Analysis of direct power control AC-DC converter under unbalance voltage supply for steady-state and dynamic response

Nor Azizah Yusoff, Azziddin M. Razali, Kasrul Abdul Karim, Raja Nor Firdaus Kashfi Raja Othman, Auzani Jidin, Nor Aishah Md Zuki, Nurfaezah Abdullah
Faculty of Electrical Engineering, Universiti Teknikal Malaysia Melaka (UTeM), Malaysia

This paper presents an analysis of Direct Power Control (DPC) technique for the Three-Phase Pulse Width Modulation (PWM) AC-DC converter under unbalanced supply condition. Unbalance condition will cause the presence of unbalanced current and voltages thus produce the negative components on the grid voltage as well as severe performance degradation of a grid connected Voltage Source Inverter (VSI). The input structures for conventional DPC has been modified with a three simpler sequence networks instead of coupled by a detailed Three-Phase system method. The imbalance voltage can be resolved by separating from the individual elements of voltage and current into symmetrical components called Sequence Network. Consequently, the input power relatively improved during unbalanced condition almost 70% through the measurement of Total Harmonic Distortion (THD) from the conventional Direct Power Control (DPC) in individual elements which is higher compared to separate components. Hence, several analyses are performed in order to analyze the steady state and dynamic performance of the converter, particularly during the load and DC voltage output reference variations.

1. INTRODUCTION
Power converter is necessary especially in AC and DC motor control circuits and acts as the link or the transforming stage between the power source and the power supply output [1]. There are several mains of converters based on the source of input voltage and the output voltage and these falls into four categories namely the AC-DC converter known as the rectifier, the DC-AC that named as inverter, the AC-AC converter or frequency changer, and lastly the DC-DC voltage or current converter. Each has its advantages and drawbacks, which determines the suitability for any specific application [2]. However, this research is approach for AC-DC converter for more specific and concern.

AC-DC converter plays an important role in many power electronics system. The vast application of this converter leads to the development of many control techniques. The example of control techniques covers hysteresis current control (HCC), voltage-oriented control (VOC) which similar to the Field Oriented Control (FOC) and Direct Power Control (DPC) which imitates the basic idea of Direct Torque Control (DTC). Each control technique has its own way of controlling the power converters as a result their aims to reduce the harmonics up to some limit [3].

However, these advanced features of PWM AC-DC converters are not fully achieve under the unbalanced three-phase input supply [4]. Thus, it indicates to harmful to all polyphase loads, especially
three phase induction machines. Otherwise, unbalance system is produce excessive heat causing to equipment failures. Although various faults in the utility line tend to happen in a few second, this fault or disturbance at grid side may introduce significant unbalanced operating conditions [5]. Unbalanced three-phase input supply both in magnitude and in phase is quite common in power system, particularly in a weak AC system [6]. Usually, the non symmetrical transformer windings in a distribution can cause to unbalanced input supply conditions. Indirectly, it has been shown that unbalanced input voltages implies for the appearance of negative sequence in voltage and current thus leads to the oscillation of system variable [7]. Therefore, a PWM AC-DC converter under unbalanced operating conditions necessitates the use of filters to reduce the harmonics at the AC input side respectively. Thus, to achieve a lower disturbances and enhanced power quality by eliminate the harmonics under unbalanced voltage input supply, a few solutions have been approach in these cases. As a result, it is essential to have an adequate model to deal with the negative sequence input voltage as well as positive sequence input voltages.

Subsequently, this paper is mainly focussing on the Direct Power Control (DPC) strategy, which it based on the instantaneous of active and reactive power control loops [8, 9]. However, conventional approaches of DPC cannot be applied for generalized unbalanced operating conditions. In this paper, DPC is modified to manage power flow during unbalanced voltage supply so that sinusoidal balanced grid currents are obtained. With this new strategy, DPC overcomes the problems related to grid voltage imbalance and can accomplished new regulation laws. At the end of this paper, the converter performance will be evaluated under steady state and dynamic conditions. The converter’s dynamic study is performed by evaluating the transient response during the magnitude variations of DC voltage reference and load resistance.

2. BASIC STRUCTURE DIRECT POWER CONTROL

The Direct Power Control (DPC) is based on the Direct Torque Control (DTC) concept in electrical machines. The intention for DPC is to control the instantaneous of active and reactive power control loops [10] as the same direction for DTC in controlling the torque and flux of induction machines. In this DPC scheme as shown in Figure 1, switching table plays a major part [11]. The input to the switching table will be the instantaneous error of the active power \( dP \), reactive power \( Dq \) and the voltage vector position \( \theta_n \) as shown in Table 1. This switching table enables the converter to select the appropriate of switching states.

![Figure 1. Control structure of direct power control](image)

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In conventional DPC, a total of four voltage sensors are used to measure the three-phase AC input voltage and DC output voltage, while three current sensors are used to measure the three-phase input currents [12]. Then, the measured currents and voltages are fed into two “αβ-αβ” blocks which utilize the Clarke Transformation. Both blocks transform the three-phase voltage and current into their corresponding αβ-reference frame. The transformation matrix to the stationary frame is utilized by referring the equation in (1). The three-phase input components are represented by $x_a$, $x_b$, and $x_c$ while $x_α$ and $x_β$ indicate two-phase components in αβ-reference frame. The angle of supply voltage vector is divided into 12 sector and each sector is $30^\circ$ wide as shown in Figure 2.

\[
\begin{bmatrix}
1 & -\frac{1}{2} & -\frac{1}{2} \\
0 & \frac{\sqrt{3}}{2} & -\frac{\sqrt{3}}{2}
\end{bmatrix}
\]

\[
P_{\text{inst}} = \frac{3}{2} [V_αI_α + V_βI_β]
\]

\[
Q_{\text{inst}} = \frac{3}{2} [V_βI_α - V_αI_β]
\]
2.1. Development of switching table for DPC
In DPC, the digitized signal $\theta_n$ calculate from the phase of voltage vector, which it measured from the three-phase power source using (4). From the equation, the alpha-betha stationary-frame is obtained from the positive sequence.

$$ \theta_n = \tan^{-1} \left( \frac{V_{\beta}}{V_{\alpha}} \right) $$  \hspace{1cm} (4)

The switching table in the circuit simulation is creating using “Matlab Function” block. The active power error, $\Delta P$ and reactive power error, $\Delta Q$ are fed into two hysteresis blocks to obtain the active and reactive power errors status given by $d_F$ and $d_Q$ respectively.

3. POWER ANALYSIS UNDER UNBALANCE GRID VOLTAGE
However, although DPC offer simple control structure and fast dynamic response, it generates high ripples and higher number of Total Harmonic Distortion (THD) during imbalanced input voltage [15, 16]. In order to make the controller to be more robust in such cases, investigations of power converters under unbalanced input voltage conditions are presented in references [17]. The interaction between the harmonic components of the DC output voltage and the converter pole voltages creates even-order harmonics at the DC output and odd-order harmonic components in the input AC current of the PWM AC-DC converter. Consequently, these harmonics components will increase the THD of the AC input current significantly [18, 19].

In general, the non-ideal conditions such as unbalanced and distorted three-phase grid voltage supply have negative impacts to the performance and filter size of AC-DC converter system [20, 21]. Therefore, PWM AC-DC converters under unbalanced operating conditions require the use of input or output filters of a large size to reduce even and odd-order harmonics at the DC output and AC input supply [22, 23]. Hence, the control techniques of an AC-DC converter need additional investigation to mitigate those negative impacts during voltage unbalance and distorted conditions [24]. For that, it is necessary to split the voltage vector into its sequence components as well as to compute the positive sequence voltage vector angle [25]. Voltage angle calculation is done by means of a PLL while a very simple algorithm is used for sequence extraction.

3.1. Sequence extractor
As in introduction part, it was explained that an unbalance input supply has causing negative or zero sequence voltage component as well as a positive sequence voltage component on the grid voltage vector. Therefore, negative sequence component was introduced to the input current in order to adequately compensate for the unbalanced operating condition so that the instantaneous active power becomes constant without oscillating components. The unbalanced detector and symmetrical component equation that acquires the positive and negative sequence component from three-phase instantaneous quantities such as voltage and current is regarded as an important functional part of the entire unbalance compensation control system. Hence, positive and negative sequence equations as shown in Table 2 will be applied in this research work in order to generate or extract a negative sequence from the input supply which known as sequence extractor.

<table>
<thead>
<tr>
<th>Table 2. Sequence extractor equation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Phase Component</td>
</tr>
<tr>
<td>------------------</td>
</tr>
</tbody>
</table>
| Zero Sequence    | \[
| V_s^{(0)}       | \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} V_s' |
| V_s^{(b)}       | \begin{bmatrix} a & a^2 & 1 \\ a^2 & 1 & a \\ 1 & a & a^2 \end{bmatrix} V_s' |
| V_s^{(c)}       | \begin{bmatrix} a^2 & a & 1 \\ a & 1 & a^2 \\ 1 & a^2 & a \end{bmatrix} V_s' |
| Positive Sequence| \begin{bmatrix} 1 & a & a^2 \\ a & 1 & a \\ a^2 & a & 1 \end{bmatrix} V_s' |
| Negative Sequence| \begin{bmatrix} a & a^2 & a \\ a^2 & a & a \\ a & a^2 & a \end{bmatrix} V_s' |

Where,
\[ a = e^{j2\pi} = -\frac{1}{2} + j\frac{\sqrt{3}}{2} \]
and
\[ a^* = e^{-j2\pi} = -\frac{1}{2} - j\frac{\sqrt{3}}{2} \]

Then, in Figure 3 has shown the block diagram for sequence extractor for from three-phase input supplies. From the figure, the input supply has been extracted into three-phase component, which is voltage and current in zero component \((V^{0}_a, V^{0}_b, V^{0}_c)\), positive \((V^{(+)a}, V^{(+)b}, V^{(+)c})\) component, and negative \((V^{(-)a}, V^{(-)b}, V^{(-)c})\) component. The extraction block diagram is creating based on the matrix equation as can be seen in Table 2. Next, the phase of input voltage and current from phase sequence are being transformed into alpha-beta stationary-frame. Lastly, the stationary-reference frame from only positive and negative sequence is then fed into another block in order to obtain the estimated instantaneous active power, \(P_{out}\), and reactive power, \(Q_{out}\).

![Block Diagram](image)

**Figure 3.** Block diagram for sequence extractor

The instantaneous of the input power \(P\) and reactive power \(Q\) in a stationary reference frame is given by (5) and (6), respectively.

\[
P_{out}(t) = \frac{3}{2} (v_{a}^{i}i_{a}^{o} + v_{b}^{i}i_{b}^{o} + v_{c}^{i}i_{c}^{o} + v_{a}^{i}i_{b}^{o} + v_{b}^{i}i_{a}^{o} + v_{a}^{i}i_{c}^{o} + v_{b}^{i}i_{c}^{o} + v_{c}^{i}i_{a}^{o} + v_{a}^{i}i_{b}^{o} - v_{b}^{i}i_{a}^{o} - v_{c}^{i}i_{b}^{o} - v_{a}^{i}i_{c}^{o} - v_{b}^{i}i_{c}^{o} - v_{c}^{i}i_{a}^{o} - v_{a}^{i}i_{b}^{o})
\]

\[
Q_{out}(t) = \frac{3}{2} (v_{a}^{i}i_{o}^{i} - v_{b}^{i}i_{o}^{i} - v_{c}^{i}i_{o}^{i} + v_{a}^{i}i_{o}^{i} - v_{b}^{i}i_{o}^{i} - v_{c}^{i}i_{o}^{i} + v_{a}^{i}i_{o}^{i} + v_{b}^{i}i_{o}^{i} + v_{c}^{i}i_{o}^{i} + v_{a}^{i}i_{o}^{i} + v_{b}^{i}i_{o}^{i} + v_{c}^{i}i_{o}^{i})
\]

### 4. RESULT AND DISCUSSION
Voltage unbalance is often occurring in supply system [26]. Therefore, the unbalance voltage can be defining as a voltage variation in a power system in which the voltage magnitudes or the phase differences between them are not equal [27, 28]. Hence, in order to confirm the effectiveness of the additional strategy of sequence extractor into DPC control system, a model of the proposed control strategy for DPC during
voltage unbalance has been simulated using MATLAB/Simulink. The simulation has been carried out using the main electrical parameter data used in the study is tabulated in Table 3. Several tests were conducted to verify the feasibility and performance of new DPC combining with sequence extractor compared to the conventional one during unbalanced conditions.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Input phase voltage (peak), $E_g$</td>
<td>70.71 V</td>
</tr>
<tr>
<td>Source Voltage frequency, $f$</td>
<td>50 Hz</td>
</tr>
<tr>
<td>DC-link voltage reference, $V_{dc,ref}$</td>
<td>200 V</td>
</tr>
<tr>
<td>Resistance of reactance, $R$</td>
<td>0.2 Ω</td>
</tr>
<tr>
<td>Inductance of reactance, $L$</td>
<td>18 mH</td>
</tr>
<tr>
<td>DC-link capacitor, $C$</td>
<td>10.8 mF</td>
</tr>
<tr>
<td>Load Resistance, $R_L$</td>
<td>140 Ω</td>
</tr>
<tr>
<td>Sampling time, $t_s$</td>
<td>20 µs</td>
</tr>
</tbody>
</table>

Simulation result of the three-phase PWM rectifier operation for unbalanced input voltage under conventional DPC is shown in Figure 4 below. In this case, the unbalance voltage supply can be seen into phase a where the amplitude had been pre-set 50% from input phase peak voltage, 70.71 V as shown in Figure 4(a) [29]. Thus, the reducing amount of voltage has resulting the value of current on phase a into an excessive amount as shown in Figure 4(b), which the current for $I_a$ is greater compared than other phases. Consequently, it resulting for a higher number of Total Harmonic Distortion (THD=22.7%) as shown in current spectrum in 4(c). It proves that, the input current in unbalance condition is highly distorted.

![Figure 4](image-url)

Figure 4. Simulation result for conventional DPC of PWM AC-DC Converter under unbalanced input voltage (a) Input voltage, (b) Input current, (c) FFT Analysis on phase $a$

Then, in Figure 5 has shown the entire results of the three-phase PWM rectifier operation under additional of sequence extractor method into DPC. It verifies that this method is capable to improve the current waveforms nearly too almost sinusoidal waveform as shown in 5(a) [30]. Accordingly, it resulting for a lower number of Total Harmonic Distortion (THD=6.48%) as shown in 5(b) and $P$ and $Q$ waveform in 4(c).
Then, the output of DC voltage is obtained in 5(d) and it can be seen that there is an increment in rising time and settling time before the output voltage reaches the steady state. This is due to the tuning of PI controller which involves increasing value of \( K_p \) and \( K_i \).

![Figure 5](image)

**Figure 5.** Simulation results for additional of sequence extractor into DPC of PWM AC-DC Converter under unbalanced input voltage, (a) Input current, (b) Harmonic spectrum on phase \( a \), (c) Active and reactive power, (d) DC voltage

Figure 6(a) shows transient response when the DC voltage reference changes from 150V to 180V and back to 150V at 3s while 6(b) from 150V to 120V and back to 150V. With the estimated quantities of the dc-link voltage \( PI \) regulator, the control performance is satisfactory. Figure 7 shows transient response during load variation. The load variation is performed by connecting abruptly a 100Ω resistor in parallel with the existing resistor across the dc-link at the time of 3s, to cause a sudden disturbance in the load current. The line current and estimated active power, immediately follow the change on the active power reference. The response occurs very quickly without any undesirable overshoot and oscillation. Forced by the voltage \( PI \) regulator, the dc output voltage recovers to the original value of 150V after experiencing a small dip.
Figure 6. Transient response for the step changes of DC-link voltage, (a) 150V to 180V, (b) 150V to 120V

Figure 7. Transient response for load variation from low to high current demand; (a) Phase $a$, (b) DC-link voltage, (c) Estimated active and reactive power

5. CONCLUSION

This paper has presented the implementation of a sequence extractor into Direct Power Control scheme. The main goal for the additional strategy of sequence extractor is to achieve for near-sinusoidal input current waveform of the converter under different amplitude input voltage conditions. In-fact, instantaneous active and reactive powers provided by harmonic component of input current are directly controlled via a switching table. Simulation result has proven excellent performance of the proposed additional strategy of sequence extractor, which is much better than conventional DPC by reducing almost for 70% of Total Harmonic Distortion (THD), even in both transient and steady states conditions. Nearly sinusoidal waveform of input current is successfully achieved under unbalance input voltage conditions. The presented simulation results confirm that the additional of sequence extractor into DPC is capable to ensure the correcting unbalance of input voltage, unlike the conventional DPC is resulting for decreasing percentage of productive current, thus it providing for high number of THD current. Then, in study for the dynamic performance for the variation in load and DC voltage reference, it is observed that the output
voltage recovers close to the reference voltage despite the sudden disturbance introduced to the system. The proper tuning of PI controller enables the output voltage remains near to reference voltage. Meanwhile, the active power increases significantly when a smaller resistance value is connected parallel with existing circuit which reduces the overall load.

ACKNOWLEDGMENT
The authors would like to thank ‘Skim Zamalah’ from Universiti Teknikal Malaysia Melaka (UTeM) as providing for continuous financial support that enabled the achievement of this research result and research incentive grant (Jurnal/2019/FKE/Q00016).

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