

## Fuzzy gain scheduling control apply to an RC Hovercraft

Huu Khoa Tran<sup>1</sup>, Pham Duc Lam<sup>2</sup>, Tran Thanh Trang<sup>3</sup>, Xuan Tien Nguyen<sup>4</sup>, Hoang-Nam Nguyen<sup>5</sup>

<sup>1</sup>Industry 4.0 Center, National Taiwan University of Science and Technology, Taiwan

<sup>1</sup>Center for Cyber-Physical System Innovation, National Taiwan University of Science and Technology, Taiwan

<sup>2</sup>Faculty of Mechanical, Electrical, Electronic and Automotive Engineering, Nguyen Tat Thanh University, Vietnam

<sup>3</sup>Faculty of Engineering and Technology, Van Hien University, Vietnam

<sup>4</sup>Faculty of Electronics and Telecommunications, Saigon University, Vietnam

<sup>5</sup>Modeling Evolutionary Algorithms Simulation and Artificial Intelligence, Faculty of Electrical and Electronics Engineering, Ton Duc Thang University, Vietnam

---

### Article Info

#### Article history:

Received Jun 16, 2019

Revised Nov 27, 2019

Accepted Dec 12, 2019

---

#### Keywords:

Fuzzy gain scheduling

ITAE criterion

PID control

RC Hovercraft

---

### ABSTRACT

The Fuzzy Gain Scheduling (FGS) methodology for tuning the Proportional-Integral-Derivative (PID) traditional controller parameters by scheduling controlled gains in different phases, is a simple and effective application both in industries and real-time complex models while assuring the high achievements over pass decades, is proposed in this article. The Fuzzy logic rules of the triangular membership functions are exploited on-line to verify the Gain Scheduling of the Proportional-Integral-Derivative controller gains in different stages because it can minimize the tracking control error and utilize the Integral of Time Absolute Error (ITAE) minima criterion of the controller design process. For that reason, the controller design could tune the system model in the whole operation time to display the efficiency in tracking error. It is then implemented in a novel Remote Controlled (RC) Hovercraft motion models to demonstrate better control performance in comparison with the PID conventional controller.

*Copyright © 2020 Institute of Advanced Engineering and Science.  
All rights reserved.*

---

### Corresponding Author:

Hoang-Nam Nguyen,

Modeling Evolutionary Algorithms Simulation and Artificial Intelligence,

Faculty of Electrical and Electronics Engineering, Ton Duc Thang University,

19 Nguyen Huu Tho street, Tan Phong ward, District 7, Ho Chi Minh City, Vietnam.

Email: [nguyenhoangnam@tdtu.edu.vn](mailto:nguyenhoangnam@tdtu.edu.vn)

---

## 1. INTRODUCTION

PID controller is one of the most popular controller and is applied in many operation conditions due to its simple structure and effectiveness [1]. In literature, PID controllers is literally divided into two main categories. The first is the controller gains, which have been tuned or chosen by traditional ways, are fixed during the running time and Ziegler-Nichols tuning methodology is the best representative off-line formula [2]. In this category, the PID controller gain designs are simple and cannot always effective, it is also mean that different gains give the different system's response. The controller designs in the second category have a similarity structure, however, its parameters are adapted on-line throughout the operating time. With the purpose of getting the optimal performance in terms of accuracy, stability and satisfactory response, the control system must carefully consider the compromise between the settling time and the overshoot. Thus, the PID parameters design of the new operating conditions have spent lots of time for tuning [1].

Gain scheduling is regarded as an excellent controller design approaches in [2, 3]. It can be classified as "divide-and-conquer" control procedure type, in which some linear sub-problems are combined to implement the non-linear design operation [2] and various gains of controllers are utilized in every regions. The critical point in building a good controller is determining the scheduling variables, which have suitable priori insight to the process dynamics [3]. State variables, errors and their changing rates are

commonly used variables [4-7]. Designers can determine the regions by magnitudes of scheduling variables or establish the regions by local linearization of dynamic model in the neighbor of some special operating points [2, 3].

In this work, we intend to create a simple and effective control system for quick positioning utilizing PID controller's characteristics. For fast convergence of the controlled system, we set gains to have large magnitude as scheduling variables are high. Similarly, for system to be settling with less fluctuation, we keep the gains have low magnitude when scheduling parameters are low. This scheme practically works in tracking. Unfortunately, this conventional approach can not satisfy the fast-rising response requirement in the beginning phase since both the time derivative and its error are too low to obtain acceptable large control output. Therefore, time delay is not very different with traditional PID controller. Actually, the setpoints in each movement could be the most suitable scheduling variable that satisfies our goal. Orelind et al. [8] first designed optimal PID gain schedule for the hydro-generators system. In [9], Beaven et al. use the gain scheduling of setpoints in high-speed independent 2-phase drive. Situm et al. [10] applied this method to servo pneumatic position control. Later, Dounis et.al. [11] and Vijaya Chandrakala et.al. [12] exploited adaptive fuzzy gain scheduling to the energy systems. Next, Kankgasabai and Jaya [13] and Ahmad et. al. [14] then control the PID gains with this technique for MIMO process control. Currently, Yao and Lakerveld employ this method to microfluidic devices [15]. Yilmaz et.al. also exploit the gain-scheduling PID controllers for Z-source inverter [16].

In our research, we proposed to apply fuzzy gain scheduling technology for designing a motion controller. Firstly, we created a PID controller that has large magnitudes of proportional and integral gains and low magnitude of derivative gain in the motion initialization period. Later, the fuzzy gain scheduling technique is applied to slowly increase the derivative gain as well as reduce the proportional and integral gains until another setpoint is met. The first setpoint is then chosen at the ending part of the trapezoid curve of constant speed region. By this way, the speed could be kept constant as less fluctuation as possible in the unchanged speed region. We aim to build a moving system to come to the target location and obtain settling state in a short period. The key technique in proposed approach is the fuzzy logic-based technique of gain scheduling. After finding the suitable regions for implementing gain scheduling. The suitable controller gains are determined to achieve our goal. The Hovercraft motion model [17-22] is utilized to demonstrate the effectiveness of this novel method. It is then compared with the traditional PID auto-tuning control.

This work is presented as follows: In section 2, the development of fuzzy gain scheduling scheme for dynamic reset of PID controllers is proposed. In section 3, we present how to configure the RC Hovercraft model. In section 4, we present the simulation results of the proposed controller system performance. Finally, conclusions are discussed in section 5.

## 2. RESEARCH METHOD

### 2.1. PID controller

In literature, discrete-time PID controller is usually defined as:

$$u(n) = K_P e(n) + K_I T_S \sum_{i=1}^n e(i) + K_D \frac{e(n) - e(n-1)}{T_S} \quad (1)$$

where,  $u(n)$  is known as the control signal and  $e(n)$  represents the error input.  $T_s$  is the sampling period. Moreover, the proportional, integral and derivative gains are represented by  $K_P$ ,  $K_I$  and  $K_D$ , respectively. These gains can be tuned to output various responses of a specific process.

### 2.2. Fuzzy gain scheduling

In many schemes of gain scheduling design process, suitable regions for the variable need to be determined [7]. The T-curve (trapezoidal velocity curve) as shown in Figure 1, which has three parts: acceleration  $t \in [0, t_1]$ , constant speed  $t \in [t_1, t_2]$ , and deceleration  $t \in [t_2, t_3]$ , is chosen to find out the regions. In the deceleration phase  $[t_2, t_3]$ , we apply fuzzy logic technique (inference rule) to change these parameters linearly and continuously. The two membership functions  $\mu_1$  and  $\mu_2$  are demonstrated in Figure 2. The Fuzzy logic inference rules are expressed as followings:

$$\begin{aligned} &\text{If } p < p_1, \text{ then } \mu_1=1 \text{ and } \mu_2=0. \\ &\text{If } p_1 \leq p \leq p_2, \text{ then } \mu_1 = \frac{p_2 - p}{p_2 - p_1} \text{ and } \mu_2 = \frac{p - p_1}{p_2 - p_1}. \\ &\text{If } p > p_2, \text{ then } \mu_1=0 \text{ and } \mu_2=1. \end{aligned}$$

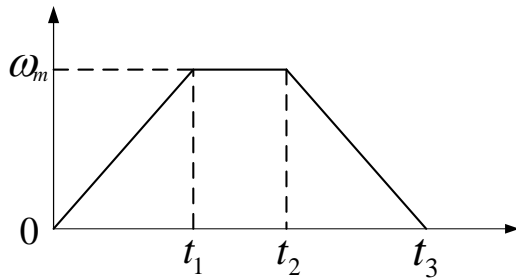


Figure 1. Trapezoidal velocity/position curve

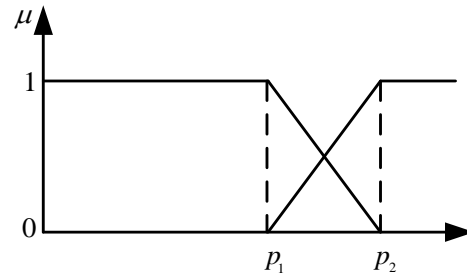


Figure 2. Membership functions vs set points

The desired positions of the moving model, which based on the above fuzzy logic rules, are employed to evaluate the response performances. The proposed Fuzzy-PID control system block diagram, which included two fuzzy logic membership functions, is demonstrated as shown in Figure 3. Specifically, weighting  $\mu_i$  of the  $i$ -th membership function depends on the current command position  $p=y_d(t)$ . We choose  $\mu_1=1$ , and  $\mu_2=0$  in phase I of initial PID gains. In phase II,  $\mu_1 = \frac{p_2 - p}{p_2 - p_1}$ , and  $\mu_2 = \frac{p - p_1}{p_2 - p_1}$  are chosen as the blended gains. The second set of initial gains in phase III are  $\mu_1 = 0$ , and  $\mu_2=1$ . The PID gains can be calculated in any time point and the subscripts 1 and 2 of the PID gains represent the membership function I and II in (2).

$$\begin{cases} K_P = \sum_i \mu_i \cdot K_{P_i} \\ K_I = \sum_i \mu_i \cdot K_{I_i} \\ K_D = \sum_i \mu_i \cdot K_{D_i} \end{cases} \quad (2)$$

The standard criterion ITAE [23-25], which are multiply by time at each sampling data and express as  $ITAE = \int_0^\infty t \cdot |e(t)| \cdot dt$ , is chosen as the eye to show the less error for both controller design methods Ziegler-Nichols and Fuzzy Gain Scheduling, which applied to the RC Hovercraft motion models.

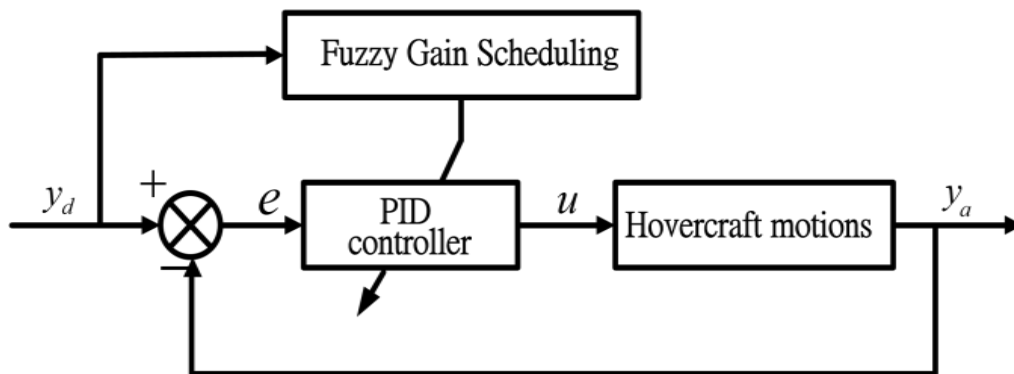


Figure 3. The fuzzy gain scheduling-PID controller diagram

### 3. RC HOVERCRAFT CONFIGURATION MODEL

A hovercraft, also known as an air cushion vehicle (ACV), consists of rotors and a cushion. The hovercraft can float and cruise smoothly on various surfacec such as rough land, water, sand beach, as well as the ice [17-22] due to the inside air pressure of the cushion. The lift propeller provides the internal cushion pressure for operating a long period of time. A hovercraft turning typically is done by directing the thrust air flow through rotor duct fan and steering by a tilt servo motor placed at the rear. The subsequent momentum generated is used to maneuver the craft. Though many modern technologies are utilized,

the hovercraft requires an advanced maneuvering system to achieve optimized performance. Hence, this paper presents an agile autonomous hovercraft model. It has a single tilt servo motor, which is equipped on the fin tail. The rotor duct fan is settled along the y-axis and the propeller is attached along the z-axis, as shown in Figure 4.

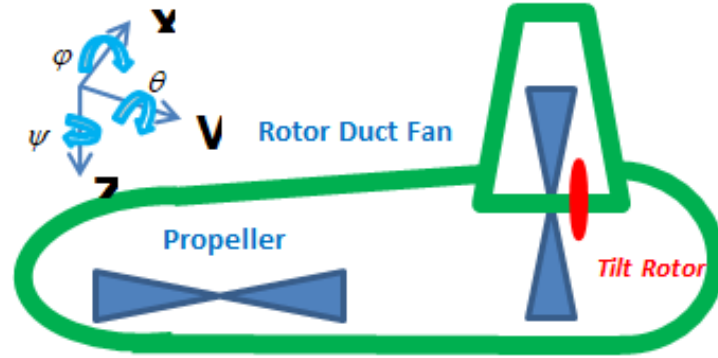


Figure 4. The Hovercraft configuration model

The dynamic of the Hovercraft model is derived from [19-21] and the vehicle is demonstrated utilizing right-hand coordinate system. Additionally, positive x-axis shows the lateral, namely sway motion or surge position. Positive y-axis goes along to the hovercraft body, namely surge motion or sway position. Besides, positive z-axis is oriented downwards. The Hovercraft’s kinematics can be expressed as:

$$\begin{cases} \dot{x} = u \cos \psi - v \sin \psi \\ \dot{y} = v \cos \psi + u \sin \psi \\ \dot{\psi} = r \end{cases} \quad (3)$$

where  $r \in \mathfrak{R}$  is called as angular velocity,  $u \in \mathfrak{R}$  and  $v \in \mathfrak{R}$  are linear velocities in surge direction and sway direction, respectively. Using (1), the kinetic and potential energy are derived to define the Lagrange  $L=T-V$  and by applying Euler-Lagrange formulation:

$$M(q)\dot{q} + C(q, \dot{q})q = \begin{bmatrix} F \\ \tau \\ 0 \end{bmatrix} \quad (4)$$

where  $F \in \mathfrak{R}$  represents the control force along the surge direction,  $\tau \in \mathfrak{R}$  is the torque moment in yaw action. The torque control depends on F and is at right angle to the center line of the hovercraft propeller.

#### 4. RESULTS AND ANALYSIS

The simulation parameters of the Hovercraft are derived from [19-21] and denoted shortly with the mass  $m = 2.1$  kg and the inertia moment  $I = 0.000257$ . Based on the Hovercraft model, the PID gains are chosen in  $[0, 20]$  range. The proposed control performances in Figures 5, 6, and 7 are displayed in each channel: surge position x, sway position y and yaw angle, respectively. We then use Matlab to implement the model. The numerical simulation results have proved that the proposed controllers show significant stability and robust performance response. The proposed Fuzzy Gain Scheduling for PID controller simulation have all received results have the maximum response time, without overshoot and less error, are just after the first second at all. The optimal gains issue is considering in the future work.

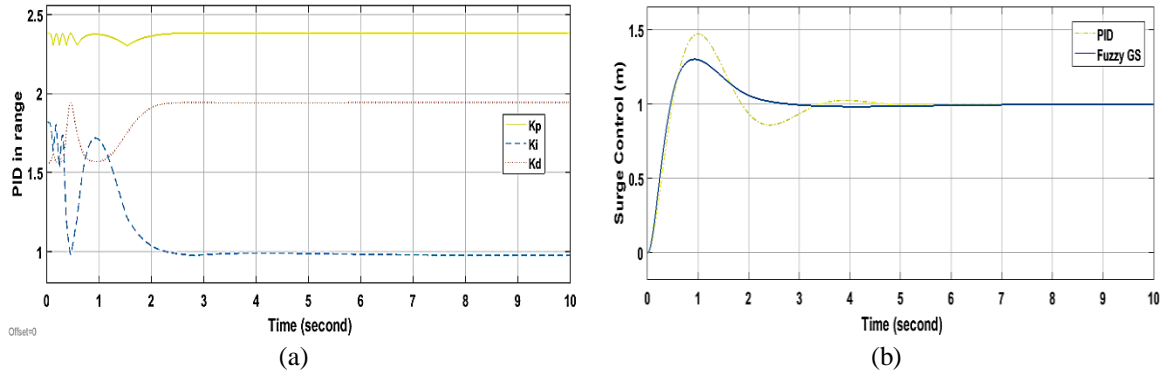


Figure 5. (a) Fuzzy gain scheduling tuning pid gains, (b) surge control

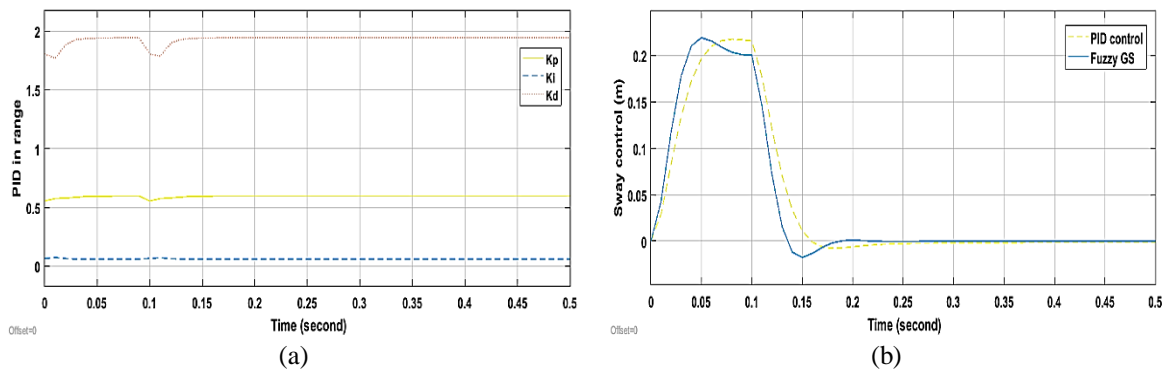


Figure 6. (a) fuzzy gain scheduling tuning PID gains, (b) sway control

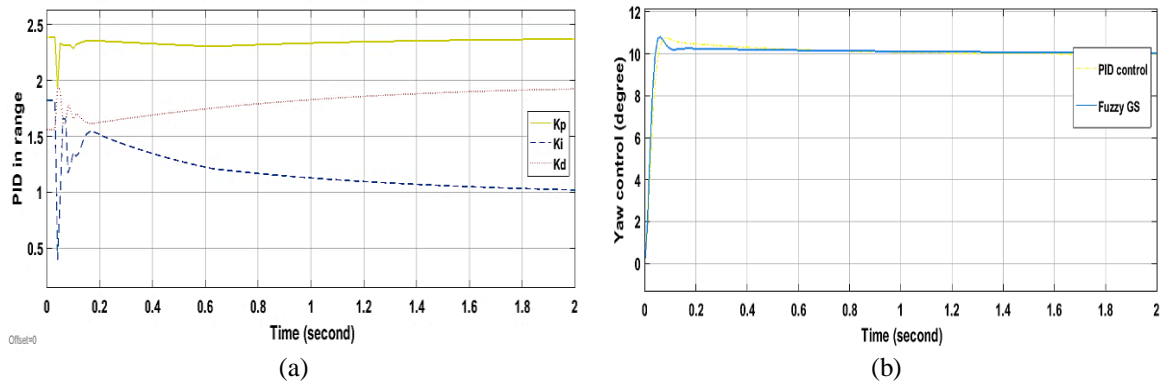


Figure 7. (a) fuzzy gain scheduling tuning PID gains, (b) Steering-yaw control

**5. CONCLUSION**

In this article, the Fuzzy Gain Scheduling is extensively to verify the conventional PID control parameters. The scheme has been tested on the motion models of the RC Hovercraft and the reasonable results are obtained. Thus, the operation time is prominently decreased and the goal of fast positioning is achieved. This method, although is simple but effective in the most control systems. It would be helpful to promote control system.

## ACKNOWLEDGEMENTS

This work was financially supported by the “Center for Cyber-physical System Innovation” from The Featured Areas Research Center Program within the framework of the Higher Education Sprout Project by the Ministry of Education (MOE) in Taiwan.

## REFERENCES

- [1] Z.-Y. Zhao, M. Tomizuka, and S. Isaka, “Fuzzy gain scheduling of PID controllers,” *IEEE Transactions on Systems, Man and Cybernetics*, vol. 23, no. 5, pp. 1392-1398, 1993.
- [2] J. G. Ziegler and N. B. Nichols, “Optimum settings for automatic controllers,” *Transaction of ASME*, vol. 64, pp. 759-768, 1942.
- [3] D. J. Leith, and W. E. Leithead, “Survey of gain-scheduling analysis and design,” *International Journal of Control*, vol. 73, no. 11, pp. 1001-1025, 2000.
- [4] K. H. McNichols, and M. S. Fadali, “Selecting operating points for discrete-time gain scheduling,” *Journal of Computers and Electrical Engineering*, vol. 29, no. 2, pp. 289-301, Mar. 2003.
- [5] K. J. Åström and B. Wittenmark, *Adaptive Control*, 2<sup>nd</sup> edition, Addison-Wesley, 1994.
- [6] C. Ling, and T. F. Edgar, “Experimental verification of model-based fuzzy gain scheduling technique,” *American Control Conference*, vol. 3, pp. 2475-2480, Jun. 1994.
- [7] T. Y. Huang and H. K. Tran, “Optimization of Setpoint-Based Fuzzy Gain Scheduling and Its Application to a Linear Stage,” *7th IEEE Conference on Industrial Electronics and Applications (ICIEA)*, 2012.
- [8] G. Orelind, L. Wozniak, J. Medanic, and T. Whittemore, “Optimal PID gain schedule for hydrogenerators-design and application,” *IEEE Transactions on Energy Conversion*, vol. 4, no. 3, pp. 300-307, 1989.
- [9] R. W. Beaven, M. T. Wright, S. D. Garvey, M. I. Friswell, and D. R. Seaward, “The application of setpoint gain scheduling to high-speed independent drives,” *Control Engineering Practice*, vol. 3, no. 11, pp. 1581-1585, Oct. 1995.
- [10] Z. Situm, D. Pavkovic, B. Novakovic, “Servo pneumatic position control using Fuzzy PID gain scheduling,” *Transactions of the ASME, Journal of Dynamic Systems, Measurement, and Control*, vol. 126, no. 2, pp. 376-387, 2004.
- [11] A. I. Dounis, P. Kofinas, C. Alfodimos and D. Tseles, “Adaptive fuzzy gain scheduling PID controller for maximum power point tracking of photovoltaic system,” *Renewable Energy*, vol. 60, pp. 202-214, 2013.
- [12] Vijaya Chandrakala, S. Balamurugan and K. Sankarannarayanan, “Variable structure fuzzy gain scheduling based load frequency controller for multi area hydro thermal system,” *International Journal of Electrical Power and Energy Systems*, vol. 53, pp. 375-381, 2013.
- [13] N. Kanagasabai and N. Jaya, “Fuzzy Gain Scheduling of PID controller for a MIMO Process,” *International Journal of Computer Application*, vol. 9, no. 10, pp. 13-20, 2014.
- [14] M.A. Ahmad, S.I. Azuma, and T. Sugie, “Performance analysis of model-free PID tuning of MIMO systems based on simultaneous perturbation stochastic approximation,” *Expert Systems with Applications*, vol. 41, no. 14, pp. 6361-6370, 2014.
- [15] Y. Gao and R. Lakerveld, “Experimental validation of scheduled PID control for directed self-assembly of colloidal particles in microfluidic devices,” *In Computer Aided Chemical Engineering*, vol. 44, pp. 2455-2460, 2018.
- [16] A.R. Yılmaz, B. Erol, A. Delibaşı and B. Erkmén, “Design of gain-scheduling PID controllers for Z-source inverter using iterative reduction-based heuristic algorithms,” *Simulation Modelling Practice and Theory*, vol. 94, pp. 162-176, 2019.
- [17] J.R. Amyot, “Hovercraft Technology, Economics and Applications,” *Elsevier Science Publishing Co.*, New York, 1989.
- [18] H. Nakamura, H. Kayanuma, S. Kimura, M. Kosugi, “A new process for small boat production based on aluminum hot-blow forming,” *Journal of Materials Processing Technology*, pp. 196-205, 1997.
- [19] Hebertt Sira-Ramirez and Carlos Aguilar Ibanez, “On the control of the Hovercraft,” *Dynamic and Control*, Kluwer Academic Publishers, vol. 10, pp. 151-163, 2000.
- [20] Rashid, Aras., Kassim, Ibrahim, Jamali, “Dynamic Mathematical Modeling and Simulation Study of Small Scale Autonomous Hovercraft,” *International Journal of Advanced Science and Technology*, vol. 46, Sep. 2012.
- [21] Dictino Chaos, David Moreno-Salinas, Rocío Muñoz-Mansilla, and Joaquin Aranda, “Nonlinear Control for Trajectory Tracking of a Nonholonomic RC-Hovercraft with Discrete Inputs,” *Mathematical Problems in Engineering*, vol. 2013, pp. 1-16 2013.
- [22] D.I. Garcia and W.N. White, “Control design of an unmanned hovercraft for agricultural applications,” *International Journal of Agricultural and Biological Engineering*, vol. 8, no. 2, pp. 72–79, 2015.
- [23] S. Skogestad, “Simple analytic rules for model reduction and PID controller tuning,” *Journal of Process Control*, vol. 13, pp. 291-309, 2003.
- [24] F.G. Martins, “Tuning PID Controllers using the ITAE Criterion,” *International Journal Engineering Education*, vol. 21, no. 5, pp. 867-873, 2005.
- [25] W. Tan, J. Liu, T. Chen, and H.J. Marquez, “Comparison of some well-known PID tuning formulas,” *Computation Chemical Engineering*, pp. 1416–1423, 2006.

**BIOGRAPHIES OF AUTHORS**

**HUU KHOA, TRAN** received Ph.D. degrees in the area of Mechatronics Technology from the Southern Taiwan University of Science and Technology (STUST), Tainan, Taiwan in 2015. He is currently an Assistant Professor at National Taiwan University of Science and Technology (NTUST), Taipei, Taiwan. He has over 15 research papers. His research interests include Artificial Intelligence, Autonomous Robot (UAV, AGV), Decision and Control, Optimization Algorithms, Big Data and Internet of Things.



**Duc-Lam Pham** graduated his Master Degree in Mechatronics Engineering from Ho Chi Minh University of Transport in 2014. He is currently working as Head of Department of Mechatronics Engineering, Nguyen Tat Thanh University (Vietnam). His research interests include automatic control, mechatronics engineering, medical engineering and artificial intelligence.



**Tran Thanh Trang** was born in Vietnam in 1979. He received the B.E and M.E degrees in electronics engineering from Ho Chi Minh city University of Technology, National University Ho Chi Minh city, Vietnam, in 2001 and 2004, respectively, and the Ph.D degree in electronics engineering from Yeungnam University, South Korea in 2012. His research interests is display engineering, photovoltaic systems, optoelectronics and automatic control system.



**Nguyen Xuan Tien** received a Bachelor of Physics - Specialization in Nuclear Electronics from Dalat University in 1988, received a Master's Degree in Mechatronics Engineering from HUTECH University of Technology, Ho Chi Minh City in 2014. Currently, he is pursuing the Ph.D. degree and is a lecturer at Faculty of Electronics and Telecommunications, Saigon University. His research fields including Automation Control, Robotics and Mechatronics systems and applications.



**Hoang-Nam Nguyen** graduated his Ph.D degree in Mechanical Engineering from National Chiao Tung University (Taiwan) in 2017. He is currently working as Lecturer of Faculty of Electrical and Electronics Engineering, Ton Duc Thang University (Vietnam). His research interests include image processing, computer vision, computational mechanics, automatic control and artificial intelligence.