

## Content adaptive single image interpolation based Super Resolution of compressed images

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### ABSTRACT

Image Super resolution is used to upscale the low resolution Images. It is also known as image upscaling. This paper focuses on upscaling of compressed images with interpolation based Single Image Super Resolution technique. A content adaptive interpolation method of image upscaling has been proposed. This interpolation based scheme is useful for single image based Super Resolution methods. The presented method works on horizontal, vertical and diagonal directions of an image separately and it is adaptive to the local content of an image. This method relies only on a single image and uses the content of the original image only; therefore, the proposed method is more practical and realistic. The simulation results have been compared to other standard methods with the help of various performance matrices like PSNR, MSE, MSSIM etc. which indicates the preeminence of the proposed method.

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## 1. INTRODUCTION

In today's time, multimedia content in the digital data is growing day by day, which leads to a very practical challenge of storage and transmission of multimedia content. It is due to the limitations of various resources in different applications. In order to solve the issue specifically, multimedia data is transmitted in the downscaled and compressed form under some standards. However, when it comes to the user side, that multimedia data containing images or videos might have lost its original quality due to downscaling and compression. As far as images are concerned, they mostly exist in downscaled and compressed formats. In addition to images, videos are also compressed in various formats. Furthermore, many time due to heavy quality reduction the original size of images get reduced. Hence, there is always a need of upscaling method for reproducing a good quality image or to increase the number of pixels of images. Upscaling method should not only upgrade the visual appearance but also make the images useful for other applications. Super Resolution (SR) is one the most famous solution for these types of issues which can be achieved in multiple ways. There are many advance ways to implement the SR, but one of the best practical solutions to implement the Super Resolution of images is interpolation, which is less time consuming as well as requires less computation. In many standard practical applications already interpolation is working for upscaling or resizing of images. Interpolation based SR is having many applications, such as medical imaging, HDTV, computer vision, satellite imaging and video surveillance etc.

Interpolation based approach is one of the fastest methods for image Super Resolution. Interpolation based zooming schemes are frequently used in the real-time when working with small images. Nearest neighbour (NN), bilinear and bicubic are the mostly used interpolation techniques [1-3]. These techniques are

non-adaptive, so these are computationally efficient but suffer from the problems of aliasing, blurring; therefore, there are chances that these techniques could be improved further [4, 5]. However, this class of methods could be used practically in many applications due to their simplicity. There are several edge directed and non-linear interpolation schemes which have been developed to minimize the problems faced by non-adaptive interpolation schemes [6-10]. In these techniques, re-sampling information is determined according to the geometrical regularities that again requires the time and increases complexity. Some adaptive interpolation based approaches [11-15] are present in literature but they are also having high computational work or may be limited to a particular type of images. Higher order derivative and other high computation based interpolation methods have also been presented in the literature [16-22]. However, the methods related to the interpolation could be improved further and an effort has been done in this work to implement the interpolation for upscaling or super resolution of images. Consequently, there is always a tradeoff between system complexity and image quality. In this paper, a content adaptive SR method based upon interpolation has been proposed. In this work proposed method works differently for the horizontal, vertical and diagonal directions. Further, in section 2, interpolation based up-scaling has been explained, section 3 presents the proposed method, section 4 deals with results analysis and in the last section 5, the conclusion has been drawn.

## 2. INTERPOLATION BASED IMAGE UP-SCALING

Image interpolation focuses on creating the high resolution image from its lower resolution version of the image. Image interpolation is basically a method of artificially increasing the number of pixels in an area inside an image. It is one of the methods which are usually present in the image processing applications like facial reconstructions, image Super-Resolution, and multiple image descriptions etc. Image interpolation is also one of the traditional methods used in the Super Resolution. Conventional systems include the bilinear and bicubic interpolations which are having good real time computational simplicity. These require very limited arithmetic operations [23-25]. Video interpolation or inter frame interpolation can also be achieved by these methods. Other, Conventional systems based on polynomials interpolation methods are also present in literature as discussed in previous section. Interpolation based approach is one of the fastest methods for image Super Resolution. However, it produces the artifacts like blurriness, aliasing effects, nonrealistic edges etc., so there is still scope of improvement in these methods. Interpolation based SR schemes are more frequently used when working with a single image only. Nearest Neighbor (NN), bilinear and bicubic are the ordinarily used interpolation techniques. In order to execute the interpolation, there are also other various techniques as described in the previous section. However, the three fundamental categories i.e. nearest neighbour, bilinear and bi-cubic interpolation are used as the base of image interpolation. All these techniques have their own basic defined procedures. Nearest neighbour interpolation is a replicating type of interpolation. It is a very basic method and has its advantage of having very less computation. Moreover, because of the lesser computation, its time consumption is also very less. Therefore, it is a good candidate for faster processing for image upscaling. It is just repeating the values of neighbours, so it is not changing any original data. Bilinear interpolation is another technique used for interpolation which is based on the average of pixels. It calculates the average in the horizontal and vertical directions. It is computationally heavier than the nearest neighbour; however, results are expected to be more favourable. Bicubic interpolation is based on a weighted average of 16 closest neighbours. It is more complex than other methods. However, in certain cases, it gives better results than other techniques. It consumes more time compared to previous methods.

## 3. PROPOSED CONTENT ADAPTIVE INTERPOLATION METHOD

In the proposed method, the image of size 'm' x 'n' has been converted to '2m' x '2n' pixel image. In order to upscale the image pixels are considered on a image pixel model of size '2m' x '2n' as shown in Figure 1. In this model, the shaded blocks in Figure 1 represent the original pixels of an image and unshaded blocks represent the vacant pixels which are required to be interpolated. In the process of filling vacant pixels, the actual pixel values of the original image have been considered. In this method, the given image pixels have been considered into three sorts; one is for filling of horizontal vacant pixels, second is for filling of vertical vacant pixels and third is for filling of diagonally middle pixels as shown in Figure 1 with letters 'H', 'V' and 'D' respectively. Depending upon the particular direction of change, pixels are updated as per the methods explained further with their respective sorts. Moreover, for all pixels, at least 4 original neighbouring pixels are considered and then the value of the vacant pixel is calculated. In these methods, quantitative variations of original pixel intensities have been considered based upon that proper value of vacant pixel would be assigned. There are various possibilities of content which can exist in the images; there could be a complex region having edges or other uniform smooth regions. Therefore, vacant pixel calculations will depend upon the content of the region. The vacant pixel calculations involved in the three sorts are explained further.

### 3.1. Horizontal pixels

In order to fill the horizontal pixels as indicated by the letter 'H' in Figure 2, the wrapping distance based method has been proposed. Clearly, depending upon the nearest pixel values this particular target pixel's value would be decided. Four neighbouring original pixels (H1-H4 in Figure 2) with original values have been used to find the required value (H) of the vacant pixel as indicated by (1-6). With reference to Figure 2, the target pixel 'H' need to be calculated. To check whether it is on a complex area or on a plane area, parameter A is calculated from A1 and A2 as per (1-3).

$$A1 = |H3 - H1| \quad (1)$$

$$A2 = |H4 - H2| \quad (2)$$

$$A = A1 - A2 \quad (3)$$

Parameter A calculated from (3) is helpful in calculations of weight vectors, W1 and W2. The values of weight vectors would be updated as per (4) and (5).

$$W1 = \frac{(1-Q*A)}{2} \quad (4)$$

Where Q is the controlling vector which would decide the weightage factor of W1 and W2, it can be varied depending upon application or type of image.

$$W2 = 1 - W1 \quad (5)$$

After calculation of W1 and W2, the target pixel H will be updated as per (6).

$$H = W1 * H2 + W2 * H3 \quad (6)$$

Basically, the impact of 'H2' and 'H3' on 'H' will depend on values of weight vectors i.e. W1 and W2. The procedure will be repeated for all horizontal pixels, in order to find all pixels of the horizontal direction from left to right row-wise.

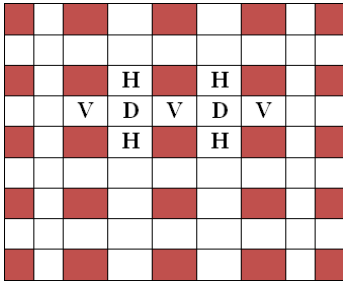


Figure 1. Pixel model of interpolation

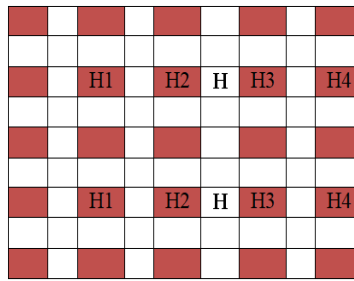


Figure 2. Horizontal pixels

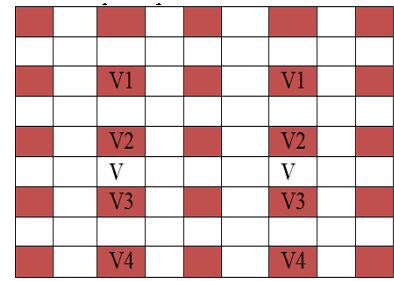


Figure 3. Vertical pixels

### 3.2. Vertical pixels

In order to update the vacant vertical pixels again method similar to the horizontal method has been used. In Figure 3, the required pixel is indicated by the letter 'V' for the vertical lines. Depending upon the values of 4 neighbouring pixels (V1-V4), calculation leads toward the new required pixel value. As explained in horizontal pixels, in a similar way vertical pixels 'V1', 'V2', 'V3' and 'V4' as shown in Figure 3 are selected and Parameter A is updated as per (7-9).

$$A1 = |V3 - V1| \quad (7)$$

$$A2 = |V4 - V2| \quad (8)$$

$$A = A1 - A2 \quad (9)$$

Here, with reference to parameter A acquired from (9), the values of W1 and W2 would be calculated.

$$W1 = \frac{(1-Q+A)}{2} \quad (10)$$

$$W2 = 1 - W1 \quad (11)$$

'V' is updated as per (12), based on the calculations of weight vectors W1 and W2.

$$V = W1 * V2 + W2 * V3 \quad (12)$$

The same procedure will be repeated for all vertical pixels, in order to find all pixels of the vertical direction.

### 3.3. Diagonal pixels

In addition to horizontal and vertical vacant pixels, the filling of vacant diagonal pixels is also required. It is indicated in Figure 4 by letter 'D'. Again, Method based on neighbouring pixels has been proposed. In this procedure firstly, the target pixel 'D' is considered along with neighbouring pixels (D1-D7) as shown in Figure 4. Firstly, with reference to target pixel 'D', the directional changes in both directional diagonals are calculated i.e. for 45 and 135 degrees, as per (13-14). The change may be more in one of the two directions. Therefore, a comparison of changes S45 and S135 is calculated with (15).

$$S45 = |(D2 + D6) - (D4 + D8)| \quad (13)$$

$$S135 = |(D1 + D5) - (D3 + D7)| \quad (14)$$

$$S = S45 - S135 \quad (15)$$

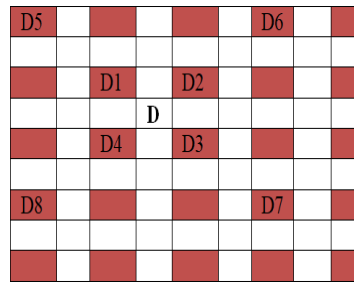


Figure 4. Diagonal pixels

The value of S can be positive or negative. If S is positive then change is more in diagonal direction along 45 degrees and the pixel is more similar along 135 degrees. If S is negative then change is more in the direction of 135 degrees and the pixel is more similar along 45 degrees. In the proposed method, there is one pre-calculated value of S called as the threshold, it is defined to detect a level of changes in neighbouring pixels. Its value will depend upon the type of image and application. If change is more in one diagonal as compared to other and along with that this change is lower than a certain defined threshold value, there is a possibility that the target vacant pixel is present in the region of small changes in its neighbourhood. Based on all these possibilities resultant value of S from (15) can be considered into 3 cases. For each case, the calculation method for 'D' has been proposed independently. So the value of 'D' would be updated based on either one of the three possible cases. All three cases have been explained as follow:

Case 1: If  $S < -$  (Threshold level)

Then D is more similar to the direction along 45-degree diagonal and therefore pixels along the 45 degree's diagonal are considered to calculate the values with the weighted method as used for horizontal and vertical directional pixel calculations. Equation (21) represents the calculated value of D based on (16-20).

$$A1 = |D2 - D8| \quad (16)$$

$$A2 = |D4 - D6| \quad (17)$$

$$A = A1 - A2 \quad (18)$$

$$W1 = \frac{(1-Q*A)}{2} \quad (19)$$

$$W2 = 1 - W1 \quad (20)$$

$$D = W1 * D2 + W2 * D4 \quad (21)$$

Case 2: If  $S > +$  (Threshold level)

Then D is more similar to the direction of 135-degree diagonal and therefore, pixels along the 135 degree's diagonal are considered to calculate the values with the weighted method as used for horizontal and vertical direction with (22-27).

$$A1 = |D3 - D5| \quad (22)$$

$$A2 = |D7 - D1| \quad (23)$$

$$A = A1 - A2 \quad (24)$$

$$W1 = \frac{(1-Q*A)}{2} \quad (25)$$

$$W2 = 1 - W1 \quad (26)$$

$$D = W1 * D1 + W2 * D3 \quad (27)$$

Case 3: Otherwise i.e.  $-(\text{Threshold level}) \leq S \leq (\text{Threshold level})$

If the value of S from (15) is lying between the negative thresholds to a positive threshold, then it is taken as the third case. If the difference S in pixels is lying in this range, then it contains the finer details for which again procedure is defined. In this case, a window of 4 x 4 pixels (D1-D16) is selected as shown in Figure 5 and in this a particular window mean is calculated. Based upon that standard deviation is calculated and thus it is detected that whether it is a soft edge or a fine area. The deviation limit L should be based on the type of image and it should provide the best results at that value.

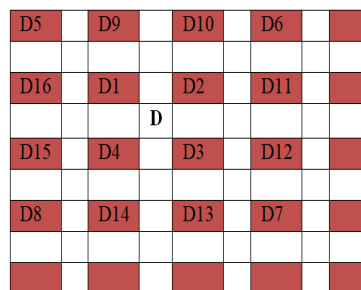


Figure 5. Pixel window of the original image

If the Standard deviation of the window (4 X 4) > (Deviation limit L), then it is a soft edge. Therefore, minimum nearest pixels will be used to calculate the unknown diagonal pixel 'D'. In order to update the target pixel 'D', different pixels as shown in Figure 5 would be considered as per (28).

$$D = \frac{D1+D2+D3+D4}{4} \quad (28)$$

Else, if the Standard deviation of the window (4 X 4) ≤ (Deviation limit L), It represents the area of some smoother finer region and weight matrix is used to calculate the unknown pixels. The weight matrix is given by (29) which is used to update pixels.

$$W = \begin{bmatrix} 0.0127 & 0.0436 & 0.0436 & 0.0127 \\ 0.0436 & 0.1500 & 0.1500 & 0.0436 \\ 0.0436 & 0.1500 & 0.1500 & 0.0436 \\ 0.0127 & 0.0436 & 0.0436 & 0.0127 \end{bmatrix} \quad (29)$$

In this case, the target vacant pixel 'D' can be calculated as per (32) which involves the element wise matrix multiplication of pixels (D1-D16) with weight matrix ( $W_{rc}$ ) i.e.  $W_{rc} \cdot D_{rc}$ . Here,  $D_{rc}$  represents the matrix of original pixels (D1-D16) as shown in Figure 5.

$$W_{rc} = \begin{bmatrix} w_{11} & \cdots & w_{1n} \\ \vdots & \ddots & \vdots \\ w_{n1} & \cdots & w_{nn} \end{bmatrix} \quad (30)$$

$$D_{rc} = \begin{bmatrix} D_{11} & \cdots & D_{1n} \\ \vdots & \ddots & \vdots \\ D_{n1} & \cdots & D_{nn} \end{bmatrix} \quad (31)$$

The value n will be 4 in case of soft smooth area:

$$D = \sum_{r=1}^n \sum_{c=1}^n W_{rc} \cdot D_{rc} \quad (32)$$

The procedure having 3 cases will be repeated for the all Diagonal 'D' vacant pixels in the complete image and the values of all unknown target pixels would be calculated. In this way all the new pixels at 'H', 'V' and 'D' are calculated in three sorts, which are used for increasing the number of pixels or super-resolving the required image. Clearly, above procedure can be repeated depending upon the level of Super Resolution i.e. depending upon magnification factor.

#### 4. RESULTS AND ANALYSIS

In order to compare the performance of method, an analysis has been performed further. In the analysis part lossy compression has been considered which includes the standard compressions. Test images are taken of size 256 x 256 pixels and have been converted to 512 x 512 pixels as a part of SR. All the test images are compressed images with two standards i.e. the "JPEG", "JPEG2000" and the level of compression or quality of test images is related with the bit rate of the test image. It has been seen that the proposed method performs better than other standard methods as shown in Figure 6.

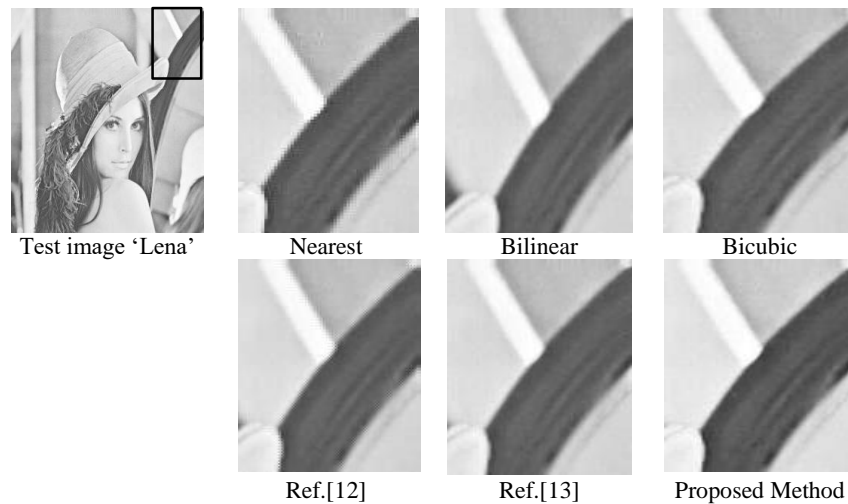


Figure 6. Comparison of Interpolation techniques for jpg compressed images for the upper right part

For the purpose of finding which particular algorithms give an improved result, it requires the organized comparative system. Clearly, same test image database is required to be tested on image interpolation methods. In order to evaluate the performance of the method well known quality metrics like Peak signal-to-noise ratio (PSNR), Mean-square error (MSE) could be used. MSSIM is mean structural similarity index, again a very useful index for qualitative comparisons [26]. Multiple images have been considered, for which PSNR, MSE and MSSIM of the proposed method have been compared with Nearest Neighbor, Bilinear, Bi-Cubic interpolation along with method given by Ref. [12] and Ref. [13] respectively.

Results have been shown in Tables 1 and 2, for JPEG and JPEG2000 based compressed images separately. Under all these performance metrics the proposed method has performed better than the standard methods.

Table 1. Comparison of interpolation techniques for JPEG compressed images

Image	Bit Rate	Parameter	Proposed Method	Nearest	Bilinear	Bicubic	Ref. [12]	Ref. [13]
Lena.jpg	0.82	PSNR	<b>35.13</b>	29.63	31.53	31.53	34.36	34.02
		MSE	<b>19.91</b>	70.73	45.69	45.73	23.80	25.74
		MSSIM	<b>0.920</b>	0.864	0.894	0.897	0.913	0.910
Child.jpg	0.90	PSNR	<b>34.64</b>	29.49	31.50	31.49	33.97	33.76
		MSE	<b>22.31</b>	73.07	45.97	46.08	26.02	27.32
		MSSIM	<b>0.935</b>	0.875	0.908	0.912	0.926	0.924
Fruits.jpg	0.85	PSNR	<b>32.24</b>	27.40	29.20	29.17	31.53	30.92
		MSE	<b>38.80</b>	118.17	78.02	78.71	45.68	52.50
		MSSIM	<b>0.901</b>	0.842	0.872	0.873	0.893	0.887
Peppers.jpg	0.95	PSNR	<b>32.81</b>	28.56	30.2	30.23	32.39	32.10
		MSE	<b>34.02</b>	90.47	60.91	61.65	37.49	40.02
		MSSIM	<b>0.844</b>	0.788	0.821	0.820	0.838	0.836
Cameraman.jpg	0.78	PSNR	<b>35.56</b>	27.97	30.31	30.44	35.08	34.11
		MSE	<b>18.05</b>	103.72	60.44	58.75	20.20	25.20
		MSSIM	<b>0.958</b>	0.902	0.930	0.936	0.949	0.948

Table 2. Comparison of interpolation techniques for JPEG2000 compressed images

Image	Bit Rate	Parameter	Proposed Method	Nearest	Bilinear	Bicubic	Ref. [12]	Ref. [13]
Lena.jp2	0.3830	PSNR	<b>34.71</b>	29.32	31.23	31.13	34.06	33.77
		MSE	<b>22.01</b>	76.00	49.04	50.10	25.51	27.30
		MSSIM	<b>0.908</b>	0.854	0.882	0.884	0.902	0.899
Child.jp2	0.3843	PSNR	<b>34.00</b>	29.19	31.16	31.06	33.46	33.33
		MSE	<b>25.91</b>	78.43	49.79	50.89	29.34	30.23
		MSSIM	<b>0.915</b>	0.859	0.890	0.892	0.907	0.906
Fruits.jp2	0.3835	PSNR	<b>31.73</b>	27.23	28.96	28.90	31.12	30.60
		MSE	<b>43.62</b>	123.16	82.71	83.74	50.28	56.65
		MSSIM	<b>0.877</b>	0.827	0.851	0.852	0.870	0.865
Peppers.jp2	0.3827	PSNR	<b>32.14</b>	28.32	29.90	29.82	31.81	31.63
		MSE	<b>39.75</b>	95.69	66.53	67.74	42.88	44.70
		MSSIM	<b>0.817</b>	0.772	0.798	0.798	0.812	0.812
Cameraman.jp2	0.3836	PSNR	<b>35.30</b>	27.79	30.18	30.21	34.89	34.00
		MSE	<b>19.20</b>	108.17	62.44	61.98	21.11	25.86
		MSSIM	<b>0.949</b>	0.892	0.921	0.925	0.941	0.940

With reference to results, it is quite clear that as the compression standard changes, the performance of up-scaling methods differs. In both the methods when the bit rate is low i.e. compression level is high, the performance of each algorithm is low. However, as the bit rate increases performance of interpolation improves further. It is due to the reason that as bits rate increases, compression ratio decreases, therefore the quality of base image also increases. As both considered standards are lossy compression standards, there is always some loss of data. If compression would be high then there will be an additional need of denoising or deblocking method along with interpolation. However, the proposed method has performed better than the other conventional methods. The proposed method is based on interpolation hence it cannot be compared with other training based methods which require a training database and often consume more time as compared to interpolation based methods. The proposed method is more practical and further performance can be enhanced by including other noise removal methods to enhance the quality of the base image.

## 5. CONCLUSION

In this paper, the presented content adaptive method of image up-scaling is based on adaptive interpolation. This method uses a single image frame and works as the post processing method of Super Resolution for the compressed images. The proposed method relies on a content adaptation of interpolation technique. In the paper, BDCT based “JPEG” and wavelet based “JPEG2000” standard compressed images have been considered in the analysis. With reference to the simulations and analysis, it can be concluded that the proposed method performs better than other conventional standard methods in terms of different quality matrices. The proposed system stands good for real life systems which require faster image Super Resolution. In the upcoming days, up-scaling of videos is also required where frame by frame interpolation could be useful and the proposed method can be modified to interpolate video signals also.

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