

Nonlinear control strategy of single-phase unified power flow controller

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ABSTRACT

In this work we propose a nonlinear control strategy of single-phase unified power flow controller (UPFC), using in order to enhance energy quality parameters of a perturbed single-phase power grid supplying nonlinear loads. The control objectives are: i) The current harmonics and the reactive power compensation, that ensure a satisfactory power factor correction (PFC) at the point of common coupling (PCC); ii) compensation of the voltage perturbations (harmonics and sags of voltage) in order to ensure the desired level, of load voltage, without distortion; iii) DC bus voltage regulation. The considered control problem entails several difficulties including the high system dimension and the strong system nonlinearity. The problem is dealt with by designing a nonlinear controller with structure including three control loops. The inner-loop regulator is designed using the Lyapunov technique to compensate the current harmonics and reactive power. The intermediary-loop regulator is designed using the Backstepping technique to compensate the voltage perturbations. The outer-loop regulator is designed using a linear PI to regulate the DC bus voltage. The control stability is proved theoretically and through simulations, these latter show the effectiveness and strong robustness of the proposed control, and prove that the above-mentioned objectives are achieved.

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1. INTRODUCTION

Nowadays, the increased use of computer equipments and power electronics-based devices on electrical grids contributes to the degradation of the electrical energy quality. In fact, the power electronics dedicated to electrical engineering as well as the electronics of computer equipments essentially contribute to the proliferation of harmonic disturbances. These devices, called nonlinear or distorting loads, generate harmonic currents which cause the distortion of the voltage waveform at the PCC (due to load current in the grid impedance) [1]. In addition, the presence of these harmonic disturbances in electrical installations becomes a real 'headache' for producers and users of electricity in the industrial, tertiary and domestic sector.

Now, the concerns of distributors and consumers of electricity focus on improving the power factor. The harmonic pollution that affects the electricity supply grid has led electricity producers and distributors to

take this new constraint seriously into account with a view to finding solutions for a better of the electrical energy quality.

In recent times, active power filters (APFs) have proved to be the best modern solution to cope with electrical power quality issues. Various APFs configurations exist namely: shunt APF [2-4], series APF [5] and UPFC system [6], which combines both parallel and series structures of APF. The UPFC system injects at PCC, appropriate current and voltage signals of harmonics compensation, which ensure the cancellation of all disturbing harmonics, in the electrical distribution networks, upstream of the PCC [7-15].

In this study, we are interested in single-phase UPFC system connected between the perturbed power grids and the nonlinear loads. The problem of controlling single-phase UPFC system has aroused a great of interest over the last years. In this respect, several control strategies have been proposed. The work [16] presented a microcontroller program used to control the single-phase UPFC system. The obtained experimental result showed a good agreement with the simulation result. The paper [17] proposed a real-time control system for a single-phase UPFC, both obtained simulation and experiment results have proved the effectiveness of the proposed control system. In [18], an attempt was made to separate the series part and the shunt part of UPFC, this gives the possibility to install series and shunt parts of UPFC at different required locations. Finally the responses of two modified DC link UPFC are compared. In [6], an implementation for controller to control the single-phase UPFC using the DSP-TMS320C31 is developed. In [19], a new hybrid technique which combines the radial basis function (RBF) neural network with the sliding mode technique is proposed to design a UPFC system for power flow control of an electric power transmission system. In [20], a proportional resonant (PR) controller is used to generate switching signals for each leg of the input full-bridge converter; by synthesizing an appropriate injection voltage, the half-bridge inverter controls the power flow of the transmission line; in addition to simulation of system by MATLAB/Simulink, an experiment realization on the UPFC was carried out. In all the previous studies, the objective was controlling the power flow in the transmission systems between the power grids and the consumer loads in order to improve the quality of electrical energy; but note that the performances of the controllers which were proposed in [6, 16-21] were not quantified by the indication of the current THD and the voltage THD. Furthermore, in most previous works, the grid internal impedance was supposed to be zero [6, 16, 18, 19]. In real life, this impedance is nonzero and must be considered in single-phase power grid model.

In the present paper, the problem of controlling single-phase UPFC system, associated with perturbed single-phase power grids supplying nonlinear loads, is addressed considering reduced-part topology. A novel nonlinear controller is designed and formally shown to meet the PFC requirement, the compensation of the voltage perturbations, and the regulation of DC bus voltage. A major feature of the new control design is that none of the limitation of previous controllers is present i.e. the grid internal impedance is not neglected. The structure of proposed nonlinear controller contains three control loops. The inner-loop is designed, using the Lyapunov technique, to ensure a perfect PFC. The intermediary-loop is designed, using the Backstepping technique, to compensate the voltage perturbations. The outer-loop is established in order to regulate the DC bus voltage, through filtered PI regulator. The closed-loop control system analysis is presented in this paper to proof, that all control objectives are actually achieved by the proposed controller. Several simulation results show that additional robustness features are reached. Compared to the controllers previously cited, the new nonlinear controller enjoys several features including:

- The present controller is designed for the single-phase UPFC system with reduced topology, this latter features less switches and a smaller number of gate drivers, compared to the Two-Leg Full-Bridge topology used in [6, 18, 19, 20]. As a result, the present nonlinear controller is simpler to implement because it involves less control signals to generate and apply.
- The control design proposed, in works [6, 16, 18, 19], relies upon very restrictive assumption e.g. the internal impedance of the single-phase power grid was supposed to be zero [6, 16, 18, 19] which entails an approximate model used in control design (because the model dimension is smaller than that of the true system). The present study does not rely on this above assumption. Therefore, the system model used in the control design is of higher dimension leading to a higher performances controller.
- The performances of the proposed controller were quantified by calculation of the THD values of current and voltage. Such a study based in terms of THD current and voltage was missing in the all previous works [6, 16-21].
- By using a rigorous theoretical analysis, the control objectives (i.e. PFC, compensation of voltage perturbations and DC voltage regulation) are actually achieved. Such a formal analysis was missing in the all previous works [6, 16-21].

This paper organized as follows: Section 2 is devoted to the description and modeling of the single-phase UPFC system. The design of the nonlinear controller is treated in section 3. The closed-loop control system analysis is presented in section 4. In section 5, the controller performances are illustrated by several numerical simulations.

2. PROBLEM FORMULATION

2.1. Single-phase UPFC topology

The proposed single-phase UPFC system is shown in Figure 1. It contains two inverters back-to-back, connected to the DC bus side including two identical energy storage capacitors C_{dc} . The IGBT-diode based inverters operate in accordance with PWM [22, 23]. From the AC side, the single-phase UPFC system is connected on the one hand in parallel with the perturbed power supply grid through filtering inductor (L_p, r_p), on the other hand in series with a nonlinear load via filtering inductor (L_s, r_s), capacitor C_s and current transformer. The perturbed power grid is modeled by a disturbed voltage source v_g in series with an internal impedance formed by a resistor r_g and an inductor L_g .

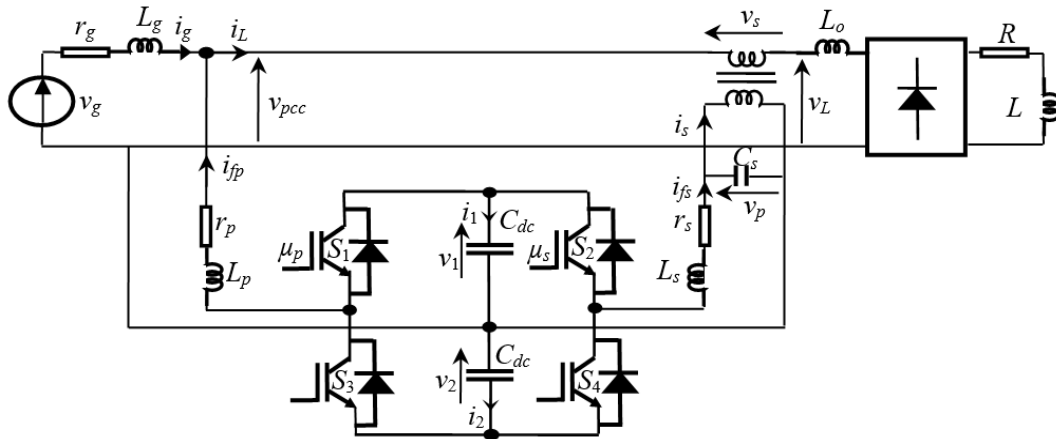


Figure 1. Single-phase UPFC system

The switching functions μ_p and μ_s of the single-phase UPFC system are defined as:

$$\mu_p = \begin{cases} +1 & \text{if } S_1 \text{ is ON and } S_3 \text{ is OFF} \\ -1 & \text{if } S_1 \text{ is OFF and } S_3 \text{ is ON} \end{cases}; \mu_s = \begin{cases} +1 & \text{if } S_2 \text{ is ON and } S_4 \text{ is OFF} \\ -1 & \text{if } S_2 \text{ is OFF and } S_4 \text{ is ON} \end{cases}$$

The load current $i_L(t)$, in steady-state, is a periodic signal that can be expressed as (1).

$$i_L(t) = \sum_{h=1}^{\infty} I_h \sin(h\omega_g t + \varphi_h) \tag{1}$$

where I_h is the current harmonic amplitude of order h , φ_h is the « h » harmonic phase at the origin.

2.2. Single-phase UPFC modeling

The instantaneous model of the single-phase UPFC system is given by:

$$\frac{di_g}{dt} = (1/L_g)(-r_g i_g + v_g - v_s - v_L) \tag{2a}$$

$$\frac{di_{fp}}{dt} = (1/L_p)(-r_p i_{fp} + \frac{\mu_p v_0}{2} + \frac{v_d}{2} - v_s - v_L) \tag{2b}$$

$$\frac{dv_s}{dt} = (1/C_s)(m_s i_{fs} + m_s^2 i_L) \tag{2c}$$

$$\frac{di_{fs}}{dt} = (1/L_s)(-r_s i_{fs} + \frac{\mu_s v_0}{2} + \frac{v_d}{2} - \frac{v_s}{m_s}) \quad (2d)$$

$$\frac{dv_0}{dt} = (1/C_{dc})(-\mu_p i_{fp} - \mu_s i_{fs}) \quad (2e)$$

$$\frac{dv_d}{dt} = (1/C_{dc})(-i_{fp} - i_{fs}) \quad (2f)$$

where m_s is the transformation ratio of current transformer, $v_0 = v_1 + v_2$ and $v_0 = v_1 - v_2$.

The model (2a-f) is useful for building up an accurate simulator of the UPFC system. However, it cannot be based upon in the control design as it involves binary control inputs, namely μ_p and μ_s . This type of difficulty is generally overcome by resorting to average models where instantaneous signals are replaced by their average shapes. The signals are averaged over cutting intervals [22, 24]. The average model of the single-phase UPFC system is expressed as (3a), (3b), (3c), (3d), (3e), (3f):

$$\dot{x}_1 = (1/L_g)(-r_g x_1 + v_g - x_3 - v_L) \quad (3a)$$

$$\dot{x}_2 = (1/L_p)(-r_p x_2 + \frac{u_p x_5}{2} + \frac{x_6}{2} - x_3 - v_L) \quad (3b)$$

$$\dot{x}_3 = (1/C_s)(m_s x_4 + m_s^2 i_L) \quad (3c)$$

$$\dot{x}_4 = (1/L_s)(-r_s x_4 + \frac{u_s x_5}{2} + \frac{x_6}{2} - \frac{x_3}{m_s}) \quad (3d)$$

$$\dot{x}_5 = (1/C_{dc})(-u_p x_2 - u_s x_4) \quad (3e)$$

$$\dot{x}_6 = (1/C_{dc})(-x_2 - x_4) \quad (3f)$$

where: $x_1, x_2, x_3, x_4, x_5, x_6, u_p, u_s$ are respectively the averaged variables $i_g, i_{fp}, v_s, i_{fs}, v_0, v_d, \mu_p, \mu_s$.

3. CONTROLLER DESIGN

The proposed nonlinear controller for the system (3a-f) represented by Figure 2 will be developed in three major steps, respectively devoted to: i) the inner loop design, ii) the intermediary loop design, iii) and the outer loop design. The first step is to design an inner-loop control, using the Lyapunov technique, to ensure a perfect PFC. The second step is to design an intermediary-loop control, using the Backstepping technique, to ensure the compensation of voltage perturbations in the power grid. In the third step, an outer-loop control, involving filtered PI regulator, is built-up to achieve DC bus voltage regulation.

3.1. Current inner-loop design

According to the PFC requirement, the current x_1 provided by the single-phase power supply grid must be a sinusoidal signal in phase with the fundamental of grid voltage namely v_{g1} . To this end, the current x_2 injected by the single-phase UPFC system should follow as closely as possible its reference x_2^* as (4).

$$x_2^* = i_L - \beta v_{g1} \quad (4)$$

where $v_{g1} = E_1 \sin(\omega t)$, and β is any positive constant. As a matter of fact, the latter is allowed to be time-varying but it must converge to a constant value. That is, β stands as an additional control input. To achieve the PFC objective, we introduce the tracking error on the filter current x_2 .

$$z_1 = x_2 - x_2^* \quad (5)$$

Using (3b), the time-derivative of (5) yields the following dynamics of the error z_1 .

$$\dot{z}_1 = ((-r_p x_2 + (u_p x_5 / 2) + (x_6 / 2) - x_3 - v_L) / L_p) - (di_L / dt) + \dot{\beta} v_{g1} + \beta \dot{v}_{g1} \quad (6)$$

The control variable, noted μ_p , appears in (6) after a single derivation of the error z_1 . This control variable must now be determined in order to make z_1 -system globally asymptotically stable. To this end, we introduce the following Lyapunov function candidate:

$$V_1 = z_1^2 / 2 \quad (7)$$

Its dynamic is given by:

$$\dot{V}_1 = z_1 \dot{z}_1 \quad (8)$$

To ensure z_1 -system global asymptotical stability, it is sufficient to choose the control law μ_p so that $\dot{V}_1 = -c_1 z_1$, and then we obtain:

$$\dot{z}_1 = -c_1 z_1 \quad (9)$$

where c_1 is any positive parameter. Comparing (9) and (6) yields the following control law:

$$u_p = (2r_p x_2 + 2x_3 - x_6 + 2v_L - 2L_p c_1 z_1 + 2L_p \frac{di_L}{dt} - 2L_p \dot{\beta} v_{g1} - 2L_p \beta \dot{v}_{g1}) / x_5 \quad (10)$$

As this control law μ_p involves the dynamics of the signal β , it follows from (6) that the signal β and its first time-derivative must be available.

3.2. Voltage intermediary-loop design

In order to compensate the voltage disturbances at the PCC, the load voltage v_L must be a sinusoidal signal at the terminals of sensitive load:

$$v_L \rightarrow v_L^* = V_{L\max} \sin(\omega t) \quad (11)$$

According to the voltage disturbances compensation requirement, the series voltage x_3 injected by the single-phase UPFC system should follow as closely as possible its reference signal x_3^* as (12).

$$x_3^* = v_{pcc} - v_L^* \quad (12)$$

where v_{pcc} is the voltage at the point of common coupling.

The proposed regulator must force the voltage x_3 to track its reference signal x_3^* . The synthesis used is known as the Backstepping technique [25] and is carried out in two steps.

– Step 1: Stabilization of tracking error z_2 .

$$z_2 = x_3 - x_3^* \quad (13)$$

The time-derivative of (13) yields the following dynamics of the error z_2 :

$$\dot{z}_2 = \left((m_s x_4 / C_s) + (m_s^2 i_L / C_s) - \dot{x}_3^* \right) \quad (14)$$

We use the following Lyapunov candidate function:

$$V_2 = z_2^2 / 2 \quad (15)$$

Its dynamic is given by:

$$\dot{V}_2 = \left((m_s x_4 / C_s) + (m_s^2 i_L / C_s) - \dot{x}_3^* \right) z_2 \quad (16)$$

Consider that $(m_s x_4 / C_s)$ is the effective control, σ is the stabilizing function, it is sufficient to take:

$$\sigma = -c_2 z_2 - (m_s^2 i_L / C_s) + \dot{x}_3^* \quad (17)$$

where c_2 is a positive parameter.

To study the stability of the above control, we define the following corresponding error z_3 :

$$z_3 = (m_s x_4 / C_s) - \sigma \quad (18)$$

Then, we get the equation of z_2 dynamics, and that of V_2 derivative:

$$\dot{z}_2 = -c_2 z_2 + z_3 \quad (19)$$

$$\dot{V}_2 = -c_2 z_2^2 + z_2 z_3 \quad (20)$$

– Step 2: Stabilization of the subsystem (z_2, z_3)

In this step 2, we present the design of the controller that makes the errors (z_2, z_3) to tend to zero. The z_3 dynamics is given in (21):

$$\dot{z}_3 = \left(m_s (-r_s x_4 + (u_s x_5 / 2) + (x_6 / 2) - (x_3 / m_s)) / C_s L_s \right) - \dot{\sigma} \quad (21)$$

The control variable, noted u_s , appears for the first time in (21). Let us consider the following Lyapunov function.

$$V_3 = V_2 + (z_3^2 / 2) \quad (22)$$

Using (20), the time-derivative of V_3 is given by:

$$\dot{V}_3 = -c_2 z_2^2 + z_3 (z_2 + \dot{z}_3) \quad (23)$$

To ensure that the (z_2, z_3) -system to be globally asymptotically stable, it is sufficient to choose the control law u_s so that $\dot{V}_3 = -c_2 z_2^2 - c_3 z_3^2$ which, due to (23), amounts to ensuring that:

$$\dot{z}_3 = -z_2 - c_3 z_3 \quad (24)$$

where c_3 is a positive parameter.

From the (21) and (24), we deduce the following backstepping control law u_s :

$$u_s = \left(2r_s x_4 - x_6 + (2x_3 / m_s) + 2C_s L_s (-z_2 - c_3 z_3 + \dot{\sigma}) / m_s \right) / x_5 \quad (25)$$

Remark: The control laws (10) and (25) involve a division by the DC bus voltage x_5 , there is no risk of singularity (division by zero) in steady state because, in practice, the DC bus voltage remains all the time positive. Otherwise, the two power converters of the UPFC system cannot work.

3.3. Voltage outer-loop design

According to the DC bus voltage regulation requirement, the outer-loop regulator generates an adjustment law for the signal β so that the DC bus voltage x_5 is regulated to its reference value x_5^* . To this end, the relation between β and the voltage x_5 is established see in Figure 2.

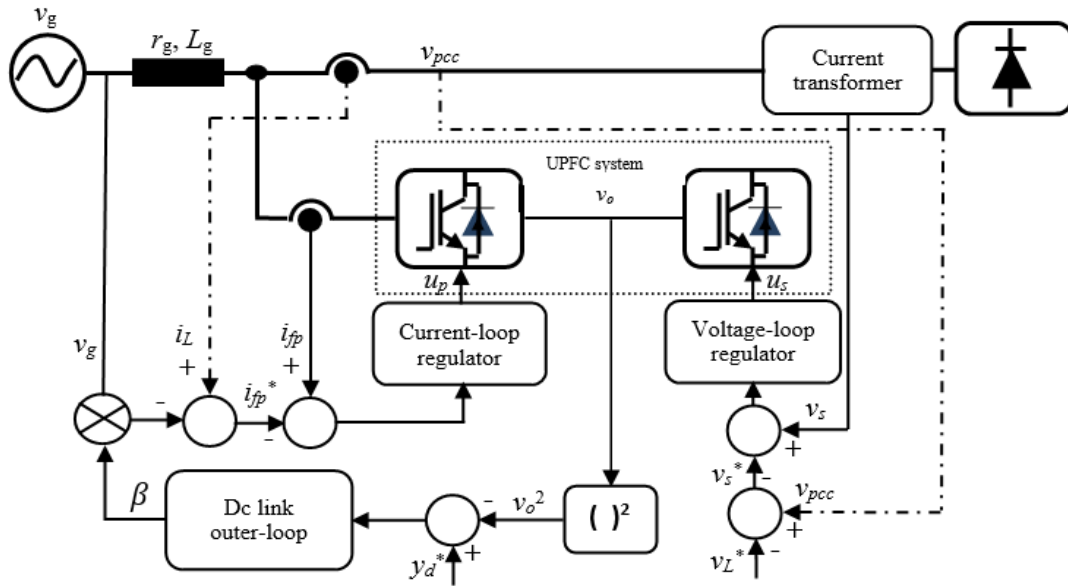


Figure 2. Synoptic scheme of the multi-loop nonlinear control of UPFC system

- The DC bus voltage x_5 varies, in response to the signal β , according (26a):

$$\dot{x}_5 = \left[K + f_1(\beta, \dot{\beta}, z_1, z_2, z_3) + f_2(\beta, \dot{\beta}, z_1, z_2, z_3, t) \right] / 2x_5 \tag{26a}$$

- Then, the squared-voltage $y_d = x_5^2$ varies, in response to the signal β , according to the following time-varying linear (26b):

$$\dot{y}_d = K + f_1(\beta, \dot{\beta}, z_1, z_2, z_3) + f_2(\beta, \dot{\beta}, z_1, z_2, z_3, t) \tag{26b}$$

with $K = (4V_{Lmax} I_1 \cos(\varphi_1) - 4E_1 I_1 \cos(\varphi_1) - 2r_p \sum_{h=1}^{\infty} I_h^2) / C_{dc}$

$$f_1(\beta, \dot{\beta}, z_1, z_2, z_3) = (4E_1 I_1 (r_g + r_p) \beta \cos(\varphi_1) + 2E_1 I_1 \beta L_g \omega_g (\cos(\varphi_1) + \sin(\varphi_1)) + 2\beta E_1^2) / C_{dc} - (2(r_g + r_p) \beta^2 E_1^2 / C_{dc}) - 2((L_g + L_p) \beta \dot{\beta} E_1^2 / C_{dc}) + (4z_1(-r_p z_1 - z_2 + L_p c_1 z_1^2) / C_{dc})$$

The expression of $f_2(\beta, \dot{\beta}, z_1, z_2, z_3, t)$ is complex and so is not cited in this paper.

The signal β stands as a control input of the system (26b). The problem is to design for β a tuning law so that the squared voltage $y_d = x_5^2$ tracks its reference $y_d^* = x_5^{*2}$. At this stage, the signal β and its first time-derivative must be available, the following filtered PI regulator is adopted:

$$\beta = c_6 (c_4 z_4 + c_5 z_5) / (c_6 + s) \tag{27a}$$

with $z_4 = y_d^* - y_d$ and $z_5 = \int_0^t z_4 d\tau$, where s denotes the Laplace variable, and the parameters

(c_4, c_5, c_6) , of the outer-loop regulator, are any positive real constants. The choice of these parameters will be clearly mentioned in the following analysis so that the control objectives are achieved. For now, let us note that (27a) implies that $\dot{\beta}$ can be computed using (27b):

$$\dot{\beta} = c_6 (c_4 z_4 + c_5 z_5 - \beta) \tag{27b}$$

4. CONTROL SYSTEM ANALYSIS

The following notations are needed to formulate the results:

$$\begin{aligned}
 k_2 &= c_6 k_1 - ((4E_1 I_1 (r_p + r_g) \cos(\varphi_1) + 2E_1 I_1 L_g \omega_g (\cos(\varphi_1) + \sin(\varphi_1)) - (2(r_p + r_g) \beta_o E_1^2 + 2E_1^2) / C_{dc})) \\
 z_6 &= \beta, \quad \varepsilon = 1/\omega_g, \quad k_1 = -2\beta_o E_1^2 (L_g + L_p) / C_{dc}, \\
 a_0 &= -c_1 c_2 c_3 c_5 c_6^2 k_1 - c_1 c_2 c_5 c_6 k_1 + c_1 c_2 c_3 c_5 c_6 k_1 + c_1 c_5 c_6 k_2, \\
 a_1 &= (-c_1 c_2 c_3 c_5 c_6 - c_1 c_4 c_5 c_6 - (c_1 + c_2) c_5 c_6 - (c_2 c_3 + c_1 (c_2 + c_3) + c_1 c_2 c_3 c_4) c_5 c_6^2) k_1, \\
 &\quad + (c_2 c_3 c_5 c_6 - c_1 (c_2 + c_3) c_5 c_6 + c_1 c_2 c_3 c_5 c_6 + c_5 c_6 + c_1 c_4 c_6) k_2, \\
 a_2 &= (c_4 c_6 - c_5 c_6 - c_1 (c_2 + c_3) c_5 c_6 - (c_1 + (c_2 + c_3) (1 + c_1 c_4) + c_2 c_3 c_4) c_5 c_6^2 - c_1 c_4 (c_2 c_3 c_6 + c_5)) k_1, \\
 &\quad + (c_2 c_3 c_5 c_6 + c_1 c_5 c_6 + (c_2 + c_3) c_5 c_6 + c_1 (c_2 + c_3) c_5 c_6) k_2 + c_1 c_2 c_3 c_6 + c_1 c_6 + c_4 c_5 c_6^2, \\
 a_3 &= c_5 c_6 k_2 - c_5 c_6^2 k_1 - c_5 c_6^2 (c_2 + c_3) + c_5 c_6 (c_2 + c_3) k_2 - c_5 c_6 (c_2 + c_3) k_1 - c_2 c_3 c_4 c_5 c_6 + c_2 c_3 c_6, \\
 &\quad - c_1 c_4 c_5 c_6^2 - c_1 c_5 c_6 k_1 + c_1 c_5 c_6 k_2 - c_1 (c_2 + c_3) c_4 c_6 k_1 + c_1 (c_2 + c_3) c_6 + c_1 c_2 c_3 + c_6 - c_4 c_5 c_6 k_1 + c_1 \\
 a_4 &= (c_5 c_6) k_2 - (c_5 c_6) k_1 - c_4 c_5 c_6^2 - c_4 c_5 c_6 (c_2 + c_3) + c_6 (c_2 + c_3) + c_2 c_3 - c_1 c_4 c_6 + c_1 (c_2 + c_3) + 1 \\
 a_5 &= c_1 + c_2 + c_3 + c_6 (1 - c_4 k_1).
 \end{aligned}$$

Theorem 1. We consider the single-phase UPFC system shown in Figure 1, represented by its average model (3a-f), in closed-loop with the nonlinear controller including the following components:

- The inner-loop regulator (10), where c_1 is any positive parameter.
- The intermediary-loop regulator (25), where c_2 and c_3 are any positive parameters.
- The outer-loop regulator (27a-b), where (c_4, c_5, c_6) are any positive parameters, the choice of which will be clearly done later.

Then, the global closed-loop control system has the following properties:

- The tracking error $z_2 = x_2 - x_2^*$ vanishes exponentially fast with $x_2^* = i_L - \beta v_{g1}$.
- The tracking errors $z_2 = x_3 - x_3^*$ and $z_3 = (m_s x_4 / C_s) - \sigma$ vanish exponentially fast with $x_3^* = v_{pcc} - v_L^*$.
- The augmented state vector $Z(t) = (z_1 z_2 z_3 z_4 z_5 z_6)^T$ undergoes state (28a):

$$\dot{Z} = f(t, Z) \quad (28a)$$

Where

$$f(t, Z) = \begin{bmatrix} -c_1 z_1 & (-c_2 z_2 + z_3) & (-z_2 - c_3 z_3) & (-K - f_1(Z) - f_2(Z, t)) & z_4 & c_6 (c_4 z_4 + c_5 z_5 - z_6) \end{bmatrix}^T \quad (28b)$$

- The control parameters $(c_1, c_2, c_3, c_4, c_5, c_6)$ are chosen so that the following inequalities hold:

$$\begin{aligned}
 b_1 &= a_5 a_4 - a_3, \quad b_2 = a_5 a_2 - a_1, \quad a_5 > 0, \quad b_1 > 0, \quad b_1 a_3 - b_2 a_5 > 0, \quad a_3 b_1 - a_3 a_5 b_2 - a_5 b_1 b_2 > 0, \quad a_0 > 0 \\
 &((a_3 b_1 - a_5 b_2) b_2) - (b_1^2 a_1 - a_5) > 0, \quad (((a_3 b_1 - a_5 b_2) b_2) - (b_1^2 a_1 - a_5)) \times \begin{pmatrix} (b_1 a_1 - a_0 a_5) \\ -(b_1 a_3 - b_2 a_5) a_0 \end{pmatrix} > 0
 \end{aligned} \quad (29)$$

Then, there exist positive constants ε^* and η^* such that for all $0 < \varepsilon < \varepsilon^*$, the system (28a-b) has a unique exponentially stable $(2\pi/\omega_g)$ -periodic solution $\bar{Z}(t, \varepsilon)$ with the property $|\bar{Z}(t, \varepsilon) - Z_0^*| \leq \eta^* \varepsilon$

(where $Z_0^* = (0 \ 0 \ 0 \ 0 \ \beta_0/c_5 \ \beta_0)^T$). With $\beta_0 = \frac{-k_4 - \sqrt{k_4^2 + 4 \times k_3 \times K}}{2 \times k_3}$, $k_3 = -2(r_p + r_g) E_1^2 / C_{dc}$, $k_4 = (4E_1 I_1 (r_g + r_p) \cos(\varphi_1) + 2E_1 I_1 L_g \omega_g (\cos(\varphi_1) + \sin(\varphi_1)) + 2E_1^2) / C_{dc}$

5. NUMERICAL SIMULATION

The control system described in Figure 2 is simulated using the MATLAB/SIMPOWER toolbox (V.R2013a). The controlled system is a single-phase UPFC which is connected between the disturbed power supply grid and the nonlinear load based on a bridge rectifier, the latter supplying a load composed of resistor R in series with inductor L . The inductor L_0 protects the bridge rectifier against abrupt voltage changes. The numerical values, of single-phase UPFC system parameters, are placed in Table 1.

Table 1. Single-phase UPFC system characteristics

Parameters of	Symbol	Values
Single-phase power grid	E_1, r_g, L_g	$220\sqrt{2}V/50 \text{ Hz}, 50m\Omega, 0.5 \times 10^{-6} H$
Single-phase UPFC system	$r_p, L_p, r_s, L_s, C_s, C_{dc}$	$80m\Omega, 3 \text{ mH}, 80m\Omega, 3 \text{ mH}, 500 \mu F, 9000 \mu F$
Nonlinear load (Bridge rectifier and RL circuit)	L_o, R, L	$5 \text{ mH}, 20 \Omega, 500 \text{ mH}$

5.1. Control performances in presence of harmonics at power grid voltage

The simulation vises at illustrating the controller behavior in response to step changes of the DC bus voltage reference v_0^* . Taking into account the system parameters values of Table 1, the simulation profile is described by Figure 3 which shows that the DC bus voltage reference switches from 800 V to 900 V at time (0.25 s) and return up to its nominal value at time (0.6 s) while the load is kept constant ($R=20 \Omega$, $L=500 \text{ mH}$). In this case, the circuit is supplying by a polluted power grid which its voltage contains the harmonics. The resulting controller performances are illustrated by Figures 3-10. The DC bus voltage v_0 converges to its reference value with a good accuracy see in Figure 3. Furthermore, it is observed that the voltage ripple oscillates at the frequency of $2\omega_g$, but its amplitude is quite small see in Figure 3 compared to the average value of the signal v_0 . Figure 4 shows the waveform of the load current i_L . It is seen that the latter presents a serious harmonic distortion. Figure 5 reveals a serious distortion in the voltage v_g of the power supply grid. Its calculated harmonic distortion rate is around $THDv_g(\%) = 24.58\%$, which recommends performing compensation. To better appreciate the controller performances, Figure 6 clearly shows that the grid current i_g remains sinusoidal all the time and in phase with the fundamental of the grid voltage namely v_{g1} . This confirms that a satisfactory PFC is well ensured. Also, Figure 7 shows that the voltage v_L , at the terminals of the nonlinear load after compensation, becomes sinusoidal. This confirms that the voltage perturbations compensation is well ensured. Figure 8 shows the load current spectrogram, where the THD value of this current equal to 32.04%. Figure 9 shows that the THD value of grid current after compensation is very low (3.82%). This latter value is below the limits of the IEEE-519 standard. Figure 10 shows the grid voltage spectrogram, where its THD value equal to 24.58%. Figure 11 shows that the THD value of load voltage after compensation is very low (0.68%). This latter value is below the limits of the IEEE-519 standard.

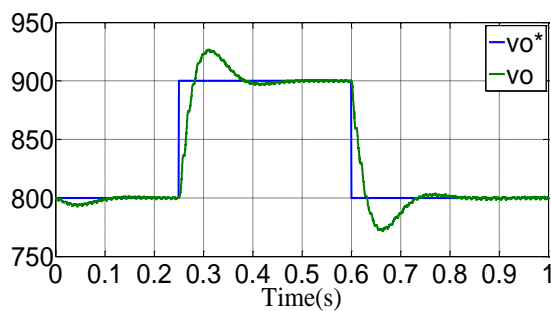


Figure 3. DC bus voltage and its reference

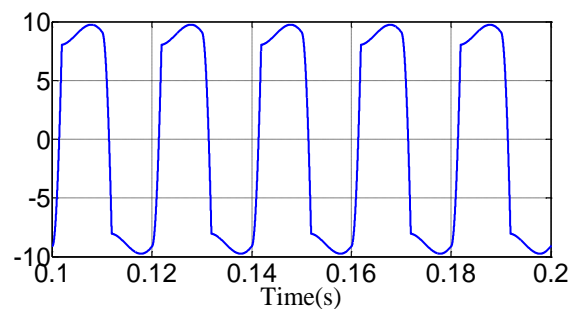
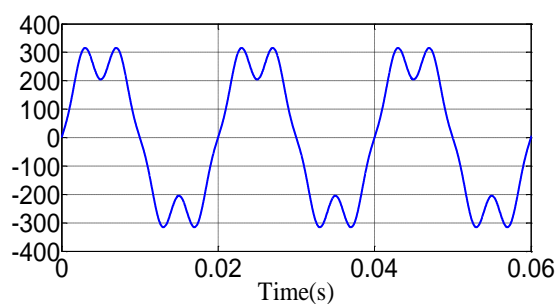
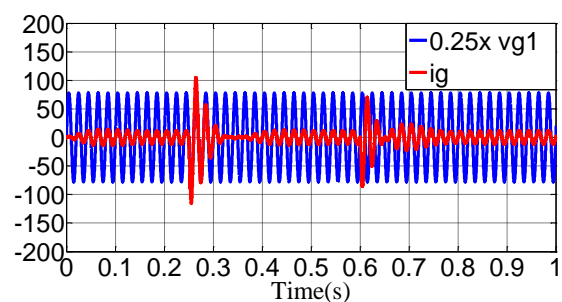
Figure 4. Load current i_L Figure 5. Distortion in the grid voltage v_g 

Figure 6. Current and fundamental voltage of grid

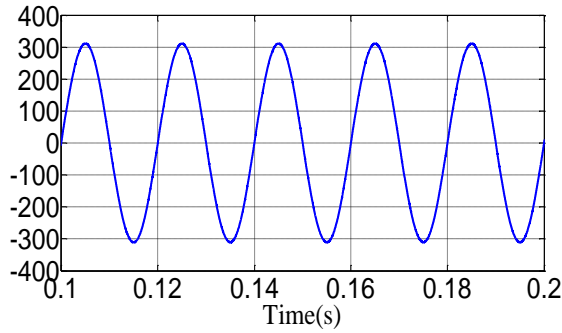


Figure 7. Load voltage after compensation

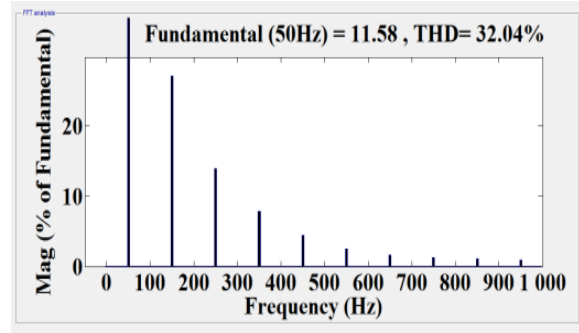


Figure 8. FFT analysis of load current

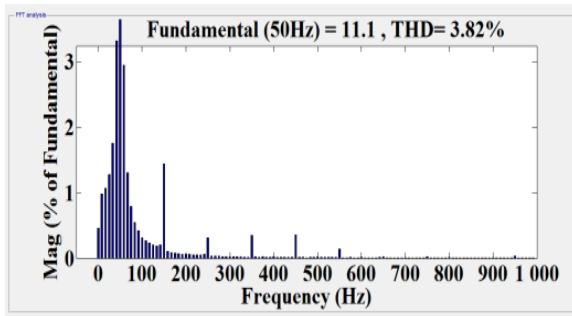


Figure 9. FFT analysis of grid current after compensation

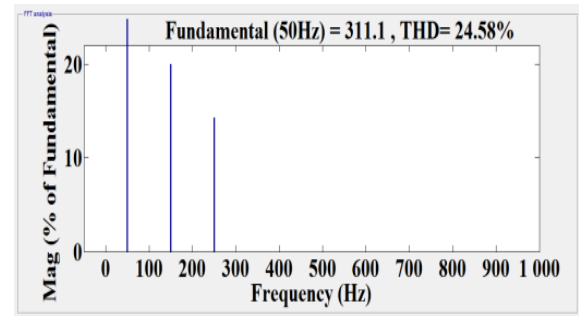


Figure 10. FFT analysis of grid voltage

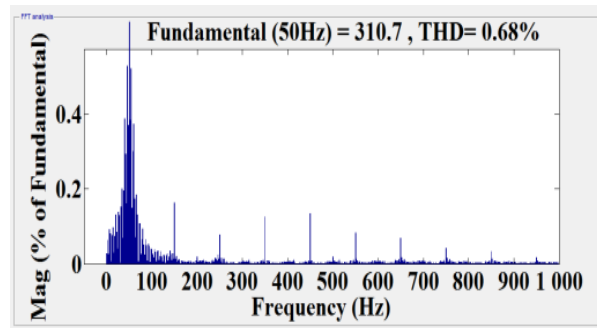


Figure 11. FFT analysis of load voltage after compensation

5.2. Control performances in presence of a sags at power grid voltage

Figure 12 to Figure 16 illustrating the behavior of the proposed controller in the presence of the voltage sags in the power grid. Indeed, Figure 12 reveals a sag in the signal of the grid voltage v_g , the depth of which is 90% of the nominal voltage and its duration is 100 ms, which exceeds the values fixed by the standard EN 50160. Figure 13 clearly shows that the grid current i_g remains sinusoidal all the time and in phase with the grid voltage v_g . This confirms that a satisfactory PFC is well ensured. As for Figure 14, it shows that the voltage v_L at the terminals of the nonlinear load after compensation is a sinusoidal signal, in this case the voltage sag decreases sharply and its depth becomes 7% which is less than the value of 10% imposed by standard EN 50160. The harmonics spectrum of the load current is plotted in Figure 15, it is noted that the THD value of this current equal to 32,04%. It is observed in Figure 16 that the THD value of grid current equal to 3.82%. This latter value is below the limits according to IEEE-519 standard.

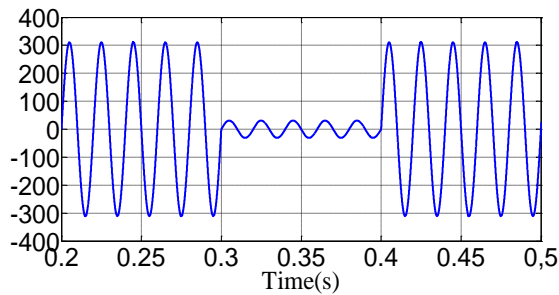
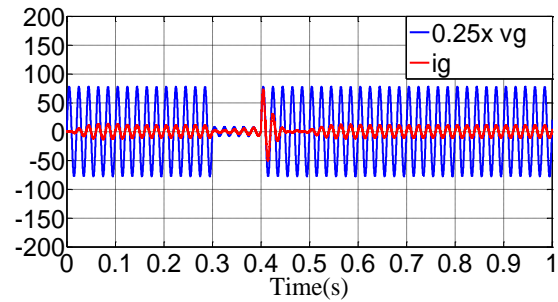
Figure 12. A sag in the signal of grid voltage v_g 

Figure 13. current and voltage of grid

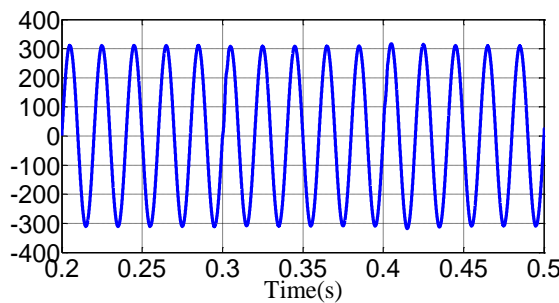


Figure 14. Load voltage after compensation

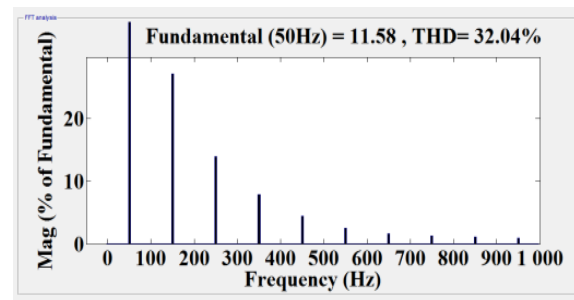


Figure 15. FFT analysis of load current

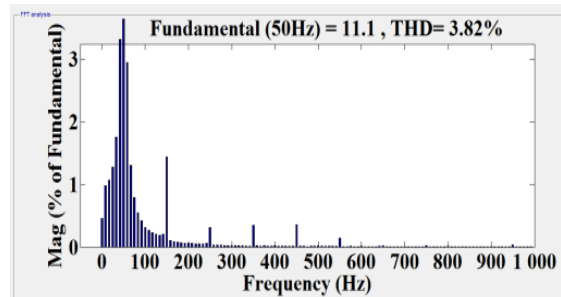


Figure 16. FFT analysis of grid current after compensation

6. CONCLUSION

The problem of controlling the single-phase UPFC system of Figure 1 is addressed in presence of disturbed single-phase power grid supplying nonlinear loads. The complexity of the control problem resides in the high dimension and the nonlinearity of the system dynamics. The proposed nonlinear controller, including the inner regulator (10), the intermediary regulator (25) and the outer regulator (27a-b), is developed by using various tools of control e.g. Lyapunov technique, Backstepping technique. It is shown that all control objectives are achieved, including PFC requirement, voltage perturbation compensation, and DC bus voltage regulation. The simulation results illustrate and prove the high performances of the proposed controller and its strongest robustness. The extension of the present study to the case of three-phase UPFC system is underway, and also an adaptive nonlinear control strategy taking into account the uncertainty on the grid impedance applied to single-phase UPFC system is underway.

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