

## Noise reduction in ECG signals for bio-telemetry

V. Jagan Naveen<sup>1</sup>, K.Murali Krishna<sup>2</sup>, K. Raja Rajeswari<sup>3</sup>

<sup>1</sup>Department of Electronics and Communication Engineering, GMR Institute of Technology, India

<sup>2</sup>Department of ECE, ANITS, India

<sup>3</sup>Department of ECE, GVPCEW, India

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### ABSTRACT

In Biotelemetry, Biomedical signal such as ECG is extremely important in the diagnosis of patients in remote location and is recorded commonly with noise. Considered attention is required for analysis of ECG signal to find the patho-physiology and status of patient. In this paper, LMS and RLS algorithm are implemented on adaptive FIR filter for reducing power line interference (50Hz) and (AWGN) noise on ECG signals. The ECG signals are randomly chosen from MIT\_BIH data base and de-noising using algorithms. The peaks and heart rate of the ECG signal are estimated. The measurements are taken in terms of Signal Power, Noise Power and Mean Square Error.

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### Corresponding Author:

V. Jagan Naveen,

Department of Electronics and Communication Engineering,

GMR Institute of Technology,

Rajam, India.

Email: jagannaveen.n@gmrit.org

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## 1. INTRODUCTION

The Electro Cardiogram (ECG) produces electrical signals of the each cardiac cycle. In the cardiac cycle, each event has its own significance to study the behaviour of patient cardiac pathophysiology. Generally ECG signals are Bio electrical signal which gives the electrical activity of heart versus time. Therefore it is very important to diagnose for analysing heart function [1]. The Bio electrodes are placed on the skin of the patient to acquire ECG signals. The pacemakers are located in the upper part of the right atrium. It fires electrical pulses to the nerves to stimulate the contraction phase. These pulses extend over the atrial walls and activate cardiac muscles to contract.

The ECG frequency range is typically 0.05 to 100Hz and power-line signal's frequency range is 50Hz. So, ECG signals sensitive to the power line signals in the range around 50Hz which are causing interference [2]. 50Hz PLIN will interrupt the P and Q waves of the ECG signal. Most of Asian regions, Domestic and hospital power line are in the range of 50 Hz. So the frequency components associated in ECG that is 50 Hz are effected by the power line signals causing interference in ECG. But lack of power line quality the power signals are swings between the 47 to 53 Hz so the interference also effects from this range of power line signal. To mitigate this dynamic interference from power line we need use adaptive filter to suppress this random noise causing from power line [3].

An adaptive noise elimination filter has been used to evade this impending loss of information. Four different waves can be observed while recording ECG signal those are PQRST. The depolarization of right atria represents P wave. While the rapid depolarization of right and left ventricles represents QRS wave. The repolarization of the ventricles represents T wave [4], [5]. Any deviation in the said parameters leads abnormalities in the heart. The wave form related to QRS complex represent the contraction of left and right ventricles, which is more powerful than that of atria. It comprises muscle mass and causing a more ECG

deflection. The Q wave signifies the signal horizontal (i.e. left to right) current as a potential travel through the inter-ventricular system. The Q wave is not having a septal origin shows myocardial violation which involves the full depth of myocardium.

The P wave arises when the SA node (Sinus Atria) generates a potential which depolarizes the atria. However as long as the atrial depolarization takes place to spread through the AV node to the ventricles, each P wave should be trailed by QRS complex [6]. From the commencement of QRS complex is called PR interval. This indicates the time that it takes for the electrical impulses produced in the SA node and to travel through the atria and across the AV node (Atria Ventricle) node to the ventricle. In adaptive filter, least mean square algorithm requires input signal and reference signal to update the (tap weights) filter coefficients of the adaptive FIR filter. For every iteration, LMS algorithm update new tap weights based on the previous tap weights to minimize the error. After several iterations, it eliminate the noise in the adaptive filter and gives best minimum mean square error. This method follows the computation based on the past available information. The RLS (Recursive least square) algorithm gives better convergence than LMS algorithm [7]. The main disadvantage of the RLS algorithm is having high computational cost. In the paper, section II shows the LMS and RLS algorithm, section III gives the simulation results and section IV gives the conclusion results.

## 2. RESEARCH ADAPTIVE FILTERING

Adaptive filter involves the alteration of filter parameters (coefficient) over time to reduce the noise in the signal and to minimize the error [8]. Digital signal processing exhibited by most of the adaptive filters will be digital in nature because of complexity in optimizing algorithms. Adaptive filters are best suited when there is large uncertainty and filter has to compensate that or signal conditions are slowly changing. The performance of adaptive filter involves two process, which are filter processing and adaptation process [9]. The adaptive filter output  $Z(n)$  is given as (1).

$$Z(n) = P(n)S(n) \quad (1)$$

Where  $S(n)$  is the input ECG signal and  $P(n)$  are the adaptive filter coefficients.

As we known ECG signal interference by 50 Hz power line signal .so, we have to suppress the 50 Hz component in the ECG signal which are originated by the power line. If we remove complete 50 Hz component in the ECG signal there may be data loss in the ECG signal which are associated with 50Hz frequencies region. So we need to estimate the disturbance by power line signal for that we giving power line signal as reference to the adaptive filter. Now the adaptive filter will track the power line components in ECG signal and we can easily extract interference part in the ECG signal. The difference between the desired signal  $d(n)$  and the signal from the output of the filter  $Z(n)$  is the error signal  $e(n)$ .

$$e(n) = d(n) - Z(n) \quad (2)$$

The filter variable updates filter coefficients at every time instantaneous.

$$P(n + 1) = P(n) + \Delta P(n) \quad (3)$$

Where  $P(n+1)$  is the updated weight vector with the previous weight vector and  $\Delta$  is the correction factor depends on the value.

### 2.1. Least mean square algorithm

These algorithms was suggested by Widrow and Hoff. They developed LMS from their studies of pattern recognition [10]. In the LMS algorithms, the correction applied to the above mentioned estimate includes product of three factors: the error signal  $e(n-1)$ , the (scalar) step-size parameter ( $\mu$ ) and the tap-input vector  $s(n-1)$ . LMS algorithm is the best selection if we are dealing with adaptive digital circuits in this case a filter that reject the bands of signal those causes interference to the ECG [11]. The basic operation of LMS algorithm is the recursive updating nature of filter coefficients by the reference of error signal. Each iteration of LMS involves three steps:

Filter output:

$$Z[n] = \sum_{n=0}^{N-1} S[n]P[n] \quad (4)$$

Estimation error:

$$e(n) = d(n) - Z(n) \quad (5)$$

Tap-weight adaptation:

$$P[n + 1] = P[n] + \mu S[n]e[n] \quad (6)$$

$d(n)$  is taken as desired signal and  $Z(n)$  is the output response of the adaptive filter equation 4 shows the output response of the Filter with input signal  $S(n)$  and filter coefficients  $P(n)$ .

## 2.2. Recursive least square algorithm

With supreme computational complexity, RLS is the fastest converging algorithm. It cancels maximum amount of noise by minimizing error with the fastest rate. So in this study, a tradeoff between computational complexity and convergence rate is done to attain the utmost noise free signal. The filter output and error function of RLS algorithm are shown in (8) and (9).

$$R(n) = \frac{\lambda^{-1}L(n-1)u(n-1)}{1+\lambda^{-1}u^HL(n-1)u(n)} \quad (7)$$

Where  $R(n)$  is the vector gain,  $L(n)$  is the inverse correlation matrix,  $u(n)$  is the buffered input vector and  $\lambda^{-1}$  denotes the reciprocal of the exponential weighting factor. The filter output is

$$Z(n) = P^T(n-1)u(n) \quad (8)$$

Error signal:

$$e(n) = d(n) - Z(n) \quad (9)$$

The updated coefficients as shown in (10-12)

$$P(n) = P(n-1) + R^H(n)e(n) \quad (10)$$

$$P(n) = P(n-1) + R^H(n)[d(n) - Z(n)] \quad (11)$$

$$P(n) = P(n-1) + R^H(n)[d(n) - P^T(n-1)S(n)] \quad (12)$$

where  $R^H(n)$  is the gain constant, with a sequence of training data up to time, the RLS algorithm estimates the weight by minimizing the resulting cost [12]. Where  $u(n)$  is the input, and  $\lambda$  is the stabilization parameter.

## 3. RESULTS AND ANALYSIS

ECG signals are randomly taken from MIT\_BIH data base as shown in Figure 1 i.e. (101,104,106,109,124) [13-15]. The length of each ECG signal is restricted to 3600 samples. In LMS algorithm the  $\mu$  is taken as 0.02 [8] and in RLS algorithm  $\lambda$  is taken as one randomly. Matlab is taken as a tool for simulations and noise is considered as Adaptive White Gaussian Noise (AWGN) with power line interference of 50Hz on ECG signal with less noise power. After de-noising using LMS and RLS algorithm, ECG signals peaks are estimated and results are compared with original signals without noise.

Implementation of LMS Algorithm by reducing channel Noise and reducing Power line interference of 50 Hz in ECG Signal. The Figure 1 shows the ECG signal 101 from the database, Figure 2 is noisy signal i.e AWGN. Figure 3. is corrupted ECE signal from noise. Figure 4. indicates the processed ECG signal after suppression of AWGN using LMS algorithm with  $\mu$  is taken as 0.02. Figure 5 specifies Power Line Interference suppression using LMS Algorithm with  $\mu$  is taken as 0.02. Figure 6 indicates the processed ECG signal after suppression of AWGN using RLS algorithm with  $\lambda$  is taken as one. Figure 7 shows Power Line Interference suppression using RLS Algorithm. Different patient signals 101, 104, 106, 109, 124. Wav files are taken from MIT BIH database. The signal power and noise power of ECG signals are measured before applying to the adaptive algorithms.

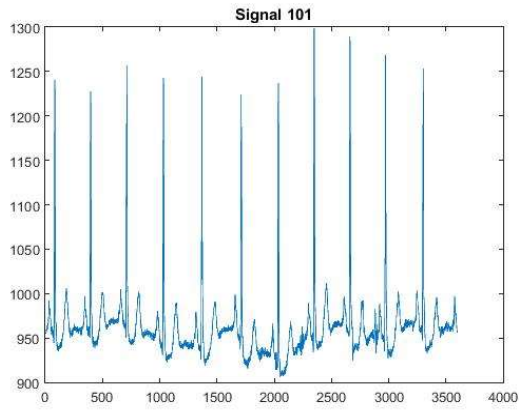


Figure 1. ECG waveform from MIT-BIH database

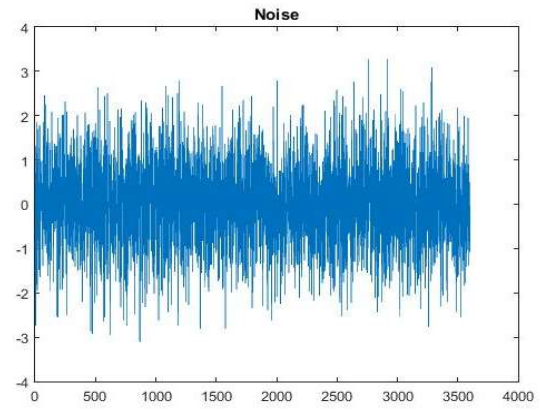


Figure 2. Noise signal

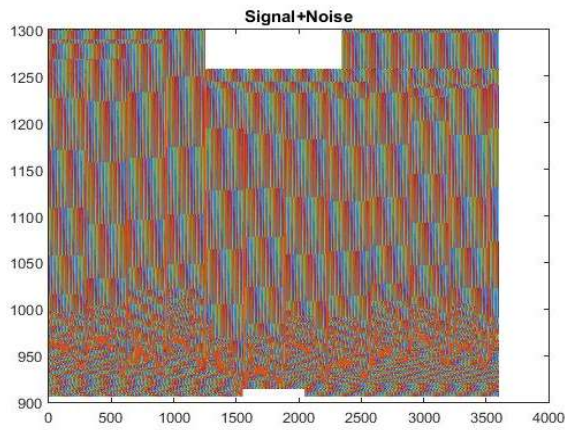


Figure 3. ECG signal+noise

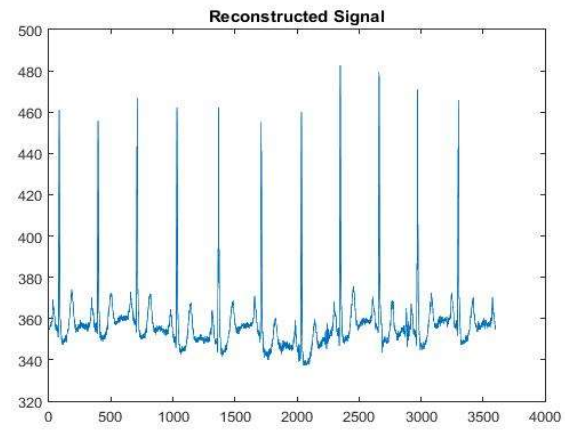


Figure 4. Noise removal in ECG signal using LMS algorithm

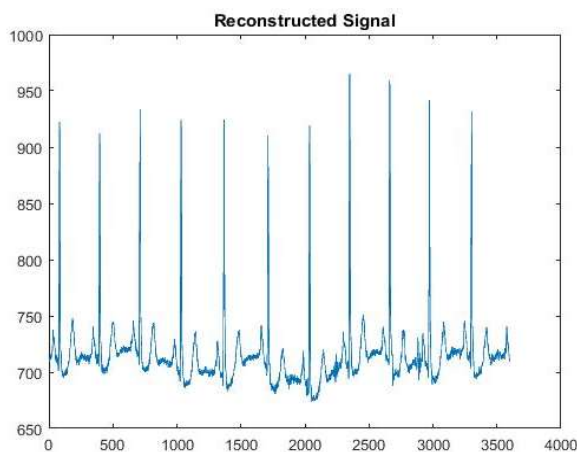


Figure 5. (50Hz) Power line interference suppression using LMS algorithm

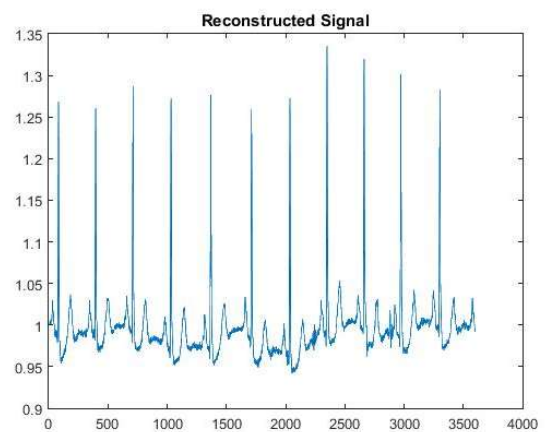


Figure 6. Noise removal in ECG signal using RLS algorithm

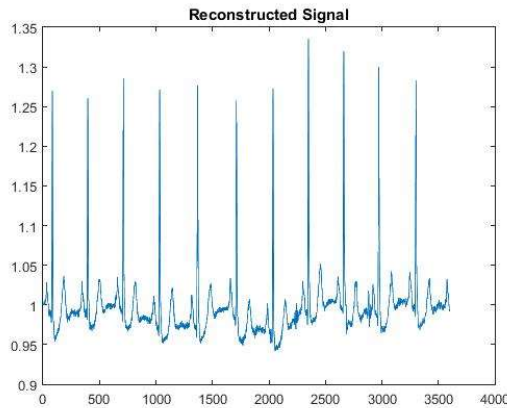


Figure 7. (50Hz) Power line interference suppression using RLS Algorithm

The convergence rate is not same for LMS and RLS algorithm [8]. These signals are processed through Several iterations by LMS and RLS algorithms in the adaptive filters to minimize the error. Table 1 and Table 3 estimates the power of the error signals and mean square deviation. The same signals are taken with 50Hz power line interference by considering uniform noise on each signal. It is observed that more the signal power, minimizes the error as shown in Table 2 and Table 4. Table 5 shows that ECG signals under noiseless conditions, QRST peaks are estimated. Table 6 and Table 7 shows that ECG signals corrupted with noise and powerline interference, QRST are measured after processed through adaptive filter using LMS algorithm. It is observed that QRST peaks are influenced with noise, but the heart beat rate information is appropriate. The same case is taken using RLS algorithm to measure QRST peaks with more influenced with noise. It is observed that heart beat rate information is appropriate and removals on QRST peaks are minimized. By observing Table 5 to Table 9 power line interference (50Hz) in the system and noise in the channel are suppressed to maximum extend using LMS and RLS algorithm. The peaks of QRST in ECG waves and heart rates are measured for different signals from MIT\_BIH data base.

Table 1. Channel Noise Reduction on ECG Signal using LMS Algorithm by Considering Interference of the Same Signal by ith Different Phase in the Channel with  $\mu=0.02$  Taken Randomly

Signals from MIT BIH data base	ECG Signal Power (dB)	Noise Signal Power (dB)	Power of the Error Signal (dB)	Mean Square deviation (dB)
101	-0.3339	0.0843	-8.9620	-21.2726
104	-0.1954	0.1034	-8.7943	-21.0287
106	-0.0922	0.0702	-8.6967	-21.0243
109	-0.4866	0.0771	-9.1009	-21.0891
124	-1.2148	-0.032	-9.8297	-22.5220

Table 2. Power Line Interference of 50Hz on ECG Signal by Reducing Interference using LMS Algorithm by Considering Interference of the Same Signal by the Different Phase in the Channel

Types of Signal from MIT BIH data base	ECG Signal Power (dB)	Noise Signal Power (dB)	Power of the Signal and Noise (dB)	Power of the Error Signal (dB)
101	-0.3339	-3.010	5.6820	-2.9158
104	-0.1954	-3.010	5.8206	-2.7737
106	-0.0922	-3.010	5.9218	-2.6680
109	-0.4866	-3.010	5.5267	-3.0627
124	-1.2148	-3.010	4.8001	-3.7882

Table 3. Channel Noise Reduction on ECG Signal using RLS Algorithm by Considering Interference of the Same Signal by ith Different Phase in the Channel with  $\lambda=1$  Taken Randomly

Signals from MIT-BIH Arrhythmia data base	ECG signal Power (dB)	Noise signal Power (dB)	Power of the errorSignal(dB)
101	-0.3339	-0.0467	-0.0274
104	-0.1954	-0.0472	-0.0581
106	-0.0922	-0.1854	-0.0630
109	0.4866	-0.2264	0.0268
124	-1.2148	-0.0494	0.0065

Table 4. Power Line Interference of 50Hz on ECG Signal by Reducing Interference using RLS Algorithm by Considering Interference of the Same Signal by the Different Phase in the Channel

Signal from MIT-BIH data base	Power of the original ECG signal (dB)	Noise signal Power (dB)	Power of the Signal and Noise (dB)	Power of the Error Signal (dB)
101	-0.3339	-3.0103	5.6879	-0.0274
104	-0.1954	-3.0103	5.8274	-0.0581
106	-0.0922	-3.0103	5.9320	-0.0630
109	-0.4866	-3.0103	5.5360	0.0268
124	-1.2148	-3.0103	4.8114	0.0065

Table 5. Each ECG Signal's Length is Having 3600 Samples Under Noise Less Conditions, QRST Peaks are Estimated in ECG Signals as Shown in the Table (mV)

Signal from MIT-BIH data base	R Peak (mV)	S Peak (mV)	T Peak (mV)	Q Peak (mV)	Heart Rate beats/min
101	203.23	-25.535	35.965	-6.672	45.83
104	266.12	3.458	259.47	141.616	58.33
106	355.24	-26.902	145.803	115.92	54.16
109	256.372	23.832	208.24	163.611	66.66
124	390.59	-41.245	20.3103	102.8	33.33

Table 6. LMS Algorithm is Taken on Noisy ECG Signals which are Corrupted with Additive White Gaussian Noise. QRST Peaks are Measured (mV)

Signals from MIT-BIH data base	R Peak (mV)	S Peak (mV)	T Peak (mV)	Q Peak (mV)	Heart Rate beats/min
101	75.65	-9.469	13.200	-2.706	45.83
104	98.99	1.317	96.503	52.671	58.33
106	132.36	-9.690	54.309	42.87	54.16
109	94.71	8.86	77.436	60.49	66.66
124	145.15	-15.42	7.398	38.233	33.33

Table 7. LMS Algorithm is Introduced on Signal of ECG to Minimize the 50Hz Power Line Interference on ECG System for Considering  $\mu=0.02$ . The Readings are Taken in Terms of Milli Volts as Shown in the Table

Signal from MIT-BIH Arrhythmia data base	R Peak (mV)	S Peak (mV)	T Peak (mV)	Q Peak (mV)	Heart Rate beats/min
101	75.745	-9.571	13.242	-2.392	45.83
104	98.855	1.691	96.343	52.503	58.33
106	132.288	-9.827	54.395	42.822	54.16
109	96.264	8.813	77.511	61.396	66.66
124	144.994	-15.207	7.584	38.137	33.33

Table 8. RLS Algorithm is Taken on Noisy ECG Signals to Reduce AWGN Noise on the Noisy ECG Signals Readings are Taken for Different Signals in MIT Data Base and Measurements are in Milli Volts

Signal from MIT-BIH Arrhythmia data base	R Peak (mV)	S Peak (mV)	T Peak (mV)	Q Peak (mV)	Heart Rate beats/min
101	0.208	-0.027	0.036	-0.003	45.83
104	0.266	0.003	0.270	0.140	58.33
106	0.341	-0.029	0.144	0.112	54.16
109	0.261	0.027	0.214	0.161	66.66
124	0.446	-0.047	0.024	0.115	33.33

Table 9. RLS Algorithm is Considered to Remove Power Line Interference on the ECG Signals Which are Interfered with 50Hz Power Line Frequency in the System Volts

Signal from MIT-BIH Arrhythmia data base	R Peak (mV)	S Peak (mV)	T Peak (mV)	Q Peak (mV)	Heart Rate beats/min
101	0.2089	-0.0275	0.0371	-0.0035	45.83
104	0.2660	0.0032	0.2702	0.1406	58.33
106	0.3412	-0.0299	0.1447	0.1056	54.16
109	0.2623	0.0272	0.2142	0.1611	66.66
124	0.4459	-0.0472	0.0246	0.1154	33.33

#### 4. CONCLUSION

In this paper, the ECG signals are taken from physio-net for analysis. For Bio-telemetry applications, signals are transmitted from remote locations, LMS and RLS adaptive algorithms are considered for suppression of AWGN noise and power line interference on ECG signals. The analysis is carried out to evaluate the ECG signal power, noise signal and Mean square error. It is observed that Mean square error is less in RLS than LMS. The rate of convergence is more fast than LMS algorithm. Noise cancellation capacity is good in RLS than LMS. But the implementation is complex over LMS. After denoising at the receiver end, QRST peaks and heart beats are estimated and compared with the original QRST peaks and heart beats.

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