energy W_{load} consumed from t = 0 to t = T, with T the simulation time, in this problem we simulate the system operating within a week, we have [16].

$$W_{\text{load}} = \int_{0}^{T} P_{\text{load}}(t) dt = \int_{0}^{T} P_{\text{const}}(t) dt + \int_{0}^{T} P_{\text{var}}(t) dt = W_{\text{const}} + W_{\text{var}}$$
(6)

where

$$W_{\rm var} = \int_0^T P_{\rm var}(t) dt \tag{7}$$

Power balance equation is given by:

$$P_{\text{bat}}(t) + P_{\text{net}}(t) = P_{\text{load}}(t) \text{ or } -P_{\text{var}}(t) + P_{\text{bat}}(t) + P_{\text{net}}(t) = P_{\text{const}}(t)$$
(8)

We take into account the vectors P_{var} , P_{bat} , P_{net} , whose elements are values corresponding to quantities $P_{\text{var}}(t)$, $P_{\text{bat}}(t)$, $P_{\text{net}}(t)$ at discrete point s t_k : { $t_1 = 0$; $t_k = t_{k-1} + h$; $t_N = T$ }, with h is the observation step during simulation - 12 minutes. Next, to make writing quantities simpler, we denote $P_{\text{var},k} = P_{\text{var}}(t_k)$, $P_{\text{bat},k} = P_{\text{bat}}(t_k)$, $P_{\text{net},k} = P_{\text{net}}(t_k)$. Then we have:

$$\mathbf{P}_{\text{var}} = \begin{bmatrix} P_{\text{var},1} \\ P_{\text{var},2} \\ M \\ P_{\text{var},N} \end{bmatrix}; \quad \mathbf{P}_{\text{bat}} = \begin{bmatrix} P_{\text{bat},1} \\ P_{\text{bat},2} \\ M \\ P_{\text{bat},N} \end{bmatrix}; \quad \mathbf{P}_{\text{net}} = \begin{bmatrix} P_{\text{net},1} \\ P_{\text{net},2} \\ M \\ P_{\text{net},N} \end{bmatrix}$$

Suppose K (t) - the price of electricity purchased from the grid changes according to the time of use according to a known rule. In this problem, we take the electricity price in the city of Saint-Petersburg, May 2019. Daytime prices are 7.6 cents / kWh and at night 4.4 cents / kWh. Similarly, we include the price vector so that we can write equations in the form of matrices. The cost for the energy storage unit will be calculated from the capacity and the optimal battery capacity received during the simulations. The objective function can be formulated as

$$f = \mathbf{K}' \mathbf{P}_{\text{net}} \to \min \tag{9}$$

The limits in (8) indicate the fact that the total power taken from the grid and the unit is equal to the load capacity at any given time. Hence, in vector form, (7) is rewritten as

$$W_{\text{var}} = \int_{0}^{T} P_{\text{var}}(t) dt = \sum_{n=1}^{N} P_{\text{var},n} h = h \cdot \mathbf{1}^{t} \cdot \mathbf{P}_{\text{var}} = B_{1} = W_{\text{load}} - W_{\text{const}}$$

where $\mathbf{1}$ – Unit vectors of the corresponding size. From the hypothesis that the initial state $W_{\text{bat}}(0)$ of the unit and the same $W_{\text{bat,N}}$ - the remaining power of the unit are equal, we get the limits:

$$W_{\text{bat}} = W_{\text{bat}}(0) + h \cdot \mathbf{1}' \cdot \mathbf{P}_{\text{bat}} = W_{\text{bat},1} + B_2 = W_{\text{bat},N} \text{ hay } h \cdot \mathbf{1}' \cdot \mathbf{P}_{\text{bat}} = B_2 = W_{\text{bat},N} - W_{\text{bat}}(0)$$

Then (8) can be reformulated as the following

$$\begin{bmatrix} -\mathbf{E} & -\mathbf{E} & \mathbf{E} \end{bmatrix} \cdot \begin{bmatrix} \mathbf{P}_{\text{var}} \\ \mathbf{P}_{\text{bat}} \\ \mathbf{P}_{\text{tiet}} \end{bmatrix} = \begin{bmatrix} P_{\text{const},1} \\ P_{\text{const},2} \\ \mathbf{M} \\ P_{\text{const},N} \end{bmatrix} = \mathbf{B}_{3}$$

Where \mathbf{E} – matrix unit. Finally, we have

$$\begin{bmatrix} h \cdot \mathbf{1}^{t} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & h \cdot \mathbf{1}^{t} & \mathbf{0} \\ -h \cdot \mathbf{E} & -h \cdot \mathbf{E} & h \cdot \mathbf{E} \end{bmatrix} \cdot \begin{bmatrix} \mathbf{P}_{\text{var}} \\ \mathbf{P}_{\text{bat}} \\ \mathbf{P}_{\text{net}} \end{bmatrix} = \begin{bmatrix} B_{1} \\ B_{2} \\ \mathbf{B}_{3} \end{bmatrix} \Rightarrow \mathbf{A}\mathbf{X} = \mathbf{B}$$
(10)

where $\mathbf{0}$ – vectors have no corresponding dimensions.

In (3), we denote that the UPS and converters have no loss then

$$0 \le W_{\text{bat,n}} = W_{\text{bat}}(0) + \sum_{i=1}^{n} P_{\text{bat},i} h \le W_{\text{bat max}}; \quad n = \overline{1, N}$$

Or in the matrix form as

$$-\mathbf{1} \cdot W_{\text{bat}}(0) \le h \begin{bmatrix} 1 & 0 & L & 0 \\ 1 & 1 & L & 0 \\ M & M & 0 & M \\ \frac{1}{144442} \underbrace{I_{444442}}_{s} \begin{bmatrix} P_{\text{bat},1} \\ P_{\text{bat},2} \\ M \\ P_{\text{bat},N} \end{bmatrix} \le \mathbf{1} \cdot \left(W_{\text{bat max}} - W_{\text{bat}}(0) \right)$$

Or
$$-\mathbf{1} \cdot \frac{W_{\text{bat}}(0)}{h} \leq \mathbf{S} \cdot \mathbf{P}_{\text{bat}} \leq \mathbf{1} \cdot \frac{W_{\text{bat}\max} - W_{\text{bat}}(0)}{h}$$
, then

$$\begin{bmatrix} \mathbf{S} \\ -\mathbf{S} \end{bmatrix} \mathbf{P}_{\text{bat}} \leq \frac{1}{h} \begin{bmatrix} \mathbf{1} \cdot \left(W_{\text{bat}\max} - W_{\text{bat}}(0) \right) \\ \mathbf{1} \cdot W_{\text{bat}}(0) \end{bmatrix}$$

Finally, we have

$$\begin{bmatrix} \mathbf{0} \\ \mathbf{S} \\ -\mathbf{S} \\ \mathbf{0} \end{bmatrix} \cdot \begin{bmatrix} \mathbf{P}_{\text{var}} \\ \mathbf{P}_{\text{bat}} \\ \mathbf{P}_{\text{net}} \end{bmatrix} \leq \frac{1}{h} \begin{bmatrix} \mathbf{0} \\ \mathbf{1} \cdot (W_{\text{bat max}} - W_{\text{bat}}(0)) \\ \mathbf{1} \cdot W_{\text{bat}}(0) \\ \mathbf{0} \end{bmatrix} \Rightarrow \mathbf{C} \mathbf{X} \leq \mathbf{D}$$
(11)

We re-list the entire mathematical model of the problem to be solved as

$$\begin{cases} 0 \le P_{\text{var}}(t) \le P_{\text{net max}} - P_{\text{load max}} \\ -P_{\text{bat max}} \le P_{\text{bat}}(t) \le P_{\text{bat max}} \\ 0 \le P_{\text{net}}(t) \le P_{\text{net max}} \end{cases} \begin{bmatrix} \mathbf{0} \\ -\mathbf{1} \cdot P_{\text{bat max}} \\ \mathbf{0} \end{bmatrix} \le \begin{bmatrix} \mathbf{P}_{\text{var}} \\ \mathbf{P}_{\text{bat}} \\ \mathbf{P}_{\text{net}} \end{bmatrix} \le \begin{bmatrix} \mathbf{1} \cdot (P_{\text{load}} - P_{\text{const}}) \\ \mathbf{1} \cdot P_{\text{bat max}} \\ \mathbf{1} \cdot P_{\text{net max}} \end{bmatrix}$$
(12)

The problem (12) is formed from the problem (9) with conditions in the form of equality (10) and inequalities (11) related to linear programming problems, and to solve problems of this type, we apply the simplex method as in [17-21]. The total number of variables when simulating the system within a week with a 12-minute observation step is 2520 variables.

3. NUMERICAL RESULTS AND DISCUSSION

Figure 1(a) corresponds to the case when $P_{var}(t) = P_{const}(t)$, when the power output is interchangeable and cannot be changed equally. As you can see, the actual UPS is almost unused (curve $W_{bat}(t)$). The capacity of the UPS can then be reduced to 10 kWh. The economic benefits are about 20% of the original. Figure 1(b) corresponds to the case $P_{var}(t) = 0.2P_{const}(t)$. It can be seen that the UPS is used very

actively (maximum battery capacity is 45kWh, and its capacity is 15kW), activities consume more energy comfortably for consumers. UPSs and converters are used very actively. Accordingly, the losses in the equipment and the depreciation costs of these devices (not included by us) can be significant [22-25]. To verify the results graphically, we turn to relative values as shown in (13).



Figure 1. Optimize electricity consumption costs when: a) - $P_{\text{var}}(t) = P_{\text{const}}(t)$ and b) $P_{\text{var}}(t) = 0.2P_{\text{const}}(t)$

In Table 1, we present the results of several dozen calculations performed for different ratios concerning the relative values above. On the vertical axis of all graphs, the percentage of energy cost savings percentage (hereinafter F) is consumed from the network. The third line in each cell of Table 1 gives the ratios of the word parameters (13). As can be seen from the graphs, the increase in converter capacity (corresponding to the capacity of the unit) reduces the cost of electricity consumption (F increases). This result is easily predictable. However, as can be seen from the diagrams (first panel of table 1) such as F = 25% when the load capacity of 100kW is more than 150kWh. The analysis of the first cell of table 1 has shown that F decreases as the maximum power from the grid decrease. This is explained by the fact that, at the maximum power allowed from the grid, there is not enough power per charge on the unit, and of course, its efficiency is low even with the capacity of the converter as well as of the large UPS. When the maximum power available from the grid increases, F increases linearly with the capacity of the unit. The second cell shows the effect of quantities on the efficiency of the use of uninterruptible power supplies. Here F also decreases as the maximum power taken from the grid decreases, An analysis of the last cell

Energy cost savings based on the uninterruptible ... (Phu Tran Tin)

of the table also shows a similar result. Thus, the general conclusion is that to save significant energy costs can only be achieved with the maximum capacity of the high grid.



Table 1. The level of economic efficiency depends on relative quantities (13)

4. CONCLUSION

The results show that even with reasonably simple assumptions, the use of a UPS helps to reduce energy costs by 5-25%. At the same time, the capital cost of additional equipment (the unit and the converter connecting it to the network) is estimated to be significant. The energy efficiency is significant (10 percent or more) when the variable power component of the load accounts for 10 percent or more of the maximum power taken from the grid. Therefore, the question of the efficiency of energy cost savings when using the UPS and the two-price mechanism receives the answer (according to our research) is insignificant because the operating costs and the costs of investing in consumer electricity storage devices are equivalent to the costs saved by increasing electricity consumption (including saving electricity) at times of low prices and reducing consumption. Electricity at a time of high prices. The situation is likely to change significantly if the owner has the opportunity to use alternative (renewable) energy sources. We intend to consider this issue further.

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