

## Noise uncertainty effect on multi-channel cognitive radio networks

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### ABSTRACT

Achieving high throughput is the most important goal of cognitive radio networks. The main process in cognitive radio is spectrum sensing that targets getting vacant channels. There are many sensing methods like matched filter, feature detection, interference temperature and energy detection which is employed in the proposed system; however, energy detection suffers from noise uncertainty. In this paper a study of throughput under noise fluctuation effect is introduced. The work in this paper proposes multi-channel system; the overall multi-channel throughput is studied under noise fluctuation effect. In addition, the proficiency of the network has been examined under different number of channels and sensing time with noise uncertainty.

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## 1. INTRODUCTION

Cognitive radio (CR) using spectrum sensing technique can be used to solve the issues of spectrum underutilization [1-3]. In cognitive radio field the secondary user (SU) detect the primary user bands and depends on this decision it selects the spectrum for its communication [4-6]. The CR system could be single channel or Multi-channel, choosing the system according to needs, because each system has benefits and drawbacks. In CR system, the secondary user have to detect the vacant channel [7-10]. When a vacant channel is detected, the secondary system will access that channel. However, spectrum sensing as an urgent issue in CR, demands the secondary user to powerfully and successfully sense the existence of primary signal [11-13]. Spectrum management is the core function in CR; contains various processes such as spectrum sensing (SS), spectrum decision and spectrum handoff. SS is one of the most important advantages of CR sensors network from old wireless sensor networks (WSNs). It overtakes few opticals like low SNR for primary users, time dispersion, channel fading, and noise uncertainty [14-16].

Maximum throughput of the network has been studied for several numbers of optimal CR users. Ahead of the issue of threshold mismatch of energy detectors with noise power uncertainty, a cooperative spectrum sensing method with dynamic dual threshold is expressed in [17]. In [18] the optimal sensing technique has been offered maximizing channel throughput. The offered optimal cooperative spectrum sensing (CSS) settings for wide-band sensing channels is investigated and determined specifically with few simple however dependable techniques. In [19] a new spectrum sensing adaptive algorithm considering noise uncertainty has been proposed. In [20] the researchers studied noise uncertainty effect and fading on the detection performance. In [21] researchers offered an evidence-theory based fusion rule for cooperative energy detection in existence of noise power uncertainty.

Authors in [22] introduce a modified two-stage detection technique that relay on energy detection under noise uncertainty. Researchers in [23] examined the act of spectrum sensing, they proposed that the throughput reaches maximum at optimal sensing time. To certify how processes of primary user is not disturbed, it has to keep the spectrum-sensing capability to get vacant channel when SU needs it. Therefore, the proficiency of sensing the existence of primary signals remains important. Spectrum sensing contains several methods (e.g. Matched filter, energy detection, feature detection, interference temperature). In [24] authors studied and analyzed the proficiency of energy detector spectrum sensing method with parameters affecting its performance on Nakagami-m fading channels under noise uncertainty and without. Authors in [25] proposed a different system of two stages spectrum sensing, Adaptive two-stage spectrum sensing (ATSS), with noise uncertainty effect ATSS is a modification of a predictable two stage spectrum sensing when the decision threshold of each stage is adapted on the distance, expected noise variance and concluded noise uncertainty range. Noise uncertainty affect the performance of multi-channel is studied with different number of channel and decides which best number ti get high throughput.

## 2. RESEARCH METHOD

This paper will introduce multi-channel system which has several channels that studies how noise uncertainty affects the system performance to get the best scenario. Our proposed system here consists of multi-channel (as each SU stands for one channel in proposed system) Spectrum sensing performance has been offered to get best number of CR users [23], sensing time, Throughput R under noise fluctuation effect. The received signal for every CR is sampled at sampling frequency  $f_s$ .

As shown in Figure 1, every cognitive frame consists of spectrum sensing time ( $t$ ) and data transmission time ( $T-t$ ), where  $T$  is the total frame time. Consider that the distribution function for noise can be summarized in an interval  $[(1 + \rho)^{-1}\sigma_{vi}^2, (1 + \rho)\sigma_{vi}^2]$ , where  $\sigma_{vi}^2$  noise variance for  $i$ th channel and  $\rho$  is a parameter that quantizes the level of the uncertainty. Assuming  $K$  is the number of samples existing during  $t$ . Therefore the number of samples,  $K=t.f_s$  [23, 25]. The probability of detection and probability of false alarm for multi-channel system under noise uncertainty effect can be written as

$$P_f = \underset{\sigma_{vi}^2 \in [(1+\rho)^{-1}\sigma_{vi}^2, (1+\rho)\sigma_{vi}^2]}{\operatorname{argmax}} \quad \frac{1}{2} \operatorname{erfc} \left( \frac{1}{\sqrt{2}} \left( \frac{\lambda}{\sigma_{vi}^2} - 1 \right) \sqrt{t.f_s} \right) \quad (1)$$

$$P_d = \underset{\sigma_{vi}^2 \in [(1+\rho)^{-1}\sigma_{vi}^2, (1+\rho)\sigma_{vi}^2]}{\operatorname{argmax}} \quad \frac{1}{2} \operatorname{erfc} \left( \frac{1}{\sqrt{2}} \left( \frac{\lambda}{\sigma_{vi}^2} - \gamma_i - 1 \right) \sqrt{\frac{t.f_s}{2\gamma_i + 1}} \right) \quad (2)$$

Solving (1), (2) under noise we will get

$$P_f = \frac{1}{2} \operatorname{erfc} \left( \frac{1}{\sqrt{2}} \left( \frac{\lambda}{(1+\rho)\sigma_{vi}^2} - 1 \right) \sqrt{k} \right) \quad (3)$$

$$P_d = \frac{1}{2} \operatorname{erfc} \left( \frac{1}{\sqrt{2}} \left( \frac{\lambda}{(1+\rho)^{-1}\sigma_{vi}^2} - \gamma_i - 1 \right) \sqrt{\frac{k}{2\gamma_i + 1}} \right) \quad (4)$$

$$P_f = \frac{1}{2} \operatorname{erfc} \left( \frac{1}{\sqrt{2}} \left( \frac{\lambda}{\beta\sigma_{vi}^2} - 1 \right) \sqrt{k} \right) \quad (5)$$

$$P_d = \frac{1}{2} \operatorname{erfc} \left( \frac{1}{\sqrt{2}} \left( \frac{\beta\lambda}{\sigma_i^2} - \frac{\gamma_i}{\beta} - 1 \right) \sqrt{\frac{k}{\frac{2\gamma_i}{\beta} + 1}} \right) \quad (6)$$

where  $\beta = 1 + \rho$ ,  $\gamma_i$  represents the SNR at the CR receiver for  $i$ th channel and  $\lambda$  represents the decision threshold. The throughput for the total false alarm probability in the absence of PU is [20, 23].

$$R_0 = \frac{T-\tau}{T} C_0 (1 - Q_{ft}) P(H_0) \quad (7)$$

where  $C_0$  represents the throughput in the absence of PU. The throughput for the total missed detection probability is

$$R_1 = \frac{T-\tau}{T} C_1 (1 - Q_{dt}) P(H_1) \quad (8)$$

where  $C_1$  represents the throughput in the existence of PU. From [20, 23] we get

$$Q_{ft} = (1 - P_f)^n \quad (9)$$

$$Q_{dt} = (1 - Q_d)^n \quad (10)$$

The total throughput R of the CR network can be expressed from previous discussion as

$$R = \frac{T-t}{T} (C_0 (1 - Q_{fopt}) P(H_0) + C_1 (1 - Q_{dopt}) P(H_1)) \quad (11)$$

As R is a function of  $P_f$  and  $P_d$ , it will be affected by changing noise fluctuations. So the throughput will be decreased when probability of false alarm increased or probability of detection decreased. Studying n that represents the number of CRs in spectrum sensing. To compare this proposed system and [17] under noise fluctuation equation of the system will be

$$P_f = \frac{1}{2} \operatorname{erfc}(\operatorname{erfc}^{-1}(2P_d) \sqrt{2\gamma_i \beta + 1} + \frac{m}{2} \gamma_i \beta) \quad (12)$$

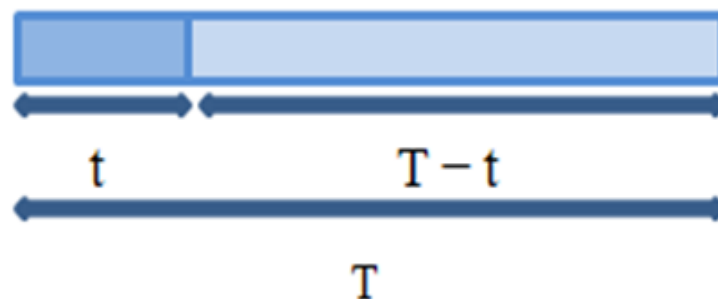


Figure 1. Cognitive frame structure

### 3. RESULTS AND ANALYSIS

Now we are going to investigate the noise fluctuation on the ED ROC. As assumed above the noise variance with uncertainty changed in the interval  $\sigma_{vi}^2 \epsilon[\sigma_{vi}^2/\beta, \beta\sigma_{vi}^2]$  where  $\beta > 1$  and changed from 1.259 to 1.585 [22]. BPSK modulation has been used by primary user to transmit its data with 3 MHz bandwidth. The maximum time for which the secondary user uninformed of the primary action is selected as  $F_s, T=3000$  [19]. The frame time of detection cycle is 100ms and target detection probability is 0.7. We choose  $P(H_0)=0.8, P(H_1)=0.2, C_0=6.6582$  and  $C_1=6.6137$ . Figure 2 shows the relation between throughput and SNR at different values for noise fluctuations. We observe that when noise increasing by 30% and SNR=-12dB, the throughput R tends to zero, which means system at  $\beta=1.3$  still working until SNR reaches -12dB.

Figure 3 explains the throughput relation with number of CRs operating at  $t=2$  ms. studying at average number of CRs =5. At  $\beta=1$ , the throughput  $R=3.5$ . At  $\beta=1.05$ , the throughput  $R=2.5$ , which means by increasing  $\beta$  by 5% throughput decreasing by 29%. At  $\beta=1.1$ , the throughput  $R=1.8$ , which means by increasing by 10% throughput decreasing by 50%. At  $\beta=1.3$ , the throughput  $R=0.5$ , which means by increasing by 30% throughput decreasing by 86%.

Figure 4 shows the relation between throughput and sensing time with different number of CRs. (a) at  $n=15$ , we observe that when noise increasing by 30%, the throughput tends to zero. (b) at  $n=10$ , we observe when increasing noise by 30%, the throughput decreasing by 70%. (c) at  $n=5$ , we observe when increasing noise by 30%, the throughput decreasing by 60%. From that we can say at  $n=10$ , this is the best number for CRs in this system under noise effect.

Figure 5 shows a comparison with [17] under noise fluctuation  $\beta=1.3$  we obtained that at  $t=3$ ms,  $P_f$  in reference system reaches to 0.55 which means it affected from noise with 30% but in our proposed system that  $P_f$  reaches 0.43 which means it affected from noise with 14%. This means that our proposed system is better than reference system.

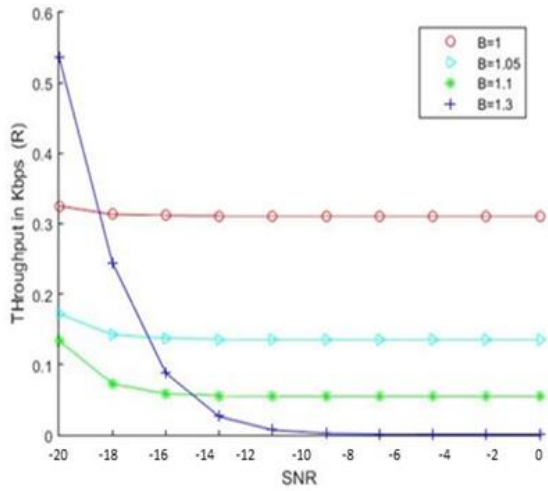


Figure 2. Throughput vs SNR

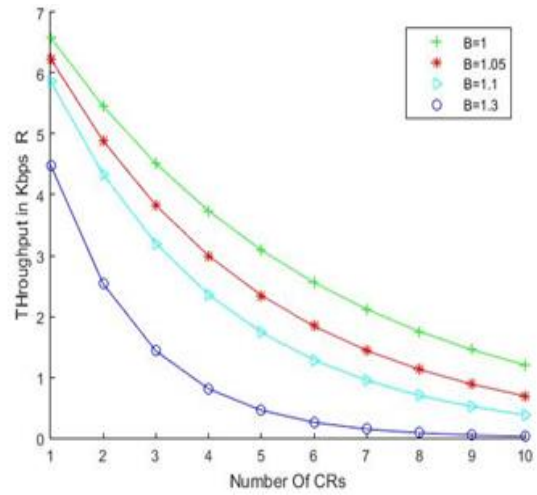
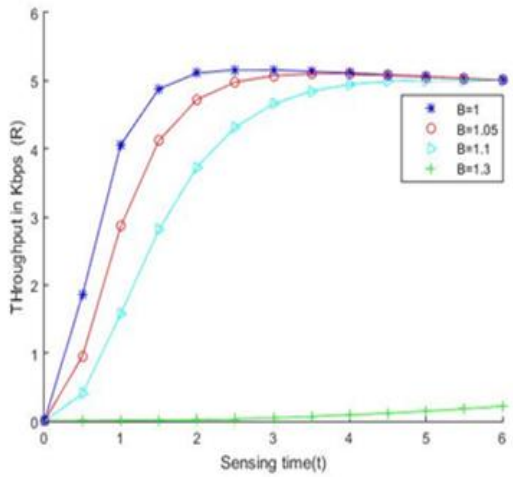
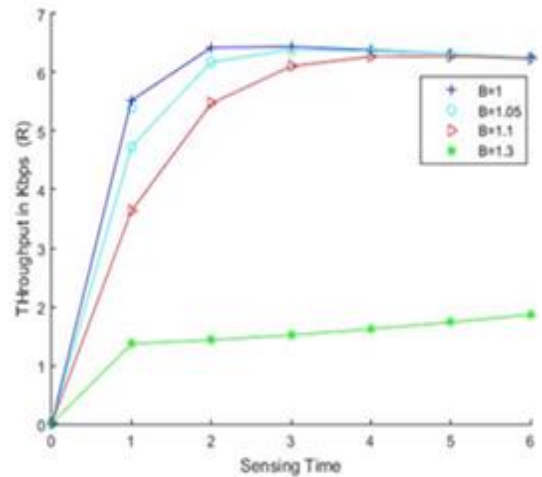


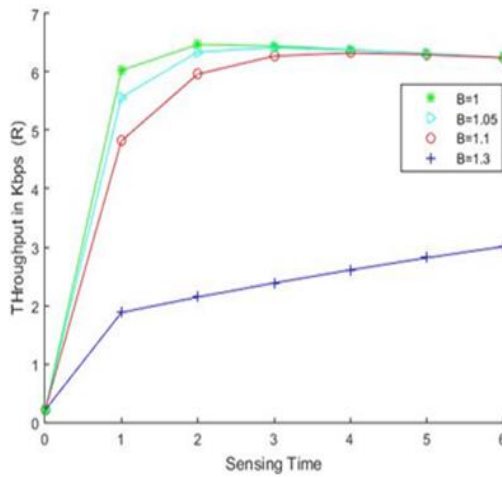
Figure 3. Throughput vs number of CRs



(a)



(b)



(c)

Figure 4. The relation between throughput R and sensing time t, (a) No. of CRs=15, (b) No. of CRs=10, (c) No. of CRs=5

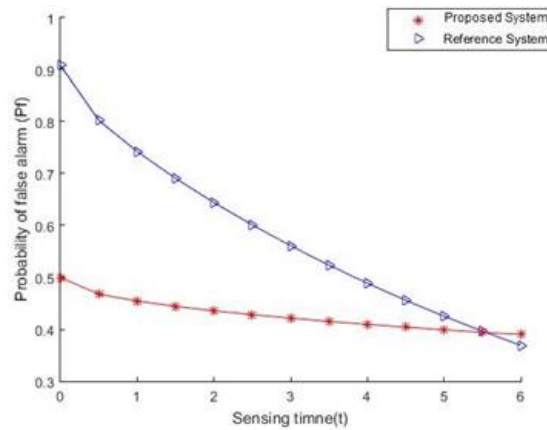


Figure 5. Sensing time vs Pf

#### 4. CONCLUSION

The noise uncertainty effect on the performance of multi-channel is studied and we observe that, in multi-channel, for our system it is good to work with 10 channels to achieve reasonable throughput in relation with SNR or with sensing time by increasing noise up to 30%. From that we can say, the proposed system can reach reasonable throughput in single or multi-channel under noise that increase of 30% effect.

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