

Robustness Study of Fractional Order PID Controller Optimized by Particle Swarm Optimization in AVR System

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ABSTRACT

In this paper a novel design method for determining fractional order PID ($PI^{\lambda}D^{\mu}$) controller parameters of an AVR system using particle swarm optimization algorithm is presented. This paper presents how to employ the particle swarm optimization to seek efficiently the optimal parameters of $PI^{\lambda}D^{\mu}$ controller. The robustness study is made for this controller against parameter variation of AVR system. This work has been simulated in MATLAB environment with FOMCON (Fractional Order Modeling and Control) tool box. The proposed $PSOPI^{\lambda}D^{\mu}$ controller has superior performance and robust compared to GA tuned $PI^{\lambda}D^{\mu}$ controller. The results are also compared with PSO tuned PID controller.

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1. INTRODUCTION

PID controllers are simple and well known for process control applications and also for simple feedback control mechanisms. The biggest challenge lies in tuning the parameters of the PID controller. Traditional tuning methods such as Ziegler and Nichols are available but do not give optimum performance [1]. AI techniques such as fuzzy logic, neural networks, neural-fuzzy logic have been widely used to proper tuning of PID controller parameters [2]-[4]. Tuning of PID controller parameters in off line made easy with the advent of heuristic optimization techniques [5]-[7]. Genetic Algorithms and Particle swarm Optimization are very popularly used random search heuristic optimization techniques for tuning PID controller parameters [6],[8]. These techniques have very high probability to achieve global optimum solution.

Since last decade the fractional order PID controllers are widely accepted in place of integer order PID controller [9],[10]. It has been proved that fractional order PID controller has superior performance compared to integer order PID controller [9]. The problem with fractional order PID controller is that it has five parameters need to be tuned, where as integer order PID controller has three parameters need to be tuned. This makes one step tuning of fractional order PID controller difficult compared to integer order PID controller. In this paper particle swarm optimization is used to tune the $PI^{\lambda}D^{\mu}$ controller in MATLAB/FOMCON environment. In this paper robustness study is made by comparing the results obtained through genetic algorithm based $PI^{\lambda}D^{\mu}$ controller.

2. RESEARCH METHOD

2.1. Automatic Voltage Regulator (AVR) System

Basic purpose of an AVR system is to control the terminal voltage of a synchronous generator by manipulating excitation. An AVR system basically contains four components namely Amplifier, Exciter, Synchronous generator and Sensor. One of the main cause of change in terminal voltage is reactive power consumption of the load. This change in voltage can be compensated by controlling the excitation to the generator. The block diagram of AVR system after linearization is presented in Figure 1.

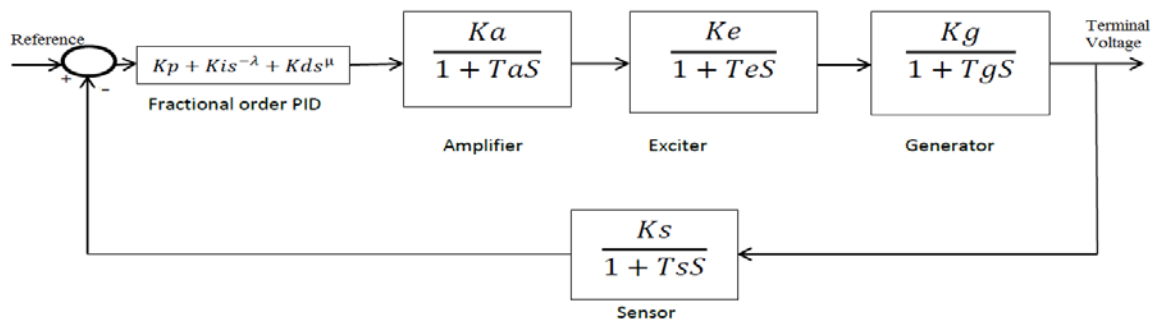


Figure 1. Block diagram of AVR system

The parameters of the generator of an AVR system depends on the load and the parameters of the remaining components depends on their design. The nominal range of the parameters are as follows [6].

$$\begin{aligned}
 &10 < K_a < 40; 0.02s < T_a < 1s \\
 &1 < K_e < 10; 0.4s < T_e < 1s \\
 &K_g \text{ and } T_g \text{ depends on the load } 0.7 < K_g < 1; 1s < T_g < 2s \\
 &0.01s < T_s < 0.06s \text{ and } K_s = 1
 \end{aligned}$$

2.2. Particle Swarm Optimization

Particle swarm optimization method was introduced by Kennedy and Eberhart in 1995. It is evolutionary optimization technique and stochastic method, developed by observing the social movement of swarms such as fish schooling and bird flocking. This method is robust in solving problems featuring nonlinearity, non differentiability, multiple optima and high dimensionality. It has stable convergence characteristics with good computational efficiency and easily implementable. Unlike other evolutionary methods where the evolutionary operators manipulate the particle, each particle in PSO flies in the search space with velocity which is dynamically adjusted according to its own flying experience and flying experience of its companions’.

At the beginning PSO algorithm introduces ‘N’ number of particles randomly. The objective function value is obtained for each particle. Then based on the flying velocity of the particle and its group the new population of particles are generated for next generation in seeking still better solution. The best value obtained by the particle so far is called pbest and the best value obtained among all the particles is called gbest. Each particle in the group updates their velocity based on the pbest and gbest as given in equation (1) and (2).

Let us assume jth particle is represented as $x_j = (x_{j,1}, x_{j,2}, \dots, x_{j,n})$ in n dimensional space. The previous best position of the jth particle is recorded as $pbest_j = (pbest_{j,1}, pbest_{j,2}, \dots, pbest_{j,n})$. The best particle among the group is represented by gbestg. The velocity of the particle j is represented as $v_j = (v_{j,1}, v_{j,2}, \dots, v_{j,n})$. The calculation of modified velocity and position of each particle using velocity and distance through $pbest_{j,g}$ to $gbestg$ is done as shown in the following formulas:

$$v_{j,n}(t+1) = w \cdot v_{j,n}(t) + c_1 \cdot rand() \cdot (pbest_{j,n} - x_{j,n}(t)) + c_2 \cdot rand() \cdot (gbest_g - x_{j,n}(t)) \tag{1}$$

$$x_{j,n}(t+1) = x_{j,n}(t) + v_{j,n}(t+1) \tag{2}$$

$$j = 1, 2, \dots, N$$

$$n=1, 2, \dots, M$$

Where,

- N number of particles in a group
- M number of members in a particle
- t generation number
- $v_{j,n}(t)$ velocity of particle j at generation t
- w inertia weight factor
- c_1, c_2 acceleration constant
- rand() Random number between 0 and 1
- $x_{j,n}(t)$ current position of particle j at generation t
- pbest_j pbest of particle j
- gbest_g gbest of the group

The updated particles are the population for next generation and continue the above procedure up to the specified number of generations. The better solution is obtained at each subsequent generation.

2.3. Fractional Order systems

2.3.1. Fractional Order Calculus

Some of the practical systems could be well described using fractional order differential equations rather than integer order differential equations, in 1695, L'Hopital coined the word fractional order calculus [11]. Since then Euler, Laplace, Fourier, Able, Riemann, and Lurel worked on this. The research on the fractional order calculus is accelerated from 1884. The basi operator in the fractional order calculus is differintegral. This name has come because a single operator represents the fractional order derivative and fractional order integrator. The differintegral is represented as following:

$$aD_t^\alpha = \begin{cases} \frac{d^\alpha}{dt^\alpha} R(\alpha) > 0 \\ 1 & R(\alpha) = 0 \\ \int_a^t (d\tau)^{-\alpha} R(\alpha) < 0 \end{cases} \tag{3}$$

Where 'a' and 't' are the limits of the operator. The operator 'α' is the order of the operation and belongs to R (any rational number) but 'α' could also be a complex number [12]. Two definitions used for the general fractional differintegral are the Grunwald-Letnikov (GL) definition and the Riemann-Louville (RL) definition [13],[14]. The GL is given here:

$$aD_t^\alpha f(t) = \lim_{h \rightarrow 0} h^{-\alpha} \sum_{j=0}^{\frac{t-a}{h}} (-1)^j \binom{\alpha}{j} f(t-jh) \tag{4}$$

The fractional differintegral defined by RL is

$$aD_t^\alpha f(t) = \frac{1}{\Gamma(n-\alpha)} \frac{d^n}{dt^n} \int_a^t \frac{f(\tau)}{(t-\tau)^{(\alpha-n+1)}} d\tau \tag{5}$$

for $(n-1 < \alpha < n)$ and $\Gamma(\cdot)$ is the Gamma function.

2.3.2. Fractional Order PID Controllers

For last one-decade fractional order PID controllers are became very popular among researchers, because its robust performance and fast response. The fractional order PID controller transfer function G(s) is defined as in (6). Figure 2 gives the graphical presentation of PID controller.

$$G(s) = Kp + Kis^{-\lambda} + Kds^\mu \tag{6}$$

Where,

- Kp → Proportional gain
- Ki → Integral gain
- Kd → Derivative gain
- λ → order of the integrator
- μ → order of the differentiator

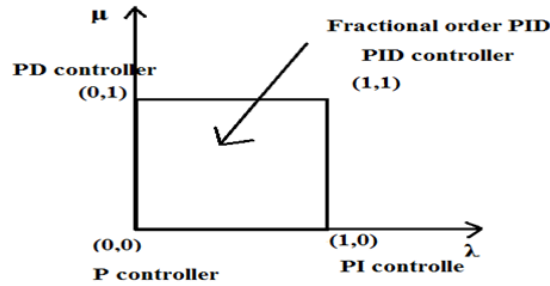


Figure 2. Graphical representation of fractional order PID controller

The fractional order PID controller needs tuning of above five parameters appropriately to make the system performance optimum.

2.4. Performance Evaluation of $PI^\lambda D^\mu$ Controller

For each particle in the population, which represents five parameters of the controller, the AVR system is simulated. Based on the system response the time domain parameters of the response such as Peak overshoot (M_p), Rise time (t_r), Settling time (t_s) and Steady state error (E_{ss}) are evaluated. These four time domain parameters depends on five parameters of the controller ($K_p, K_i, K_d, \lambda, \mu$). The system is good when these four parameters are minimum. The performance criterion (O) of the $PI^\lambda D^\mu$ controller is defined as in (7).

$$O(K_p, K_i, K_d, \lambda, \mu) = \beta(M_p + E_{ss}) + (1 - \beta)(t_s + t_r) \tag{7}$$

Since the objective function (O) has to be minimised, the fitness function (f) is defined as in (8)

$$f = 1/O \tag{8}$$

More importance is given to reduce peak overshoot and best value for β is found to be 0.92.

3. RESULTS AND ANALYSIS

The proposed robust analysis of fractional order PID controller optimized by PSO in AVR system is carried out through MATLAB/SIMULINK in combination with fractional order systems tool box FOMCON. The PSO algorithm is implemented through MATLAB code. The search space for the PSO- $PI^\lambda D^\mu$ is defined as follows:

The controller parameters search space is chosen as

$$3 < K_p < 8, 0.5 < K_i < 2, 0.5 < K_d < 1.5, 0 < \lambda < 1.5, 0 < \mu < 1.5$$

The velocity limits for each parameter and limits of inertial factor is chosen as

$$-1.2 < V_{min}(K_p) < 1.2, -0.35 < V_{min}(K_i) < 0.35, -0.2 < V_{min}(K_d) < 0.2 \\ -0.15 < V_{min}(\lambda) < 0.15, 0.15 < V_{min}(\mu) < 0.15, 0.4 < w < 0.9$$

When AVR system shown in Figure 1 is optimized through PSO- $PI^\lambda D^\mu$ and GA- $PI^\lambda D^\mu$ for the system parameters shown in Table 1, the convergence of the objective function for 100 generations is presented in Figure 3. It shows that the convergence in the case of PSO- $PI^\lambda D^\mu$ is superior than GA- $PI^\lambda D^\mu$. The optimum controller parameters and time response is shown in Table 2 and Figure 4. Table 2 also presents the performance comparison for controller parameters tuned by RGAPID and PSOPID. Among all these methods the PSO- $PI^\lambda D^\mu$ controller gives better time response.

Table 1. Parameters of AVR system

| K_a | T_a | K_e | T_e | K_g | T_g | K_s | T_s |
|-------|-------|-------|-------|-------|-------|-------|-------|
| 10 | 0.1 | 1 | 0.4 | 1 | 1 | 1 | 0.01 |

Table 2. Performance comparison of PSO-PI^λD^μ with other tuning methods

| Method | Kp | Ki | Kd | λ | μ | Ts(s) | Tr(s) | Osh(%) |
|------------------------------------|--------|--------|--------|--------|--------|--------|--------|--------|
| RGAPID | 0.6820 | 0.2660 | 0.1790 | 1 | 1 | 1.2682 | 1.0668 | 4.00 |
| PSOPID | 0.6570 | 0.5389 | 0.2458 | 1 | 1 | 0.4025 | 0.2767 | 1.16 |
| GAPID ^λ D ^μ | 5.6471 | 1.2471 | 0.6667 | 1.1471 | 1.4824 | 0.3000 | 0.0900 | 4.63 |
| PSOPID ^λ D ^μ | 4.0143 | 0.8963 | 0.5014 | 1.3349 | 1.4154 | 0.2000 | 0.13 | 2.69 |

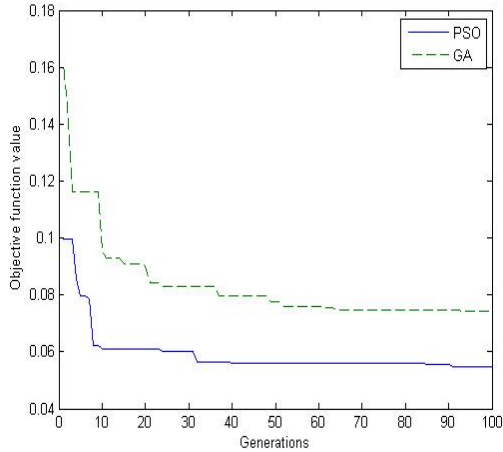


Figure 3. Convergence of objective function over 100 generations

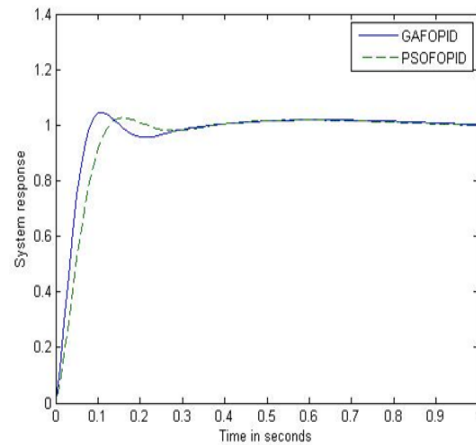


Figure 4. Time response of GAFOPID and PSOFOPID for Kg=1 and Tg=1

By observing the time response in Figure 4, the settling time and peak overshoot is less in the case of PSOPID^λD^μ compared to GAPID^λD^μ, PSOPID and RGAPID controllers. The rise time is marginally high compared to other controllers.

To study the robustness of the AVR system for PSOPID^λD^μ controller, the optimum controller parameters are obtained for 24 combinations of quantized values of generator parameters in their variation range. Kg and Tgis quantized as {0.7, 0.8, 0.9, 1}, {1, 1.2, 1.4, 1.6, 1.8, 2} respectively. The obtained optimum controller parameters and time response parameters are shown in Table 3, Figure 5 and Figure 6.

Table 3. Optimum controller parameters and time response parameters tuned by PSOPID^λD^μ

| S.No. | Generator Parameters | | Controller Parameters | | | | | Time response parameters | | |
|--|----------------------|-----|-----------------------|--------|--------|--------|--------|--------------------------|---------|-------|
| | Kg | τg | Kp | Ki | Kd | λ | μ | Ts(sec) | Tr(sec) | Mp(%) |
| 1 | 0.7 | 1 | 4.0710 | 1.0384 | 0.6099 | 1.0849 | 1.3569 | 0.17 | 0.18 | 1.4 |
| 2 | 0.8 | 1 | 4.3582 | 1.8241 | 0.6206 | 1.3993 | 1.3760 | 0.22 | 0.14 | 3.23 |
| 3 | 0.9 | 1 | 6.5388 | 1.1746 | 0.7393 | 1.0300 | 1.500 | 0.30 | 0.08 | 4.16 |
| 4 | 0.7 | 1.2 | 3.666 | 1.7325 | 0.7984 | 0.6470 | 1.2902 | 0.28 | 0.17 | 3.67 |
| 5 | 0.8 | 1.2 | 4.2216 | 1.0428 | 0.6581 | 1.3410 | 1.3445 | 0.23 | 0.17 | 2.21 |
| 6 | 0.9 | 1.2 | 3.9876 | 0.9057 | 0.5704 | 1.3173 | 1.3807 | 0.16 | 0.17 | 1.95 |
| 7 | 0.7 | 1.4 | 6.4880 | 0.6434 | 0.9432 | 0.8358 | 1.3947 | 0.21 | 0.14 | 2.43 |
| 8 | 0.8 | 1.4 | 4.9261 | 1.0149 | 0.8350 | 1.0264 | 1.3447 | 0.18 | 0.18 | 1.66 |
| 9 | 0.9 | 1.4 | 4.2029 | 0.6006 | 0.6550 | 1.1792 | 1.3645 | 0.17 | 0.17 | 1.60 |
| 10 | 1 | 1.4 | 3.0928 | 0.7700 | 0.5488 | 1.0379 | 1.3269 | 0.19 | 0.20 | 1.76 |
| 11 | 0.7 | 1.6 | 7.5407 | 0.8775 | 1.1104 | 1.1828 | 1.3978 | 0.21 | 0.14 | 2.95 |
| 12 | 0.8 | 1.6 | 5.4834 | 0.5086 | 0.8613 | 1.3337 | 1.337 | 0.16 | 0.17 | 1.74 |
| 13 | 0.9 | 1.6 | 3.0835 | 1.0773 | 0.6782 | 0.9281 | 1.2780 | 0.21 | 0.22 | 1.9 |
| 14 | 1 | 1.6 | 3.0362 | 0.5779 | 0.5932 | 1.1169 | 1.2971 | 0.21 | 0.22 | 1.23 |
| 15 | 0.7 | 1.8 | 4.8817 | 1.1221 | 0.9568 | 1.0393 | 1.3078 | 0.21 | 0.22 | 1.92 |
| 16 | 0.8 | 1.8 | 5.0936 | 1.1821 | 0.9861 | 1.0232 | 1.3260 | 0.25 | 0.17 | 2.59 |
| 17 | 1 | 1.8 | 4.5345 | 0.6019 | 0.7565 | 1.4763 | 1.3603 | 0.17 | 0.17 | 1.66 |
| 18 | 0.7 | 2 | 6.9420 | 0.7572 | 1.1710 | 1.2067 | 1.3611 | 0.17 | 0.18 | 1.99 |
| 19 | 0.8 | 2 | 5.7915 | 0.5640 | 0.9942 | 1.2597 | 1.3505 | 0.18 | 0.19 | 1.82 |
| 20 | 0.9 | 2 | 4.2913 | 0.9132 | 0.8873 | 0.9023 | 1.3092 | 0.19 | 0.20 | 1.82 |
| 21 | 1 | 2 | 5.7162 | 0.7704 | 0.9614 | 1.0908 | 1.3838 | 0.37 | 0.14 | 2.59 |
| Average values of PI ^λ D ^μ (AVPI ^λ D ^μ) | | | 4.7641 | 0.9095 | 0.7820 | 1.1310 | 1.3552 | | | |

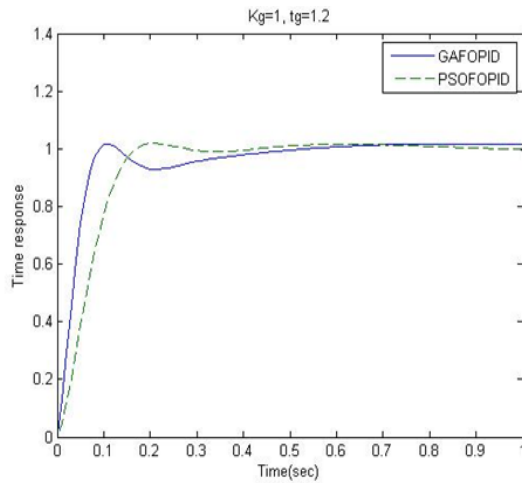


Figure 5. Time response of $GAPID^\mu$ and $PSOPID^\mu$ $K_g=1$ and $T_g=1.2$

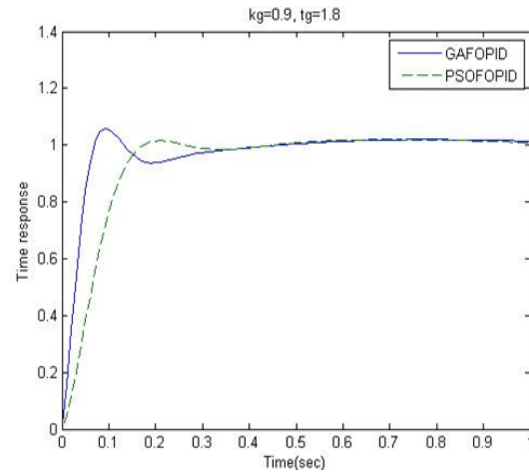


Figure 6. Time response of $GAPID^\mu$ and $PSOPID^\mu$ $K_g=0.9$ and $T_g=1.8$

The Table 3, Figure 5 and Figure 6 clearly shows that the time response of $PSOPID^\mu$ controller tuned against parameter variations achieves very good time response. The peak overshoot and settling time is less compared to GA tuned PI^μ controller i.e 4.63% and 0.3 seconds respectively (Table 2). However the rise time is marginally high which is normally not so important if the settling time is less.

In this Paper to compare the robustness of the $PSOPID^\mu$ controller, $GAPID^\mu$ controller has been considered. Similar to the $PSOPID^\mu$ controller, optimum controller parameters are obtained for parameter variation for $GAPID^\mu$ controller. The results are presented in Table 4 [15].

Table 4. Optimum controller parameters and time response parameters tuned by $GAPID^\mu$

| S.No. | Generator Parameters | | Controller Parameters | | | | | Time response parameters | | |
|---|----------------------|----------|-----------------------|--------|--------|-----------|-------|--------------------------|-------------------|-----------|
| | K_g | τ_g | K_p | K_i | K_d | λ | μ | $T_s(\text{sec})$ | $T_r(\text{sec})$ | $M_p(\%)$ |
| 1 | 0.7 | 1 | 6.6824 | 1.8118 | 0.9020 | 1.1529 | 1.5 | 0.37 | 0.09 | 2.17 |
| 2 | 0.8 | 1 | 6.6824 | 2.4118 | 0.9255 | 1.0941 | 1.5 | 0.34 | 0.08 | 5.00 |
| 3 | 0.9 | 1 | 4.8000 | 1.1765 | 0.7059 | 1.2882 | 1.5 | 0.44 | 0.09 | 1.44 |
| 4 | 1 | 1 | 5.5294 | 1.0235 | 0.7216 | 1.4471 | 1.5 | 0.35 | 0.08 | 4.88 |
| 5 | 0.7 | 1.2 | 7.3412 | 1.9412 | 1.1294 | 1.2471 | 1.5 | 0.42 | 0.09 | 2.50 |
| 6 | 0.8 | 1.2 | 7.3882 | 1.5647 | 1.0118 | 0.9765 | 1.5 | 0.34 | 0.08 | 3.70 |
| 7 | 0.9 | 1.2 | 6.0706 | 1.2706 | 0.8154 | 1.2882 | 1.5 | 0.36 | 0.10 | 1.99 |
| 8 | 1 | 1.2 | 4.9647 | 1.1647 | 0.7529 | 1.3294 | 1.5 | 0.42 | 0.10 | 1.85 |
| 9 | 0.7 | 1.4 | 7.6471 | 1.7176 | 1.2784 | 0.9882 | 1.5 | 0.45 | 0.09 | 1.85 |
| 10 | 0.8 | 1.4 | 7.7647 | 1.3765 | 1.0667 | 1.3588 | 1.5 | 0.35 | 0.10 | 2.40 |
| 11 | 0.9 | 1.4 | 6.0706 | 1.3882 | 0.9804 | 1.0059 | 1.5 | 0.42 | 0.09 | 2.00 |
| 12 | 1 | 1.4 | 5.7882 | 1.1882 | 0.9020 | 1.0412 | 1.5 | 0.41 | 0.09 | 2.40 |
| 13 | 0.7 | 1.6 | 9.3882 | 1.5059 | 1.4588 | 1.2471 | 1.5 | 0.40 | 0.09 | 2.50 |
| 14 | 0.8 | 1.6 | 8.6118 | 1.1647 | 1.2627 | 1.3588 | 1.5 | 0.37 | 0.09 | 2.70 |
| 15 | 0.9 | 1.6 | 5.4588 | 2.4824 | 1.1451 | 0.2000 | 1.5 | 0.40 | 0.09 | 2.27 |
| 16 | 1 | 1.6 | 7.0118 | 1.3882 | 1.0980 | 1.2118 | 1.5 | 0.39 | 0.08 | 3.97 |
| 17 | 0.7 | 1.8 | 8.4235 | 2.1176 | 1.6784 | 0.5647 | 1.5 | 0.47 | 0.09 | 2.10 |
| 18 | 0.8 | 1.8 | 9.0118 | 1.6588 | 1.5137 | 1.2706 | 1.5 | 0.42 | 0.08 | 3.45 |
| 19 | 0.9 | 1.8 | 8.0471 | 2.8588 | 1.5216 | 0.2741 | 1.5 | 0.34 | 0.07 | 5.90 |
| 20 | 1 | 1.8 | 7.9059 | 1.0353 | 1.2627 | 1.1000 | 1.5 | 0.38 | 0.08 | 4.50 |
| 21 | 0.7 | 2 | 9.4118 | 1.0471 | 1.7961 | 1.2765 | 1.5 | 0.51 | 0.09 | 1.59 |
| 22 | 0.8 | 2 | 8.8235 | 1.1882 | 1.5922 | 1.0765 | 1.5 | 0.46 | 0.09 | 2.32 |
| 23 | 0.9 | 2 | 8.1412 | 2.0706 | 1.4510 | 0.1706 | 1.5 | 0.35 | 0.09 | 3.60 |
| 24 | 1 | 2 | 9.3176 | 1.5294 | 1.4824 | 1.1000 | 1.5 | 0.35 | 0.07 | 5.62 |
| Average values of $PIAD_\mu$ ($AVPI^\mu$) | | | 7.3451 | 1.5868 | 1.1856 | 1.0445 | 1.5 | | | |

Robustness study is made by taking the average controller parameters in both the cases. The performance of the both the systems against parameter variations with fixed average $PI^{\lambda}D^{\mu}$ controller parameters (calculated in Table 3 and Table 4) is presented in Table 5, Figure 7 and Figure 8.

Table 5. Time response for fixed $PI^{\lambda}D^{\mu}$ controller parameters against parameter variations

| Kg | τ_g | Method | Kp | Ki | Kd | λ | μ | Ts(s) | Tr(s) | Osh (%) |
|------|----------|------------------------------|--------|--------|--------|-----------|--------|-------|-------|---------|
| 0.77 | 1.50 | RGA PID | 0.7246 | 0.3601 | 0.1643 | 1 | 1 | 1.19 | 0.81 | 2.16 |
| | | AVGAPI $^{\lambda}D^{\mu}$ | 7.3451 | 1.5868 | 1.1856 | 1.0445 | 1.5 | 0.97 | 0.1 | 2.07 |
| | | AVGPSOPI $^{\lambda}D^{\mu}$ | 4.7641 | 0.9095 | 0.7820 | 1.1310 | 1.3552 | 0.18 | 0.19 | 1.94 |
| 0.79 | 1.15 | RGA PID | 0.6598 | 0.2927 | 0.1743 | 1 | 1 | 1.11 | 0.94 | 0.29 |
| | | AVPI $^{\lambda}D^{\mu}$ | 7.3451 | 1.5868 | 1.1856 | 1.0445 | 1.5 | 0.42 | 0.07 | 6.34 |
| | | AVGPSOPI $^{\lambda}D^{\mu}$ | 4.7641 | 0.9095 | 0.7820 | 1.1310 | 1.3552 | 0.39 | 0.13 | 4.59 |
| 0.85 | 1.30 | RGA PID | 0.7379 | 0.2862 | 0.1643 | 1 | 1 | 0.90 | 0.84 | 6.33 |
| | | AVPI $^{\lambda}D^{\mu}$ | 7.3451 | 1.5868 | 1.1856 | 1.0445 | 1.5 | 0.41 | 0.07 | 5.69 |
| | | AVGPSOPI $^{\lambda}D^{\mu}$ | 4.7641 | 0.9095 | 0.7820 | 1.1310 | 1.3552 | 0.37 | 0.14 | 4.27 |
| 0.75 | 1.67 | RGA PID | 0.6321 | 0.3601 | 0.2643 | 1 | 1 | 1.80 | 1.07 | 0.06 |
| | | AVPI $^{\lambda}D^{\mu}$ | 7.3451 | 1.5868 | 1.1856 | 1.0445 | 1.5 | 1.11 | 0.53 | 2.56 |
| | | AVGPSOPI $^{\lambda}D^{\mu}$ | 4.7641 | 0.9095 | 0.7820 | 1.1310 | 1.3552 | 0.9 | 0.45 | 2.55 |
| 0.99 | 1.45 | RGA PID | 0.7080 | 0.3601 | 0.1652 | 1 | 1 | 0.77 | 0.77 | 1.96 |
| | | AVPI $^{\lambda}D^{\mu}$ | 7.3451 | 1.5868 | 1.1856 | 1.0445 | 1.5 | 0.38 | 0.07 | 6.79 |
| | | AVGPSOPI $^{\lambda}D^{\mu}$ | 4.7641 | 0.9095 | 0.7820 | 1.1310 | 1.3552 | 0.35 | 0.13 | 5.48 |
| 0.99 | 1.96 | RGA PID | 0.6030 | 0.3601 | 0.1757 | 1 | 1 | 1.41 | 0.99 | 0.04 |
| | | AVPI $^{\lambda}D^{\mu}$ | 7.3451 | 1.5868 | 1.1856 | 1.0445 | 1.5 | 1.1 | 0.10 | 2.60 |
| | | AVGPSOPI $^{\lambda}D^{\mu}$ | 4.7641 | 0.9095 | 0.7820 | 1.1310 | 1.3552 | 0.92 | 0.19 | 2.82 |

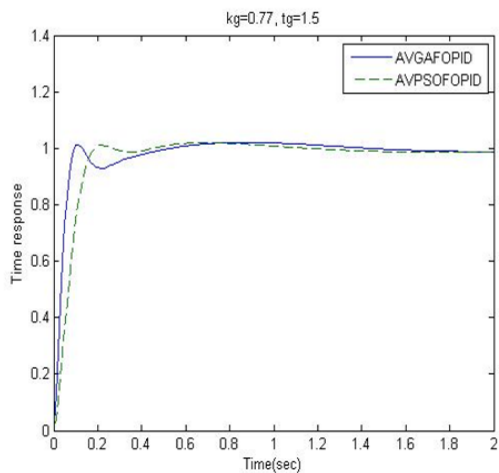


Figure 7. Time response of GAPI $^{\lambda}D^{\mu}$ and PSOPI $^{\lambda}D^{\mu}$ for fixed controller parameters (Kg=0.77,Tg=1.5)

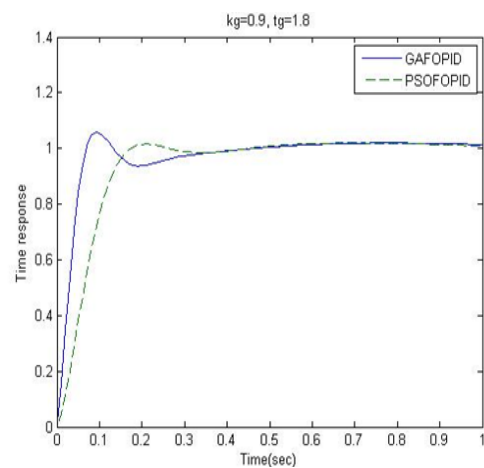


Figure 8. Time response of GAPI $^{\lambda}D^{\mu}$ and PSOPI $^{\lambda}D^{\mu}$ for fixed controller Parameters (Kg=0.9,Tg=1.8)

The results shown in Table 5, Figure 7 and Figure 8 clearly indicates, even when PSOPI $^{\lambda}D^{\mu}$ controller parameters are set fixed to average values, the time response of the AVR system is robust against parameter variations.

4. CONCLUSION

This work has been simulated in MATLAB/SIMULINK environment in combination with FOMCON tool box. The obtained results show that when fractional order PID controller is tuned with PSO algorithms, the results obtained is superior than when tuned with PSOPID and GAPI $^{\lambda}D^{\mu}$. Further robustness study shows that the AVR system is more robust with PSOPI $^{\lambda}D^{\mu}$ against parameter variations compared to GAPI $^{\lambda}D^{\mu}$ controller.

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