

Switching FOC Method for Vector Control of Single-Phase Induction Motor Drives

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ABSTRACT

This paper proposes a novel vector control method based on Rotor flux Field-Oriented Control (RFOC) for single-phase Induction Motor (IM) drives. It is shown that in a rotating reference frame, the single-phase IM equations can be separated into forward and backward equations with balanced structures. In order to accommodate for these forward and backward equations, a drive system consisting of two RFOCs that are switched interchangeably, is proposed. Alternatively, these two RFOC algorithms can be simplified as a single FOC algorithm. The analysis, controller design and simulation of the proposed technique showed that it is feasible for single-phase IM drive for high performance applications.

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1. INTRODUCTION

Single-phase Induction Motor (IM) is one of the most applicable electrical machines which are used in low power domestic and industrial applications. This electrical motor can be used in vacuum cleaners, washers, compressors, fans and etc. Generally, a single-phase IM has two main and auxiliary windings and its operation needs one or two capacitors. To guarantee the efficient use of energy, the investigation of different single-phase IM drive schemes have been increased by researchers. In these drives the single-phase IM, without capacitor, is treated as an asymmetric 2-phase IM [1].

Different converter topologies have been proposed to supply single-phase machine, for example, one-leg inverter [2], 2-leg inverter [1], [3] 3-leg inverter [4], [5] and 4-leg inverter [6]. This paper investigates the use of 2-leg inverter as shown in Figure 1 for feeding the single-phase IM. This configuration is indicated for high performance applications [1], [3] (It should be pointed out that the focus given here is on the detailed analysis and design of the vector control strategy for single-phase IM drives). Field-Oriented Control (FOC) method is widely used for implementing high performance vector control of single-phase IM drives. This method has been increasingly adopted as the standard control technique for industrial demands [1], [3], [7]-[16].

One of the main drawbacks in the presented FOC methods to control single-phase IM drives is using the supposition of $(M_d/M_q)^2 = L_{ds}/L_{qs}$ (L_{ds} , L_{qs} , M_d , M_q indicate the stator and rotor d-q axes self and mutual

inductances) [1], [3], [7]-[15]. It can be noted that for simplifying vector control equations in single-phase IM the supposition of $(M_d/M_q)^2=L_{ds}/L_{qs}$ is used. It was shown in [16] using this assumption is reflected in the torque response of the single-phase IM drive system. In [16], a method for Indirect Rotor flux FOC (IRFOC) of single-phase IM without using $(M_d/M_q)^2=L_{ds}/L_{qs}$ has been presented. However, the introduced method in [16] is extremely depends on motor parameters variations.

This study shows the single-phase IM can be modeled as two balanced circuits (forward and backward circuits). Based on this simplifying, a novel vector control method for single-phase IM based on FOC algorithm and without using $(M_d/M_q)^2=L_{ds}/L_{qs}$ is presented (switching FOC). This paper is organized as follows: After introduction in section 1, in section 2, d-q model of single-phase IM is presented. Next, section 3 describes the development of the FOC algorithm, followed by presenting proposed switching FOC scheme for vector control of single-phase IM drives. The performance of the presented method is analyzed and checked using Matlab/Simulink software in section 4 and section 5 concludes the paper.

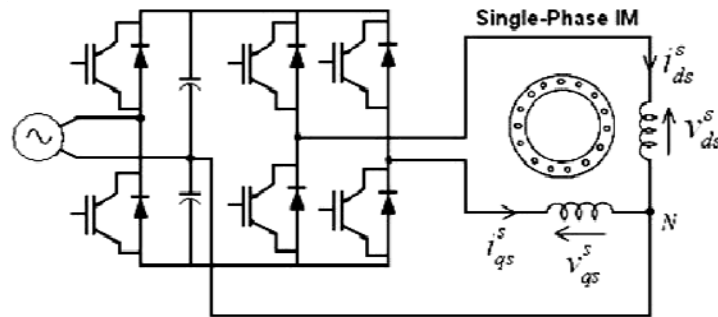


Figure 1. Single-phase IM drive system (2-leg inverter)

2. MODELING OF SINGLE-PHASE IM

Neglecting the core saturation, the d-q model of the single-phase IM in the stationary reference frame (superscript “s”) can be shown as the following equations [15]:

$$\begin{aligned}
 v_{ds}^s &= r_{ds} i_{ds}^s + \frac{d\lambda_{ds}^s}{dt} & , & & v_{qs}^s &= r_{qs} i_{qs}^s + \frac{d\lambda_{qs}^s}{dt} \\
 0 &= r_r i_{dr}^s + \frac{d\lambda_{dr}^s}{dt} + \omega_r \lambda_{qr}^s & , & & 0 &= r_r i_{qr}^s + \frac{d\lambda_{qr}^s}{dt} - \omega_r \lambda_{dr}^s \\
 \lambda_{ds}^s &= L_{ds} i_{ds}^s + M_d i_{dr}^s & , & & \lambda_{qs}^s &= L_{qs} i_{qs}^s + M_q i_{qr}^s \\
 \lambda_{dr}^s &= M_d i_{ds}^s + L_r i_{dr}^s & , & & \lambda_{qr}^s &= M_q i_{qs}^s + L_r i_{qr}^s \\
 \tau_e &= \frac{Pole}{2} (M_q i_{qs}^s i_{dr}^s - M_d i_{ds}^s i_{qr}^s) \\
 \frac{Pole}{2} (\tau_e - \tau_l) &= J \frac{d\omega_r}{dt} + F \omega_r
 \end{aligned} \tag{1}$$

In (1), v_{ds}^s, v_{qs}^s are the stator d-q axes voltages, i_{ds}^s, i_{qs}^s are the stator d-q axes currents, i_{dr}^s, i_{qr}^s are the rotor d-q axes currents, $\lambda_{ds}^s, \lambda_{qs}^s$ are the stator d-q axes fluxes and $\lambda_{dr}^s, \lambda_{qr}^s$ are the rotor d-q axes fluxes. r_{ds}, r_{qs}, r_r indicate the stator and rotor d-q axes resistances. $L_{ds}, L_{qs}, L_r, M_d, M_q$ denote the stator and rotor d-q axes self and mutual inductances. ω_r is the motor speed. τ_e, τ_l are electromagnetic torque and load torque. J, F are the moment of inertia and viscous friction coefficient respectively.

3. SWITCHING FOC METHOD FOR VECTOR CONTROL OF SINGLE-PHASE IM

In this section, a novel method for vector control of single-phase IM drives based on IRFOC is proposed. In the RFOC strategy it is necessary that the machine equations transfer to the rotating reference

frame. For this purpose, the transformation matrix as shown in equation (2) is applied to the machine equations [17]:

$$[T_s^e] = \begin{bmatrix} \cos \theta_e & \sin \theta_e \\ -\sin \theta_e & \cos \theta_e \end{bmatrix} \quad (2)$$

In (2), superscript “e” indicates that the equations are in the rotating reference frame. Moreover, “ θ_e ” is the angle between the stationary and rotating reference frames. By applying (2) to the equations of the single-phase IM (equations (1)), equations (3a) and (3b) are obtained:

$$\begin{bmatrix} v_{ds}^e \\ v_{qs}^e \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} \frac{(r_{ds} + r_{qs}) + (L_{ds} + L_{qs})}{2} \frac{d}{dt} & -\omega_e \frac{(L_{ds} + L_{qs})}{2} & \frac{(M_d + M_q)}{2} \frac{d}{dt} & -\omega_e \frac{(M_d + M_q)}{2} \\ \omega_e \frac{(L_{ds} + L_{qs})}{2} & \frac{(r_{ds} + r_{qs}) + (L_{ds} + L_{qs})}{2} \frac{d}{dt} & \omega_e \frac{(M_d + M_q)}{2} & \frac{(M_d + M_q)}{2} \frac{d}{dt} \\ \frac{(M_d + M_q)}{2} \frac{d}{dt} & -(\omega_e - \omega_r) \frac{(M_d + M_q)}{2} & r_r + L_r \frac{d}{dt} & -(\omega_e - \omega_r) L_r \\ (\omega_e - \omega_r) \frac{(M_d + M_q)}{2} & \frac{(M_d + M_q)}{2} \frac{d}{dt} & (\omega_e - \omega_r) L_r & r_r + L_r \frac{d}{dt} \end{bmatrix} \begin{bmatrix} i_{ds}^{+e} \\ i_{qs}^{+e} \\ i_{dr}^{+e} \\ i_{qr}^{+e} \end{bmatrix} \\ + \begin{bmatrix} \frac{(r_{ds} - r_{qs}) + (L_{ds} - L_{qs})}{2} \frac{d}{dt} & \omega_e \frac{(L_{ds} - L_{qs})}{2} & \frac{(M_d - M_q)}{2} \frac{d}{dt} & \omega_e \frac{(M_d - M_q)}{2} \\ \omega_e \frac{(L_{ds} - L_{qs})}{2} & -\frac{(r_{ds} - r_{qs}) + (L_{ds} - L_{qs})}{2} \frac{d}{dt} & \omega_e \frac{(M_d - M_q)}{2} & -\frac{(M_d - M_q)}{2} \frac{d}{dt} \\ \frac{(M_d - M_q)}{2} \frac{d}{dt} & (\omega_e - \omega_r) \frac{(M_d - M_q)}{2} & 0 & 0 \\ (\omega_e - \omega_r) \frac{(M_d - M_q)}{2} & -\frac{(M_d - M_q)}{2} \frac{d}{dt} & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{ds}^{-e} \\ i_{qs}^{-e} \\ i_{dr}^{-e} \\ i_{qr}^{-e} \end{bmatrix} \quad (3a)$$

$$\begin{bmatrix} i_{ds}^{+e} \\ i_{qs}^{+e} \\ i_{dr}^{+e} \\ i_{qr}^{+e} \\ i_{ds}^{-e} \\ i_{qs}^{-e} \\ i_{dr}^{-e} \\ i_{qr}^{-e} \end{bmatrix} = \begin{bmatrix} \cos \theta_e & \sin \theta_e & 0 & 0 \\ -\sin \theta_e & \cos \theta_e & 0 & 0 \\ \cos \theta_e & -\sin \theta_e & 0 & 0 \\ \sin \theta_e & \cos \theta_e & 0 & 0 \\ 0 & 0 & \cos \theta_e & \sin \theta_e \\ 0 & 0 & -\sin \theta_e & \cos \theta_e \\ 0 & 0 & \cos \theta_e & -\sin \theta_e \\ 0 & 0 & \sin \theta_e & \cos \theta_e \end{bmatrix} \begin{bmatrix} i_{ds}^s \\ i_{qs}^s \\ i_{dr}^s \\ i_{qr}^s \end{bmatrix} \quad (3b)$$

In (3a), “ ω_e ” is the angular velocity of the rotor field oriented reference frame. As can be seen, in general, equation (3a) includes two terms (forward term: superscript “+e” and backward term: superscript “-e”). Each term represents a balanced equation where rotates in the forward or backward direction as shown in Figure 2.

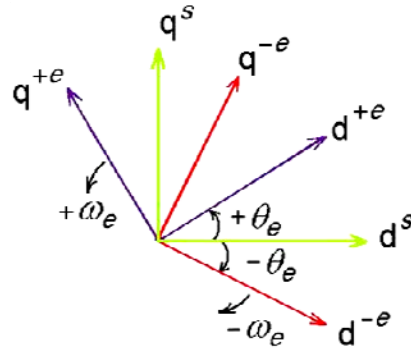


Figure 2. Forward, backward and stationary reference frames (“+e”: forward, “-e”: backward and “s”: stationary)

As can be seen from (3a), the structure of the forward and backward terms is similar to the conventional 3-phase IM equations. The only difference between forward terms and conventional 3-phase IM equations is that, in the forward terms there are: $(r_{ds}+r_{qs})/2$, $(L_{ds}+L_{qs})/2$ and $(M_d+M_q)/2$ but in the conventional 3-phase IM we have: r_s , $L_s=L_s+1.5L_{ms}$ and $M=1.5L_{ms}$. Moreover, the difference between backward terms and conventional 3-phase IM equations is that, in the backward terms there are: $(r_{ds}-r_{qs})/2$, $(L_{ds}-L_{qs})/2$, $(M_d-M_q)/2$, $r_r=0$, $L_r=0$ and there are $-i_{qs}^e$ and $-i_{qr}^e$ but in the conventional 3-phase IM we have: $L_s=L_s+1.5L_{ms}$, $M=1.5L_{ms}$, $r_r \neq 0$, $L_r \neq 0$ and there are i_{qs}^e and i_{qr}^e . The block diagram of forward and backward IRFOC can be shown as Figure 3 and Figure 4 respectively.

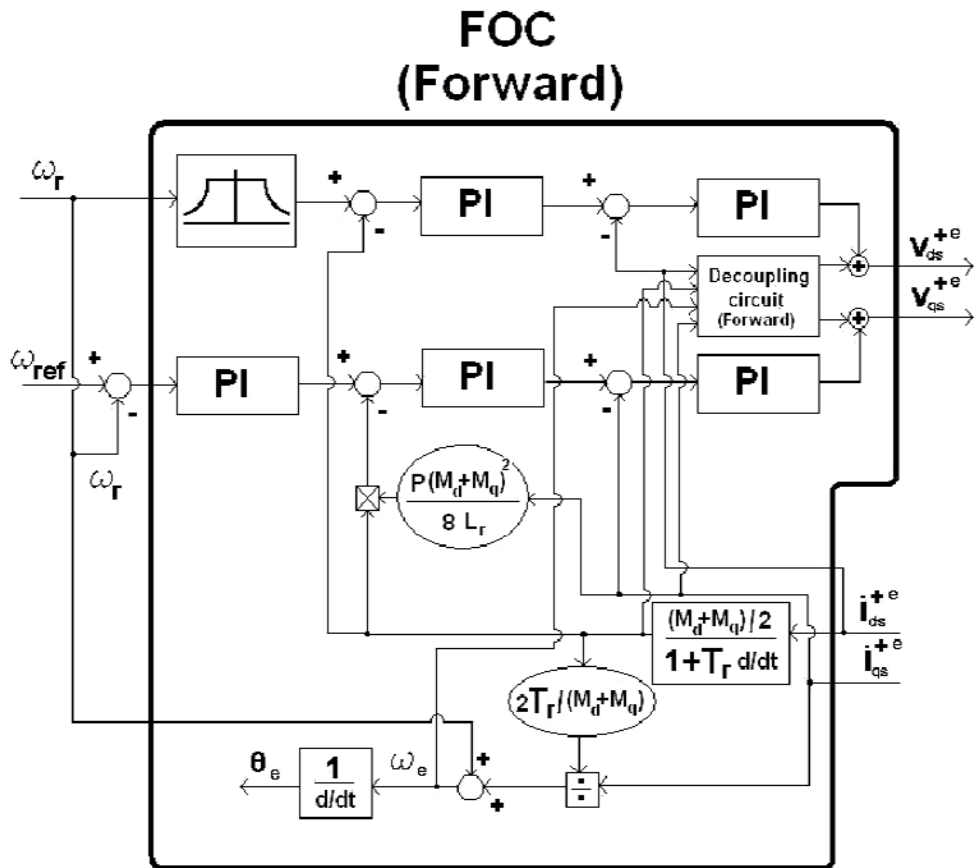


Figure 3. Block diagram of forward IRFOC

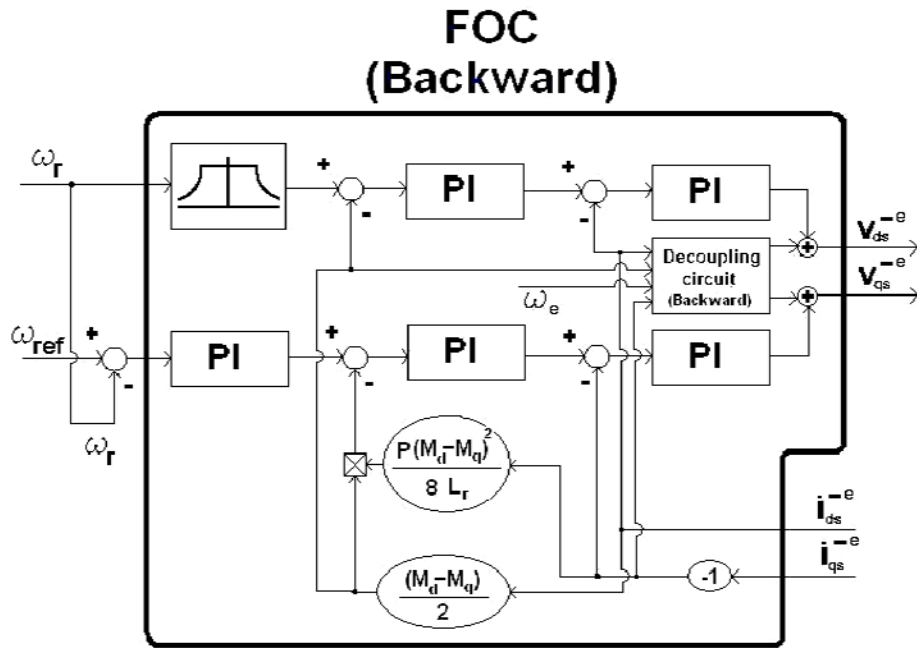


Figure 4. Block diagram of backward IRFOC

Therefore, two developed IRFOC algorithms with two forward and backward currents can be used for vector control of a single-phase IM. The block diagram of the proposed IRFOC for single-phase IM drives is shown in Figure 5. In Figure 5, in order to alternately switched between the forward and backward states, a switch is used whereby this switch will consecutively change positions in each sampling time.

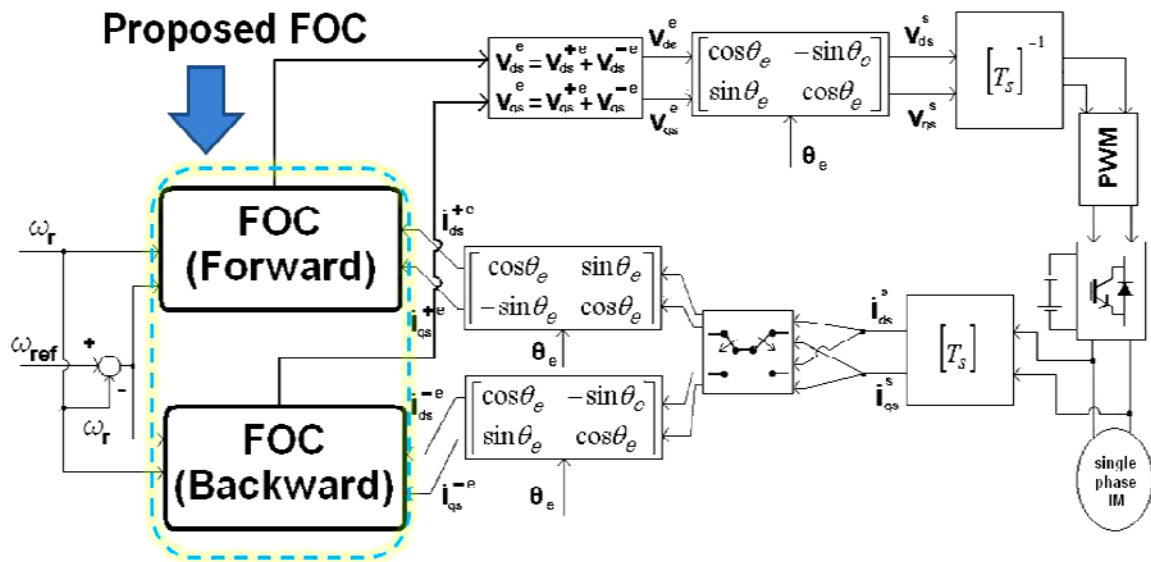


Figure 5. Block diagram of the proposed IRFOC for vector control of single-phase IM drives

In Figure 5, 2 to 2 transformation matrix ($[T_s]$) is obtained as (4):

$$[T_s] = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \tag{4}$$

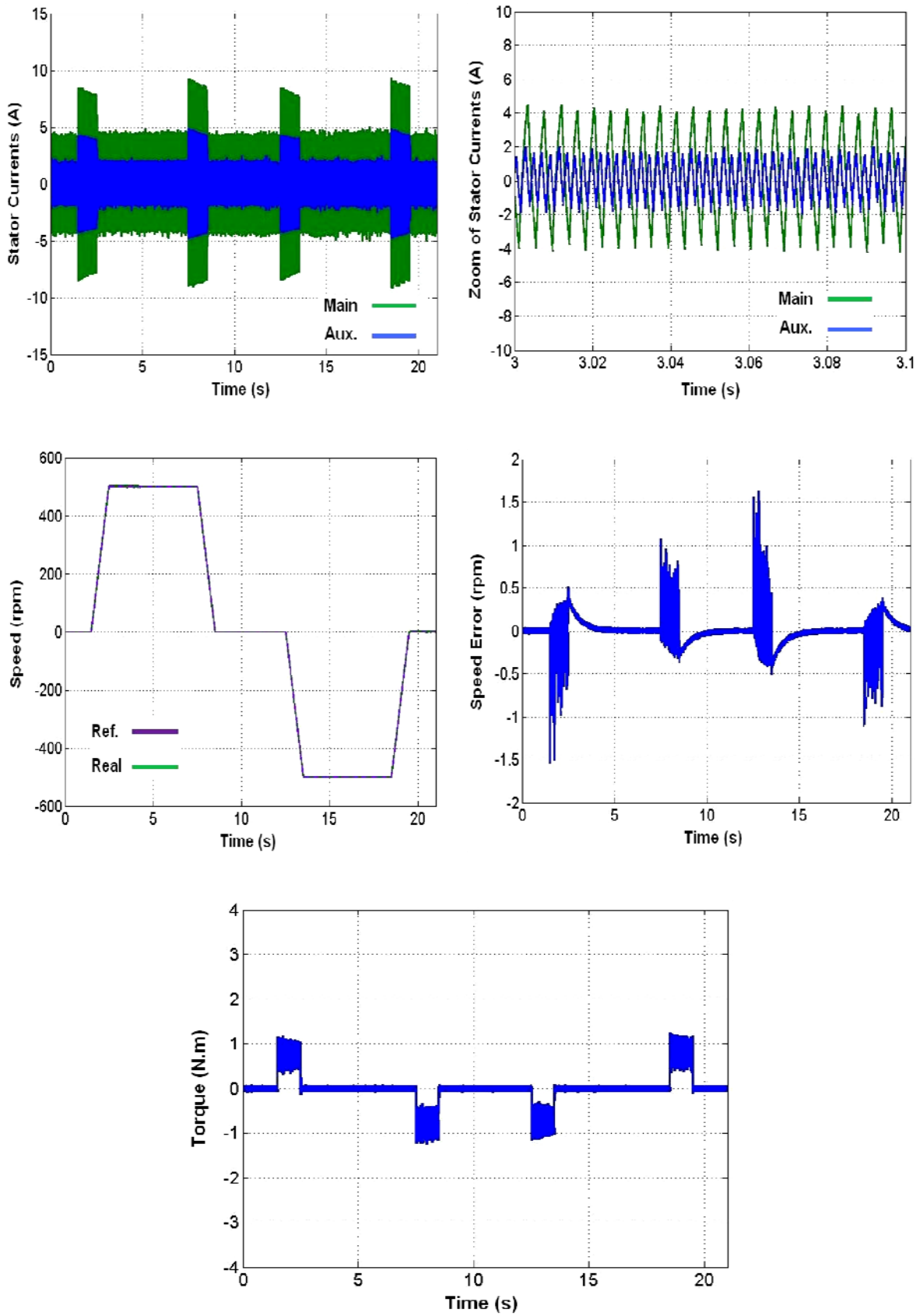


Figure 7. Simulation results of the proposed controller for the trapezoidal reference speed from top to bottom: Stator Currents, Zoom of Stator Currents, Speed, Speed Error, Torque

Figure 8 shows simulation results of the proposed strategy for vector control of the single-phase IM in the nominal and zero reference speeds and under load condition. In Figure 8, the motor is running at the reference speed of 0rpm. Then at $t=3s$ a step change of 1800rpm is introduced. In addition, at $t=9s$, a step load of 1.2N.m is introduced and at $t=11s$ is removed. It is evident from Figure 8 that although at the moment of applying load there is a small speed dip but then it is restored quickly. Based on presented results in Figure 8, using proposed drive system, the maximum speed error in nominal speed and during load condition is about 0.4 rpm. Moreover, the maximum speed error in zero reference speed is about 0.1 rpm. As shown from Figure 8 the torque increases accordingly to ensure that the speed is maintained at 1800rpm. It can be seen from Figure 7 and Figure 8 that the dynamic performance of the proposed controller for the single-phase IM is extremely acceptable.

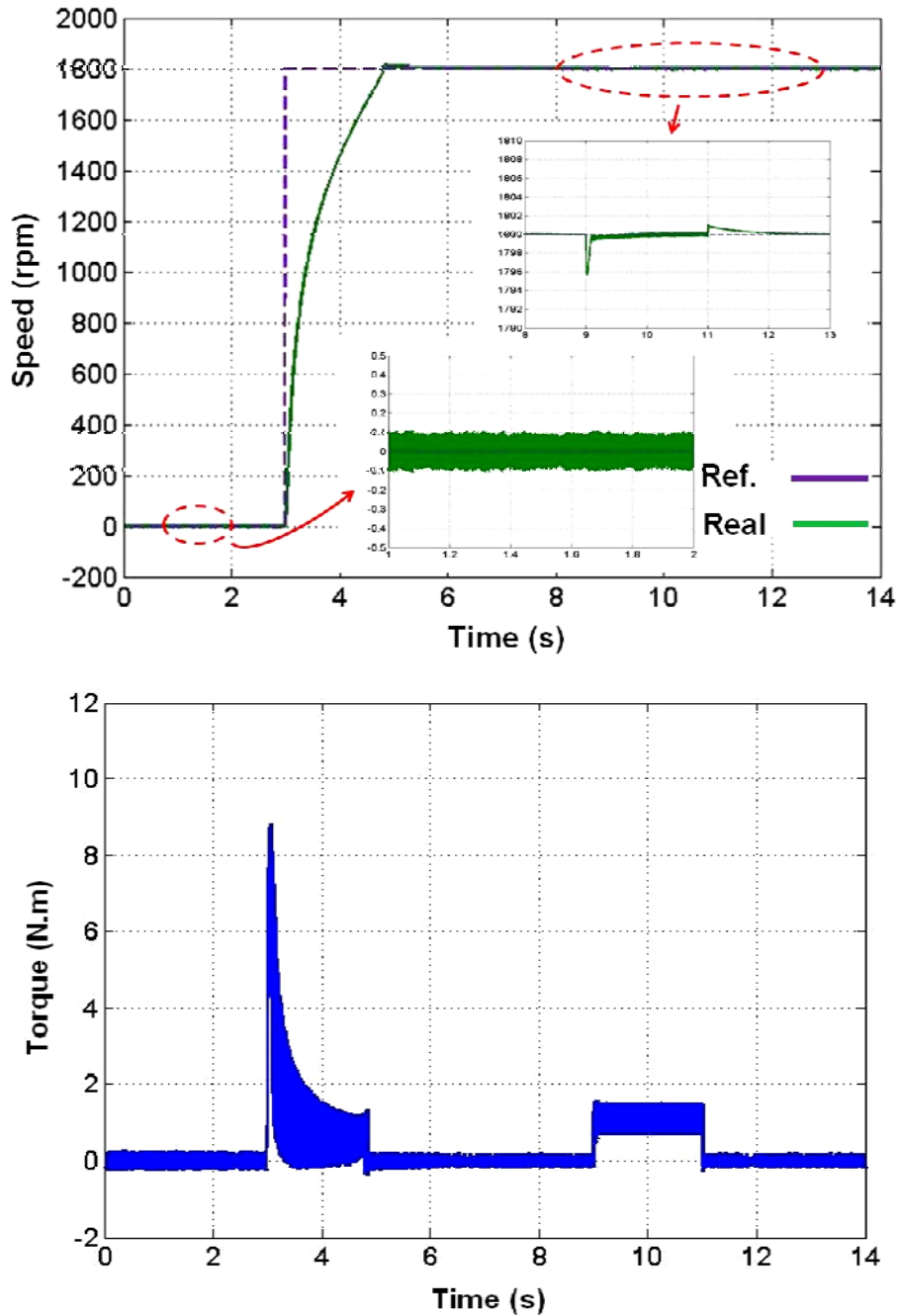


Figure 8. Simulation results of the proposed controller in the nominal and zero reference speeds and under load condition from top to bottom: Speed, Torque

Figure 9 shows the comparison between the steady-state torque response of the RFOC at the nominal reference speed by considering $(M_d/M_q)^2=L_{ds}/L_{qs}$ (e.g., [1], [3], [7]-[15]) and without considering $(M_d/M_q)^2=L_{ds}/L_{qs}$ (switching FOC). Larger torque ripple can be seen when the assumption $(M_d/M_q)^2=L_{ds}/L_{qs}$ is used. It is concluded in comparison with the previous schemes for RFOC of single-phase IM drives, the proposed controller in this study gives better performance.

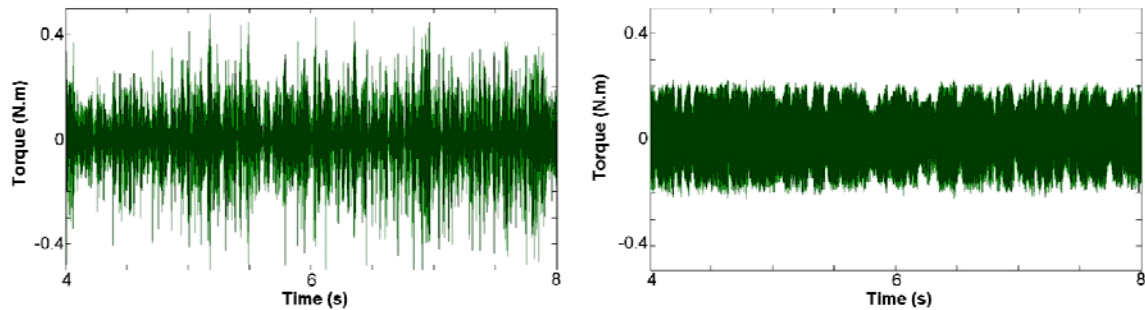


Figure 9. Simulation results of the comparison between torque response at the nominal reference speed; left: assuming $(M_d/M_q)^2=L_{ds}/L_{qs}$, right: not assuming $(M_d/M_q)^2=L_{ds}/L_{qs}$.

5. CONCLUSION

In this paper, a vector control strategy for single-phase IM drives based on Indirect Rotor flux Field-Oriented Control is proposed and tested. It was shown that the single-phase IM equations in the rotating reference frame can be classified as the balanced equations. Based on this simplicity, a novel vector control method using two developed IRFOC algorithms was proposed. As a result, these two algorithms were simplified as single IRFOC algorithm. Simulation results showed that the proposed switching FOC strategy works well over most speed ranges and under load condition.

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